

# Non-equilibrium many-body physics with alkaline earth atoms and polar molecules

Ana Maria Rey



**JILA**  
NIST/UCU

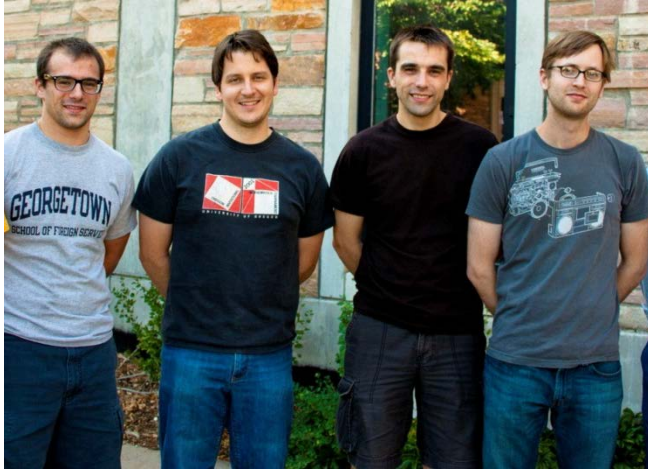
\$ Funding \$

NSF, AFOSR, ARO,  
ARO-DARPA-OLE,

**The 11th US-Japan Joint Seminar 2013**

“Ultimate Quantum Systems of Light and Matter- Control and Applications”

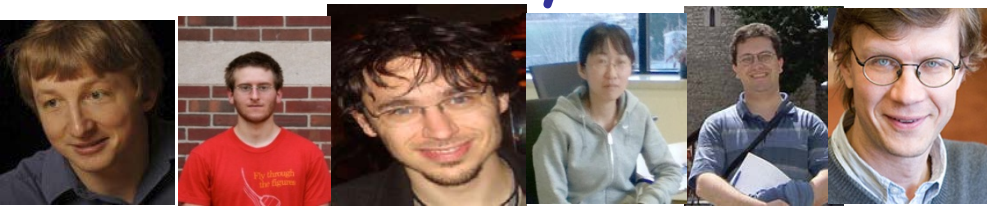
# The Sr team:



Jun Ye

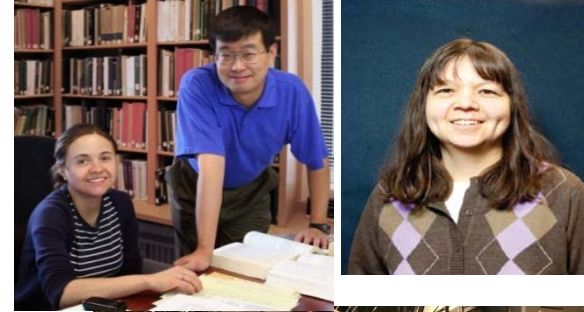
M. Swallows, M. Martin, M. Bishof, S. Blatt, X. Zhang, C. Benko

# Theory team:

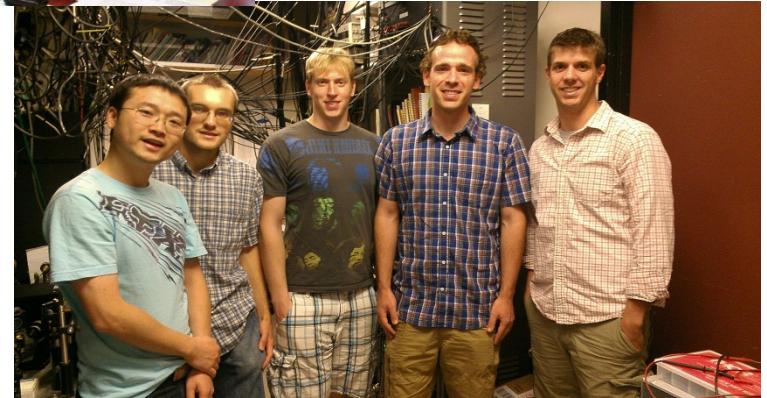


A. Gorshkov, M. Foss-Feig, K. Hazzard, B. Zhu, S. Manmana, M. Lukin

# KRb team:



D. Jin



B. Yan, S. Moses, J. Covey, B. Neyenhuis and B. Gadway

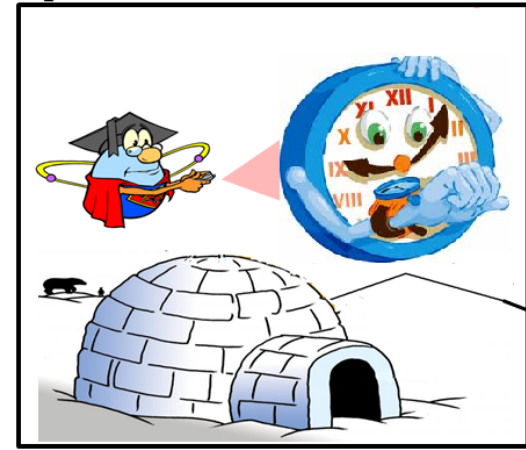


# Ultra-cold Matter

- Fully controllable quantum systems

The most precise measurements,  
e.g. clocks

Quantum sensors



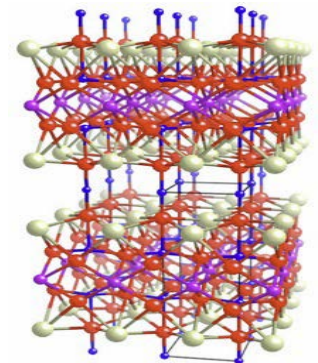
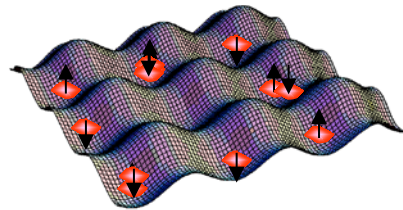
- A tool for understanding quantum complexity

Quantum simulation

## Atomic Simulator



Richard Feynman

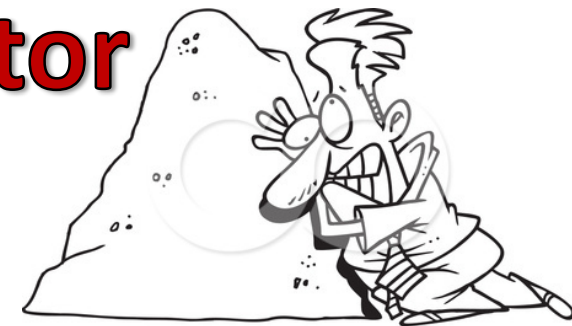


Atoms  $\leftrightarrow$  Electrons

Optical lattice  $\leftrightarrow$  Ionic Crystal

# Ultra-cold atomic Simulator

Possible but challenging



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Atoms heavier than electrons

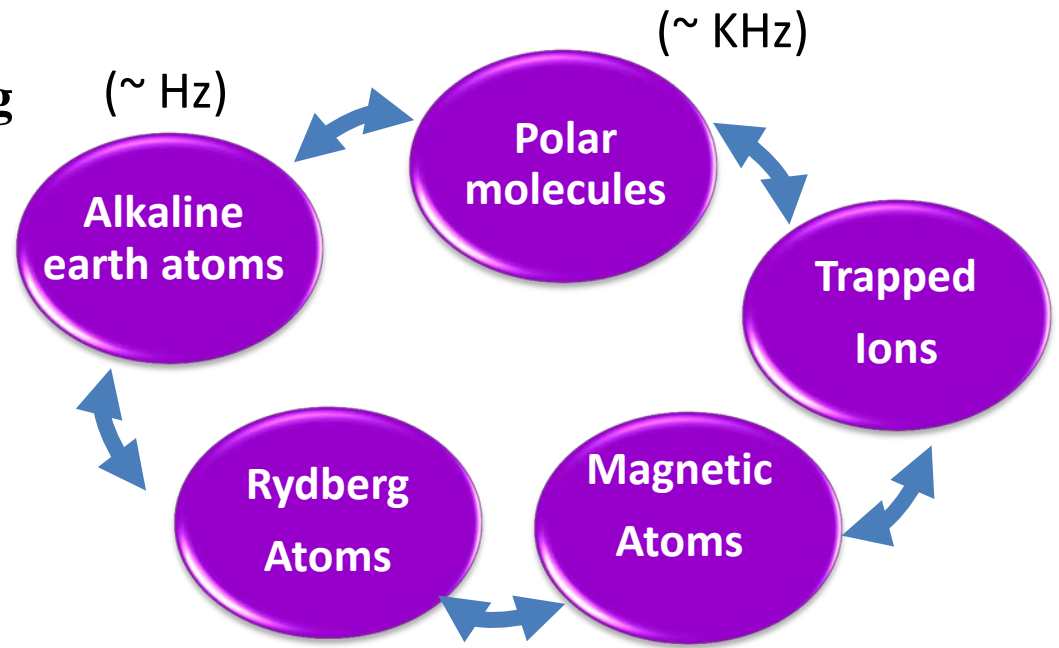
Optical lattice spacing much larger than ionic lattice spacing

Extra low temperatures

$10^{-11}$  K in atomic systems ~ K in solid state systems

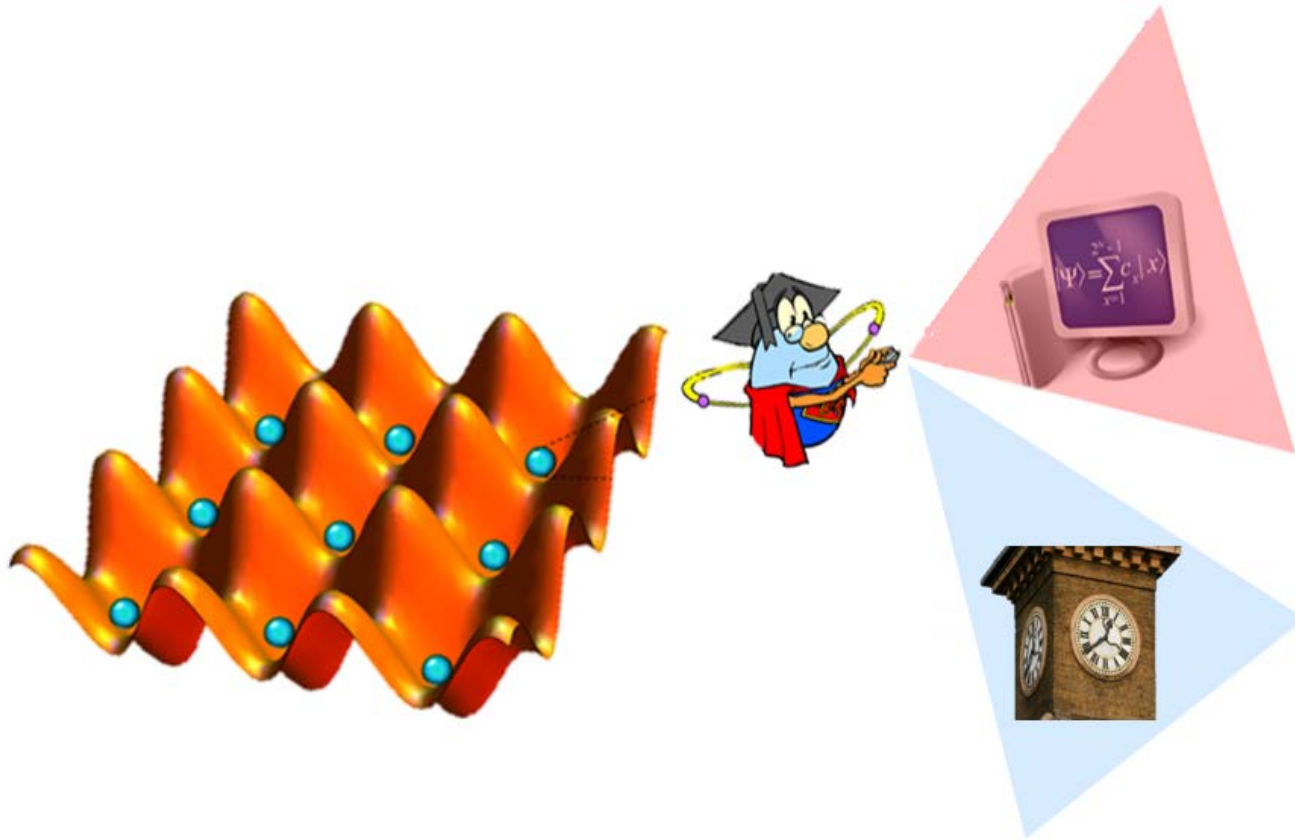
## Solutions

- Develop sophisticated cooling methods
- Explore new type of systems
- Take advantage of ultra-precise tools



# Many body physics with clocks

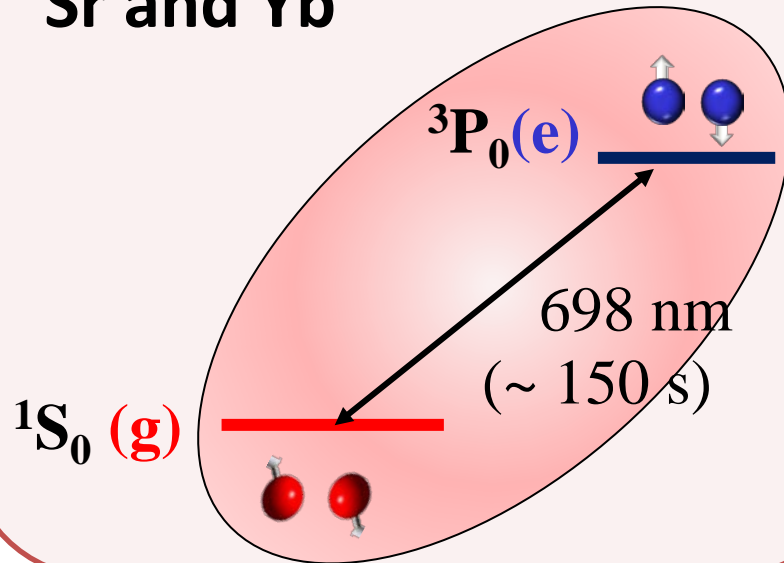
Understanding quantum systems from few- to many-body  
with “clock” precision and control



# Alkaline earth - super coherence

Metastable state

Sr and Yb

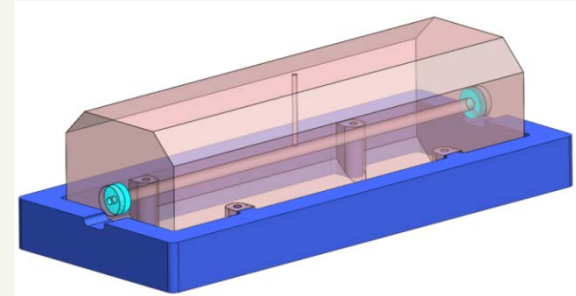


JILA Ultra-coherent spectroscopy:

Nicholson *et al.*, Phys. Rev. Lett.  
109 (2012) 230801

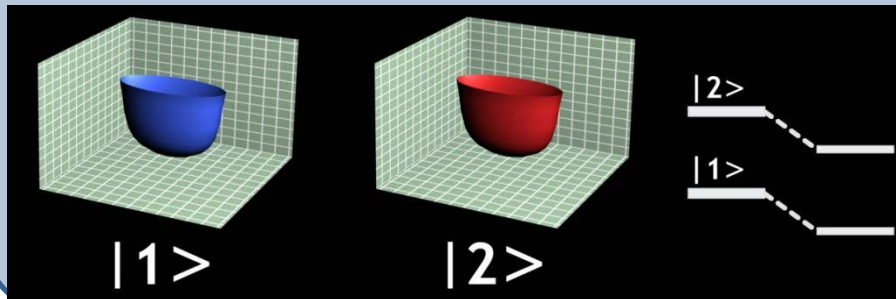
Ye's talk this afternoon

$Q \sim 10^{15}$ , seconds coherence time



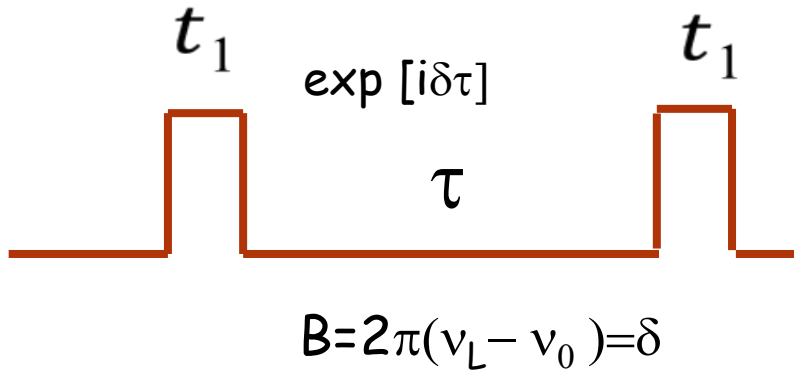
Magic wave length

Ye, Kimble, & Katori, Science **320**, 1734 (2008).



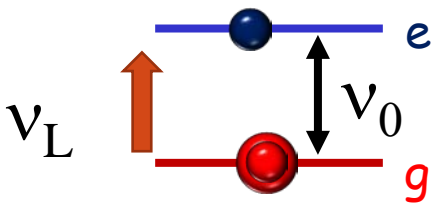
No Doppler, No Recoil  
No Stark shift

# Ramsey Spectroscopy

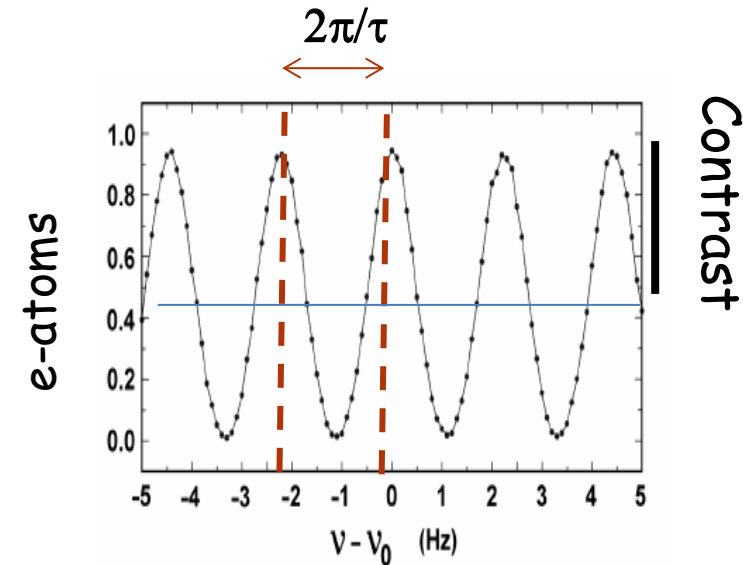
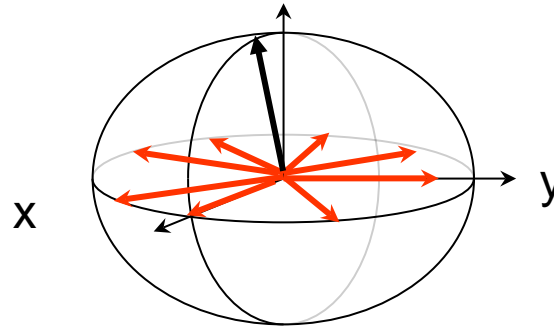
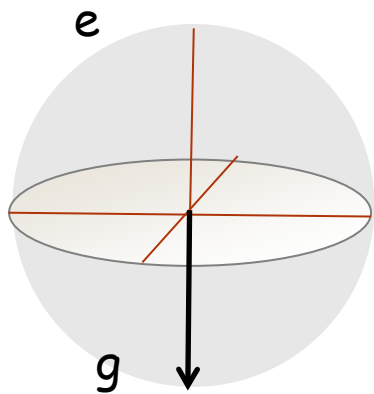


Measure # of e atoms

N. Ramsey. Nobel prize 1989



$\delta$ : Detuning

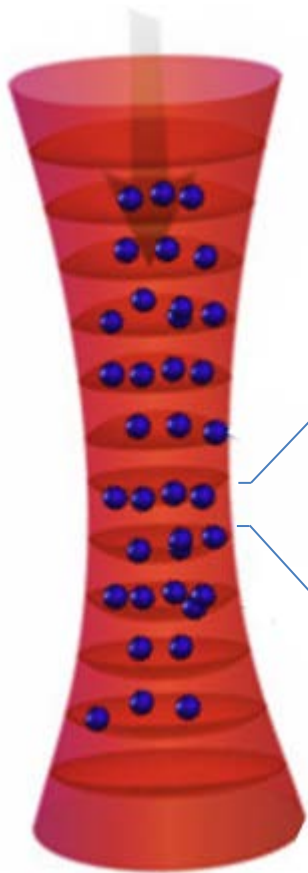


What happens in the real experiment with N particles?

Non-interacting: Collective-spin  $S = N/2$   $S_{x,y,z} = \sum_n S_n^{x,y,z}$  Interactions?

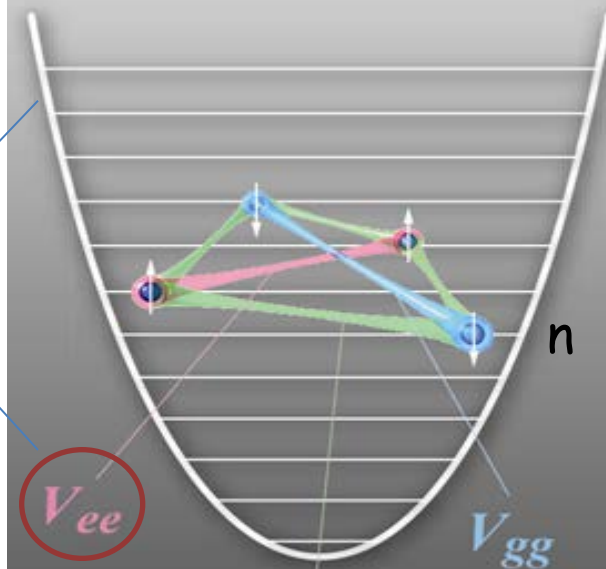
# $^3P_0(e)$ $\uparrow$ **1D lattice clock: @ $T \sim \mu K$**

$^1S_0(g)$   $\downarrow$  Effective spin 1/2 system during clock interrogation



Array of pancakes

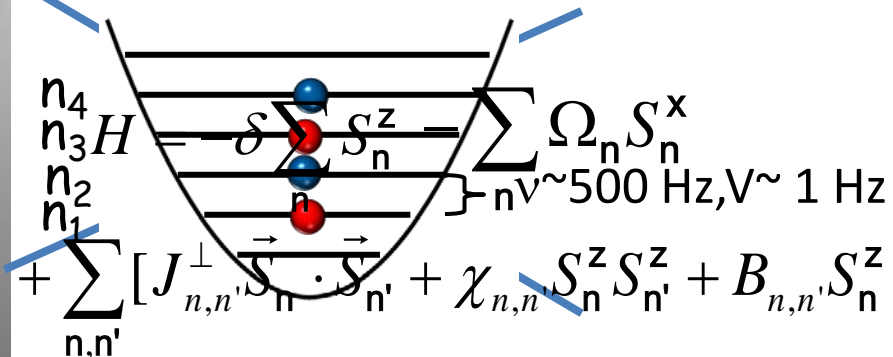
Dominant p-wave collisions  
Both elastic and inelastic



$V_{ee}$   
 $V_{eg}$   
 $V_{gg}$   
 $v \sim 500$  Hz  
**reactive**

Mode occupation is conserved. No laser/interaction induced mode changing collisions.

Decoupled motional/spin



$\delta$ : Detuning

$\Omega_n$ : Rabi Frequency

Interaction parameters

$$J_{n,n'}^\perp = (V_{n,n'}^{eg} - U_{n,n'}^{eg})$$

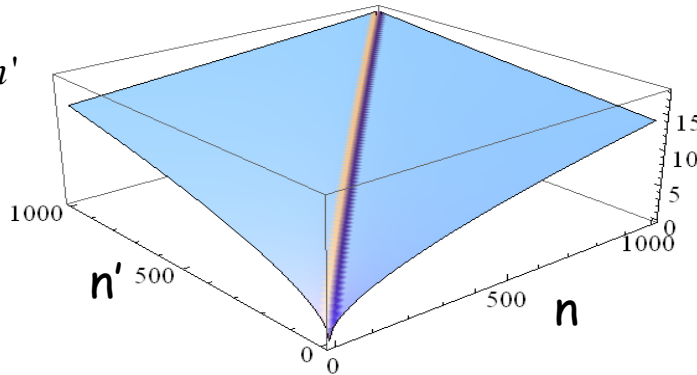
$$\chi_{n,n'} = (2V_{n,n'}^{eg} - V_{n,n'}^{ee} - V_{n,n'}^{gg})$$

$$B_{n,n'} = (V_{n,n'}^{ee} - V_{n,n'}^{gg})$$



# Spin Model: Collective Mode approximation

$$J_{n,n'}^\perp, \chi_{n,n'}$$



$$J_{n,n'}^\perp, B_{n,n'}, \chi_{n,n'} \rightarrow \bar{J}^\perp + \Delta J_{n,n'}^\perp,$$

$$\bar{B} + \Delta B_{n,n'}$$

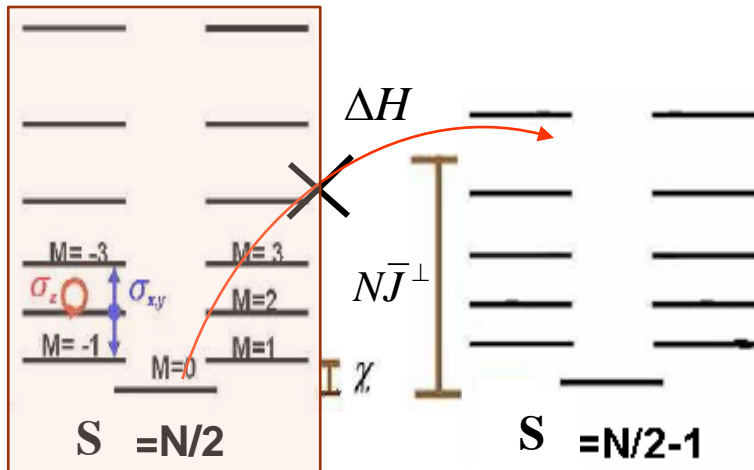
Long range!!

$$\bar{\chi} + \Delta\chi_{n,n'}$$

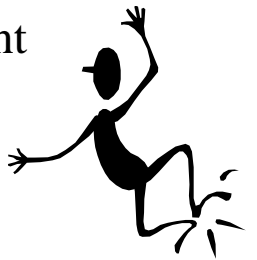
constant

$$H = -(\delta - (N-1)\bar{B})S_z - \bar{\Omega}S_x + \bar{J}(\vec{S} \cdot \vec{S}) + \bar{\chi}S_z^2 + \sum_{n,n'} \Delta H_{n,n'}$$

$$S_{x,y,z} = \sum_n S_n^{x,y,z}$$

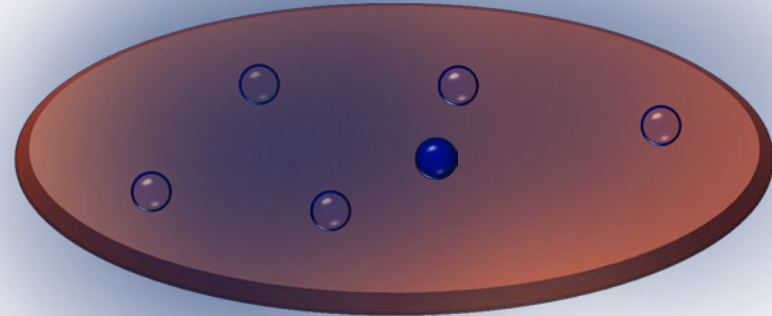
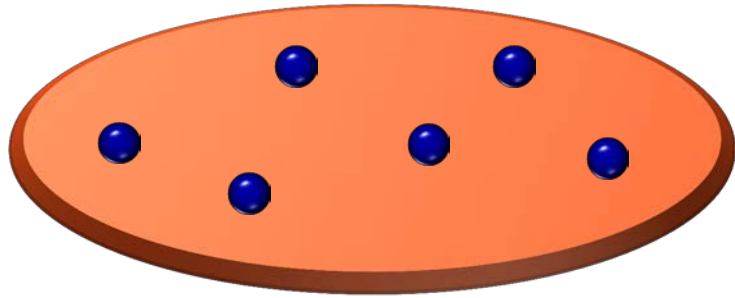


Same Hamiltonian that two component Bose Einstein Condensate: Sorensen, Moller, Cirac, Zoller, Lewenstein, ...



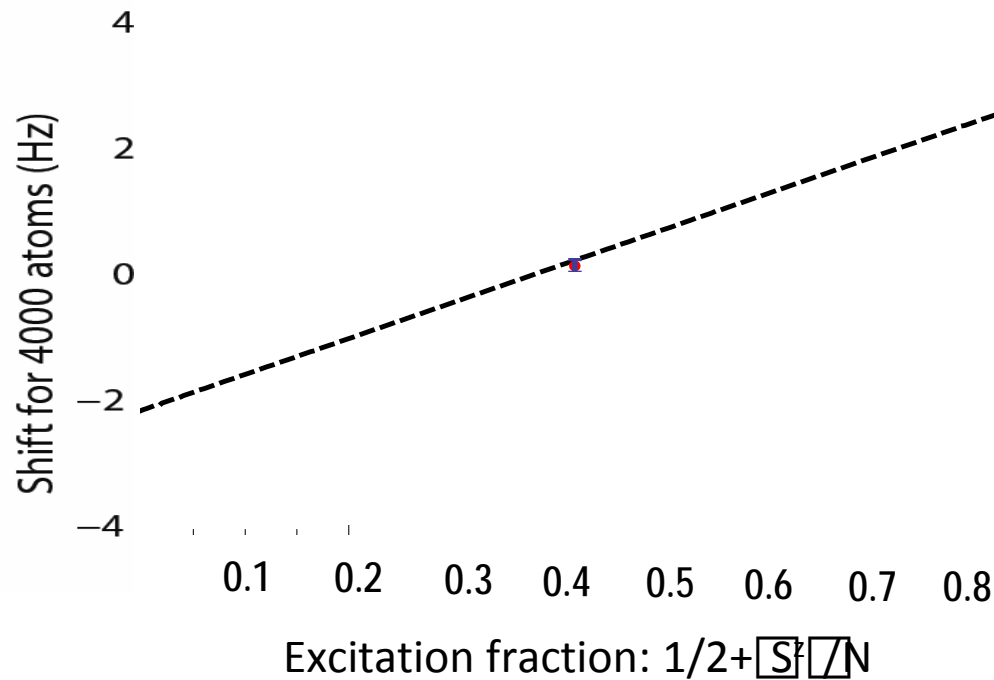
# Mean Field

Treat other surrounding atoms as an average

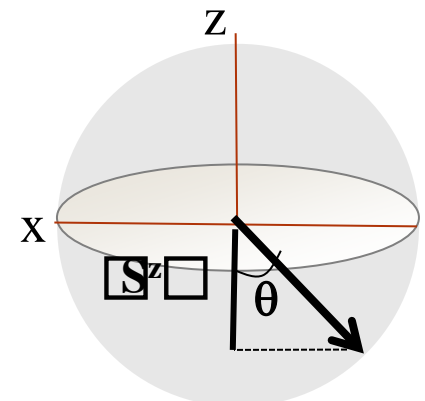


$$H = -\sum_i (S^z_i)^2 \rightarrow 2 \sum_i S^z_i \sum_j S^z_j \equiv B S^z$$

$$B = -2 \sum_j S^z_j \equiv -N \langle S^z \rangle \cos \theta$$



Spin precesses with a modified rate with depends on atom number



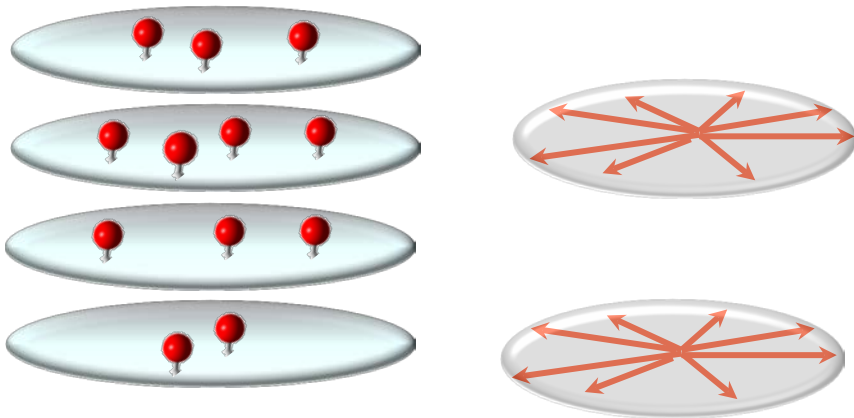
$\theta$  controlled by first pulse

# Quantum correlations – beyond mean field

Quantum correlations should manifest on the amplitude of the oscillations

- At the mean field level interactions only affect the precession rate.
- Amplitude remains constant

But..... in the experiments there are many pancakes with different atom number. Due to interactions the pancakes with more atoms precess faster.



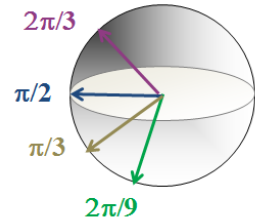
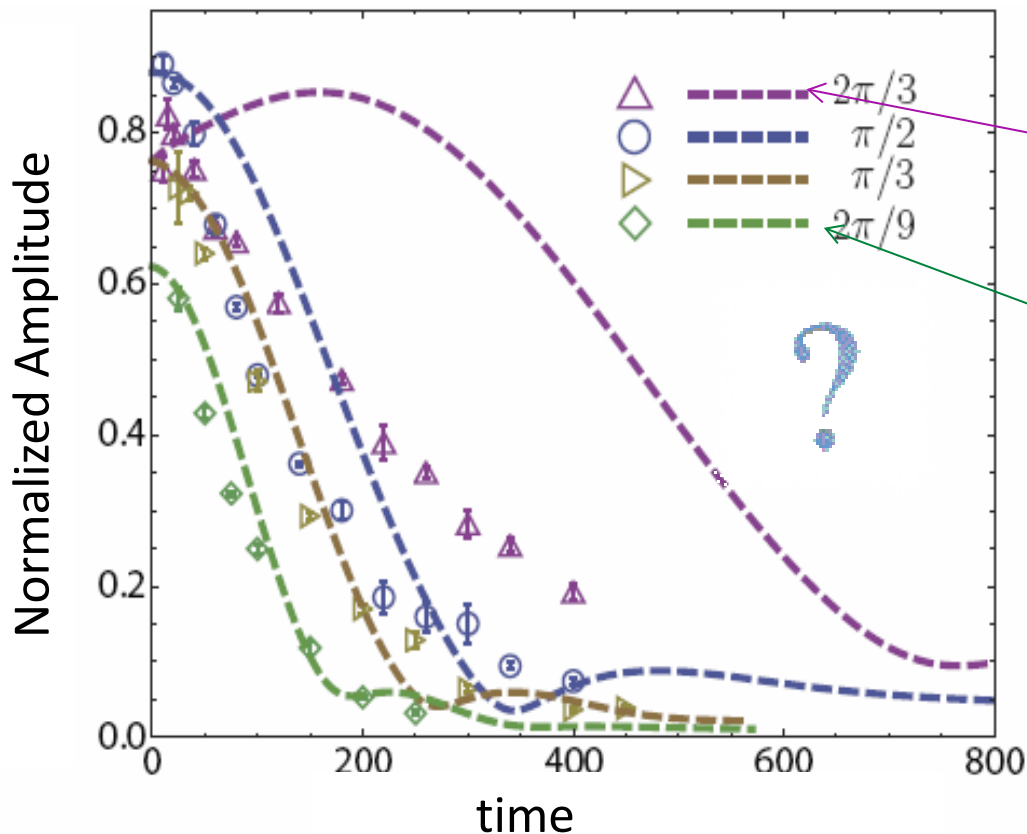
Signal adds → amplitude of the oscillations decay due to dephasing or destructive interference between pancakes

- Atom number decay also leads to decay of the amplitude

# Comparisons with experiment

## Ramsey fringe decay vs. the spin tipping angle

To eliminate the effect of decay we normalize the amplitude with atom number



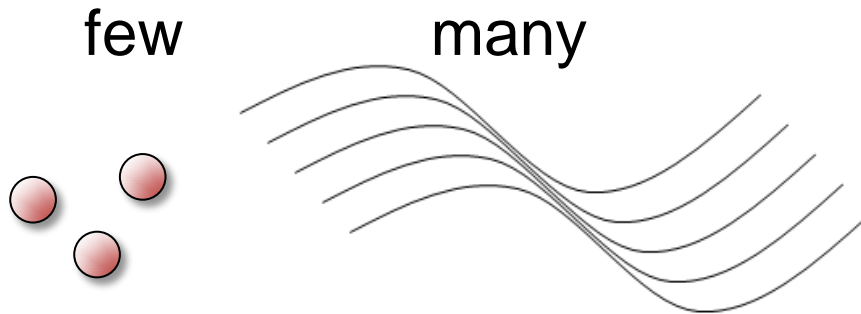
Shift

Excitation fraction

**Mean field fails to reproduce the amplitude decay at tipping angles where the density shift vanishes**

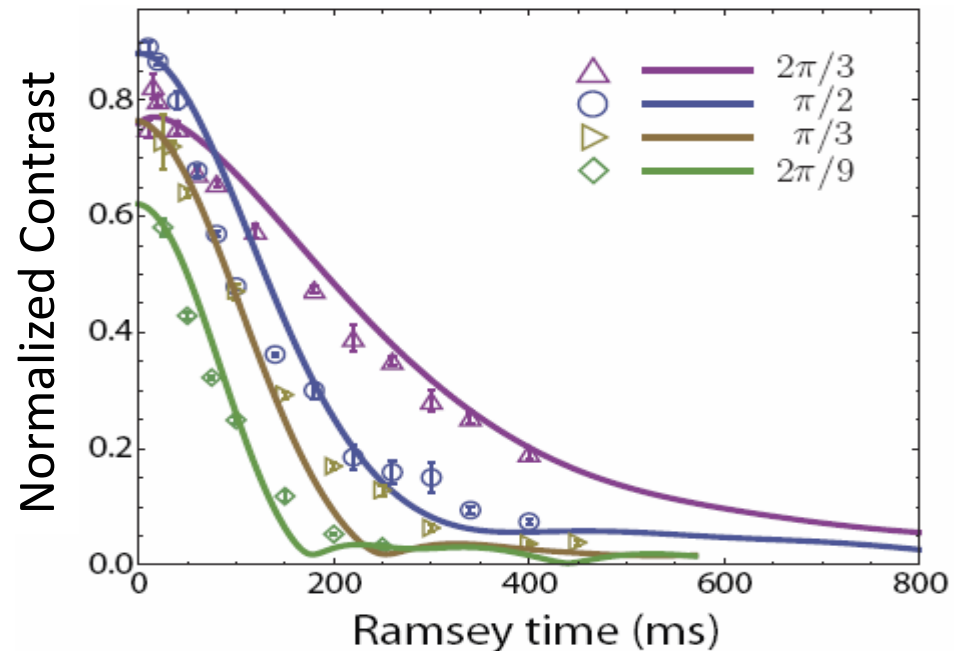
# Quantum fluctuations – beyond mean field

Interplay between interactions and decoherence: complicated

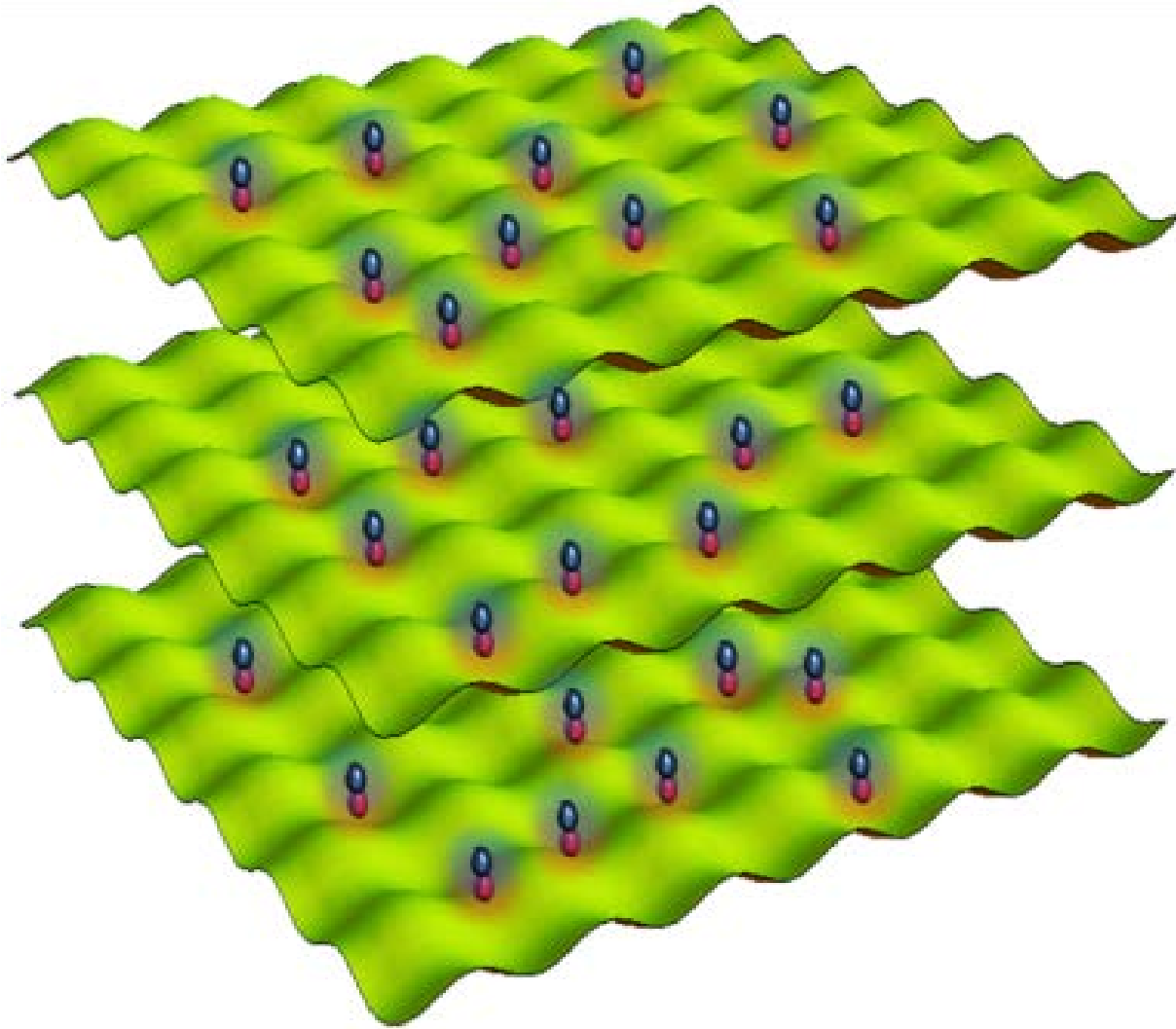


Quantum correlations induce faster decay of the amplitude

**We were able to solve the full master Eq for the collective model.**



# Polar molecules

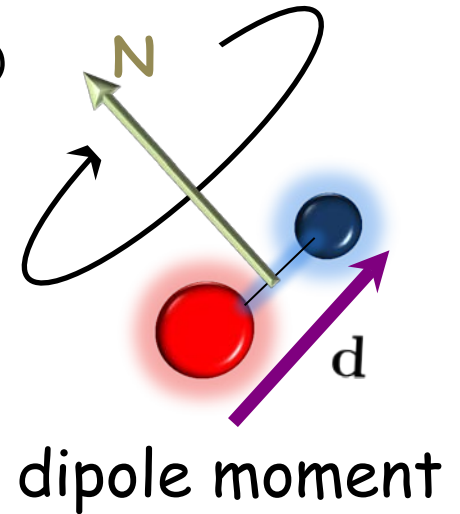


# Quantum Magnetism

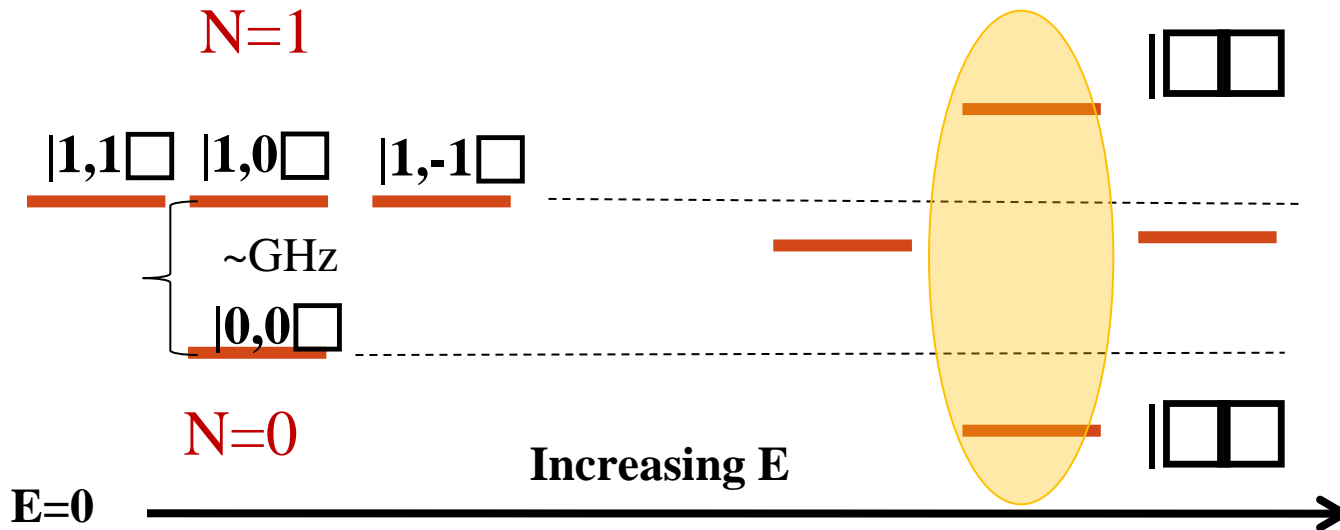
Gorshkov *et al*: PRL.107.115301(2011), PRA 84,033619 (2011)

Rotation  $\Rightarrow$  "spin"

**Rigid Rotor**  $H_i^{rot} = BN_i^2 - \vec{d}_i \cdot \vec{E}$



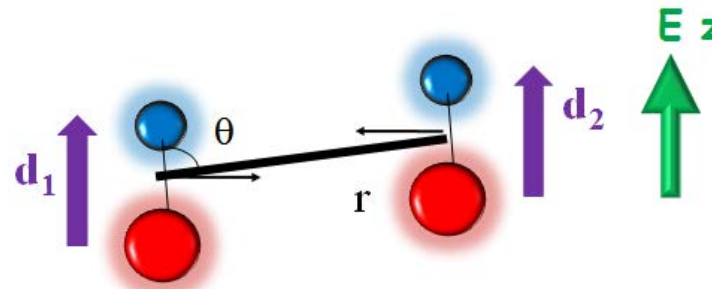
Select two dressed levels :  
Effective spin  $1/2$  system



## Related previous work

**Other schemes:** *Micheli et al, Nat. Phys. 2 341 (2006); Brennen et al, NJP 9 138 (2007); Buechler et al, Nat. Phys. 3 726 (2007); Perez-Rios, et al NJP 12, 103007; Wall-Carr Phys. Rev. A 82, 013611 (2010)...*

# Spin model: Frozen molecules in a lattice



$$H_{dd} = d_i d_j V_{dd}^{ij} \quad V_{dd}^{ij} = \frac{(1 - 3 \cos^2 \theta)}{|r_i - r_j|^3}$$

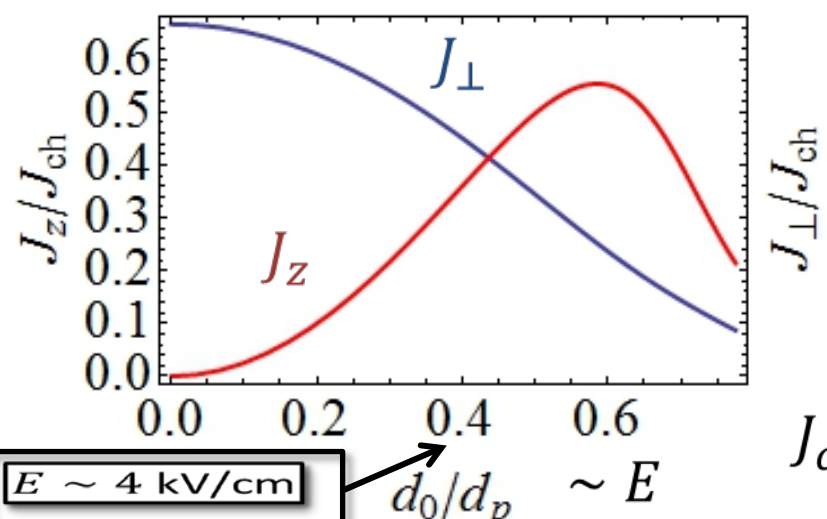
- Project  $d_i$  on the two selected rotational levels

$$d_i = \hat{z} \sum_{\sigma, \sigma'} d_{\sigma, \sigma'} |\sigma_i\rangle \langle \sigma_i'| \quad d_{\sigma\sigma'} = \langle \sigma | d | \sigma' \rangle$$

$$|\uparrow\rangle = |N=1, M=0\rangle$$

$$|\downarrow\rangle = |N=0, M=0\rangle$$

$$H_{dd} = \sum_{i,j} V_{dd}^{ij} \left[ \underbrace{J_z(d_{\sigma\sigma'}) S_i^z S_j^z}_{\text{Ising}} + \underbrace{J_{\perp}(d_{\sigma\sigma'}) (S_i^x S_j^x + S_i^y S_j^y)}_{\text{Flip-flop}} \right]$$



$$J_{\perp} = 2(d_{\uparrow\downarrow})^2$$

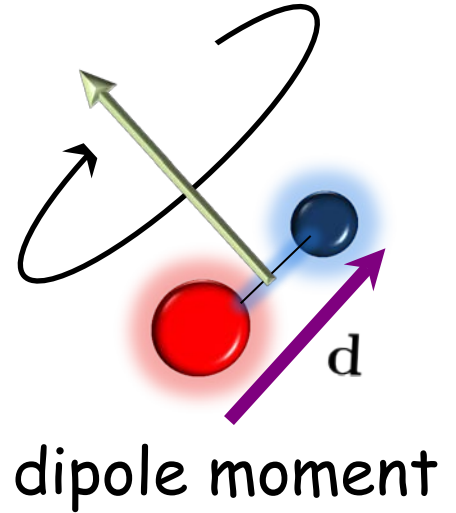
$$J_z = (d_{\uparrow\uparrow} - d_{\downarrow\downarrow})^2$$

$J_{ch} \sim 2\pi \times 250\text{Hz} \rightarrow 1\text{ms}$

$E \sim 4 \text{ kV/cm}$   $d_0/d_p \sim E$



# Quantum Magnetism



- Use direct dipole-dipole interaction to generate direct strong ( $\sim$ KHz) spin exchange interaction:

**10-100 larger than super-exchange or magnetic dipoles**

- Fully tunable coefficients by E field (microwaves)

**Gorshkov *et al*: PRL.107.115301(2011),  
PRA 84,033619 (2011)**

- Long-range ( $1/r^3$ ) and anisotropic interactions:

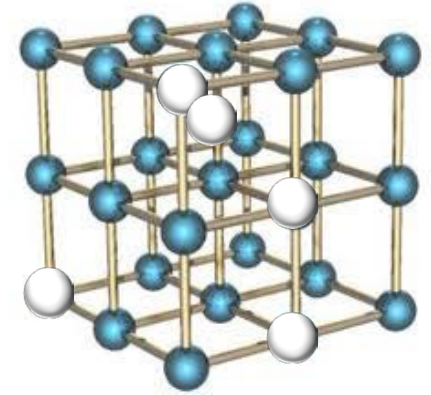
**S. R. Manmana *et al* PRB 87, 081106(R) (2013),  
A. V. Gorshkov *et al* arXiv:1301.5636**

- Spin *temperature*, not motional *temperature* matters:

**Relevant ratio is interaction time ( $\sim$ ms) to cloud lifetime (25 sec!):  
K. R.A. Hazzard *et al* PRL 110, 075301 (2013)**

# Filling factor: $f$

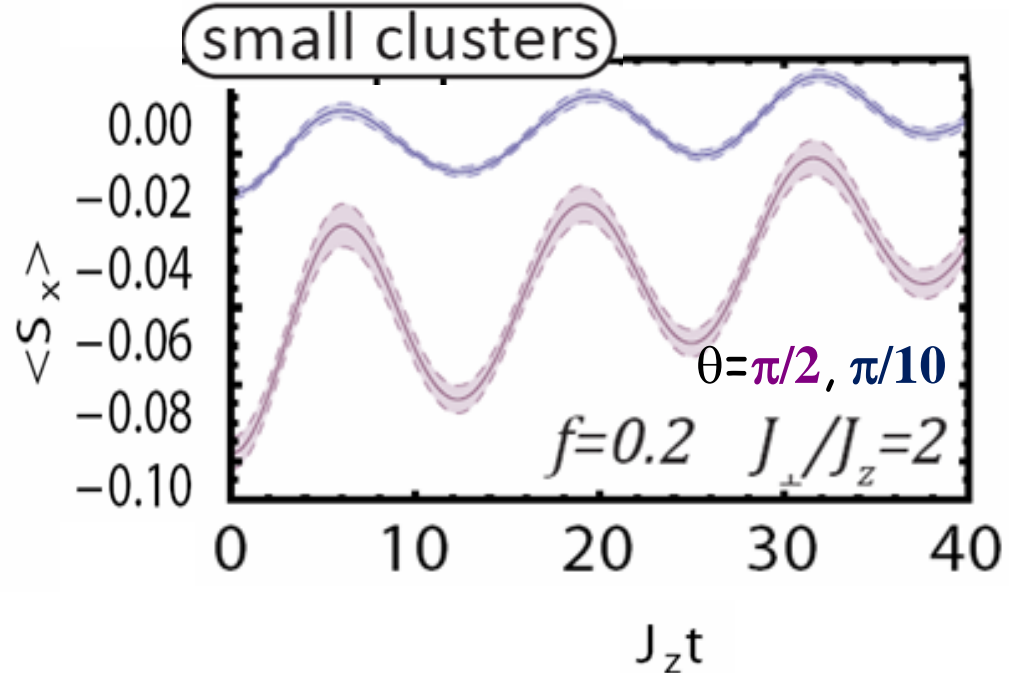
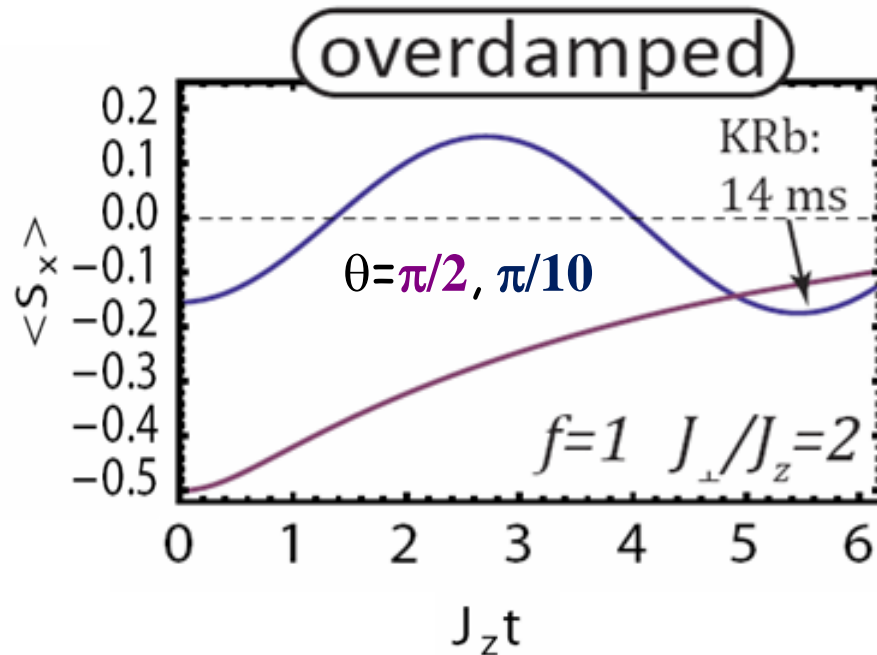
- Empty sites act as defects
- Need to perform disorder average



Dipolar interactions will be visible in the Ramsey fringe contrast even in dilute samples

## Full solution 1D-DMRG

K. R.A. Hazzard et al PRL 110, 075301 (2013)



# 3D-KRb lattice experiment

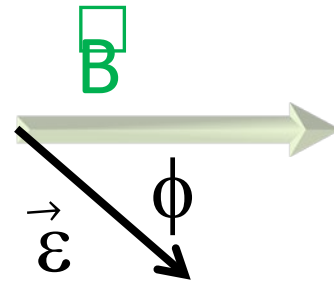
Current experiments are carried out in a 3D lattice with a B field

B: determines quantization axis

$$| \square \square \square \rangle \equiv | N=1, M=-1 \rangle$$

$$| \square \square \square \rangle \equiv | N=0, M=0 \rangle$$

Polarization  
trapping light

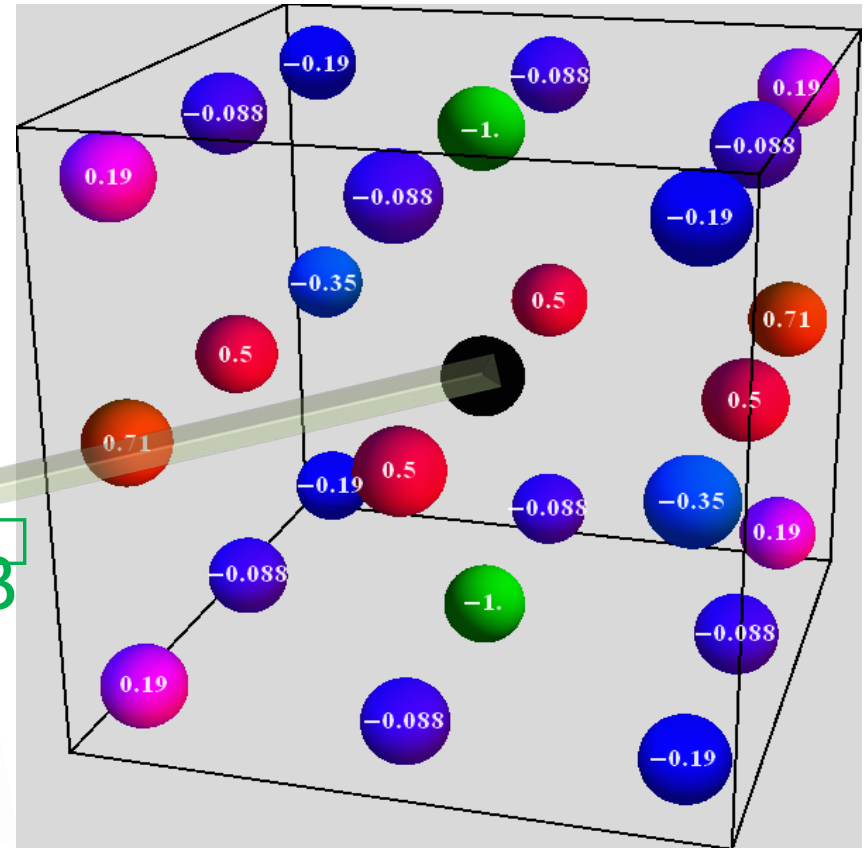
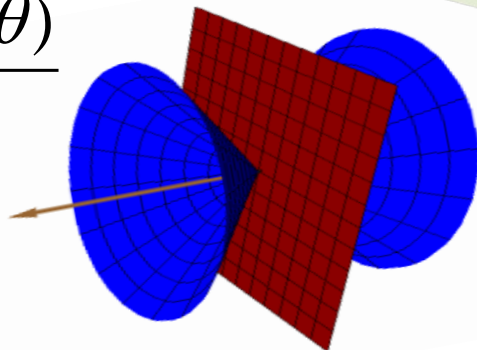


Magic wavelength for their  
lattice

B. Neyenhuis *et al*/Phys. Rev. Lett. 109,  
230403 (2012)

- Non-trivial dependence on the geometry due to the anisotropic dipolar interactions.

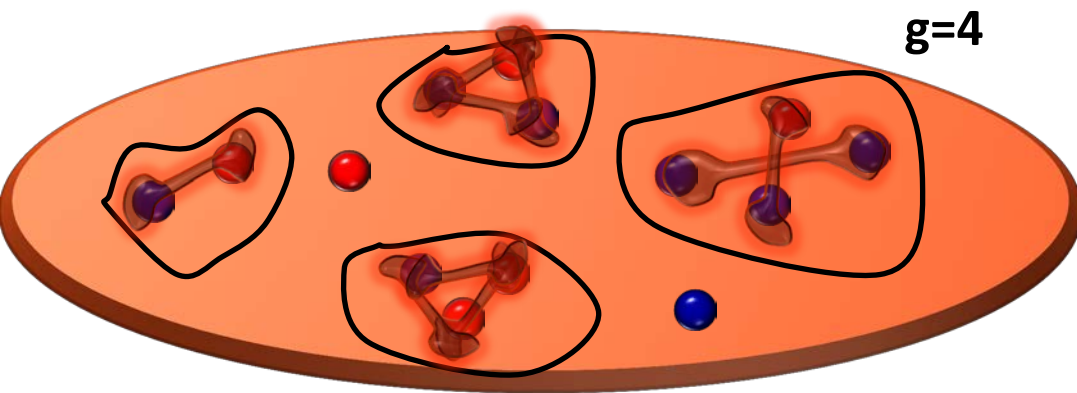
$$V_{dd}^{ij} = \frac{(1 - 3 \cos^2 \theta)}{|r_i - r_j|^3}$$



# 3D-lattice experiment in B field

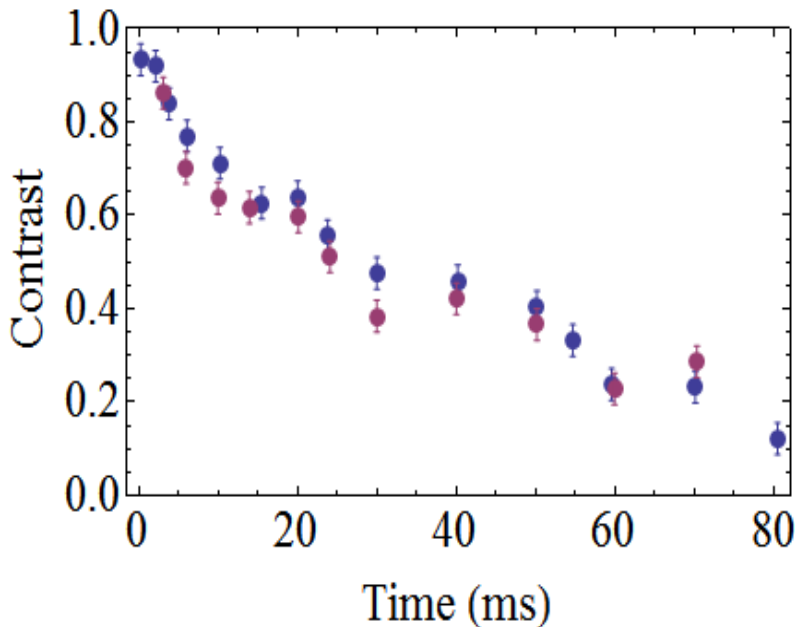
$$H = J_{\perp} \sum_{\langle i,j \rangle} V_{ij} [S^x_i S^x_j + S^y_i S^y_j] \quad J_{\perp} = -(d_{\uparrow\downarrow})^2$$

## Cluster Expansion

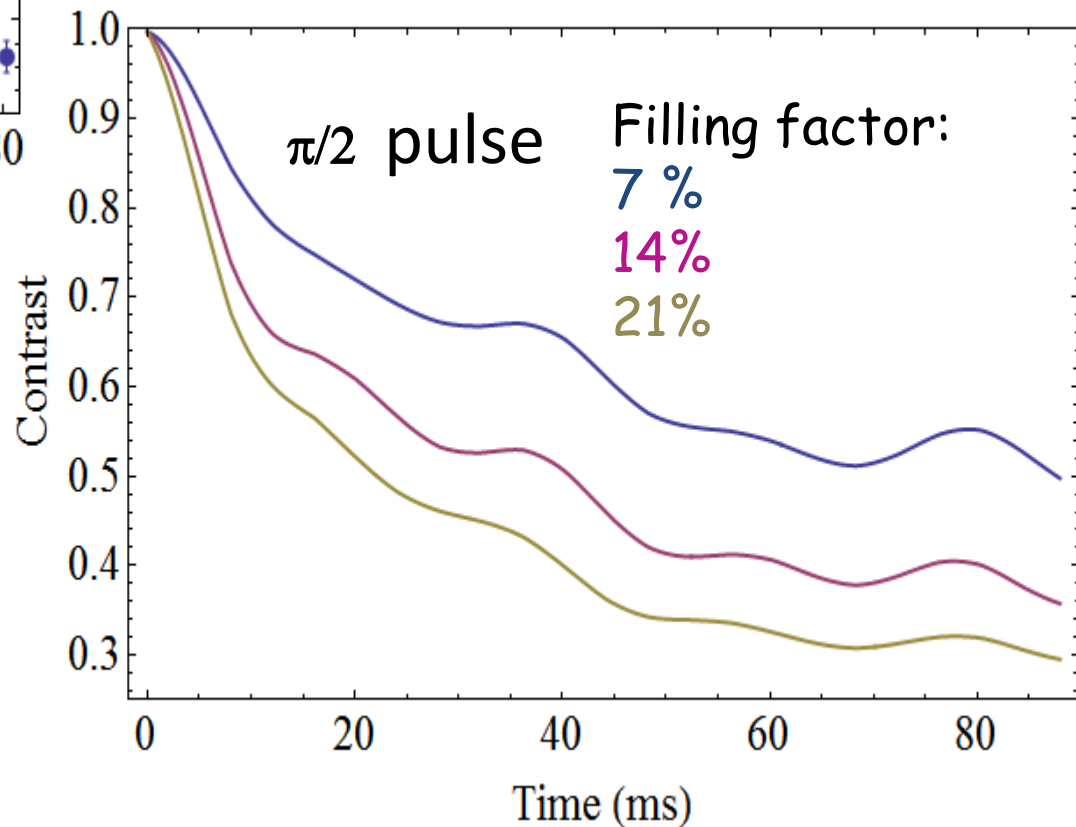


- Spins grouped in cluster of max size  $g$ .
- Intra-cluster interactions kept
- Inter-cluster interactions neglected or treated as a perturbation.

# Preliminary comparisons with experiment



Solid lines: Cluster expansion  $g=10$   
Gaussian distribution:

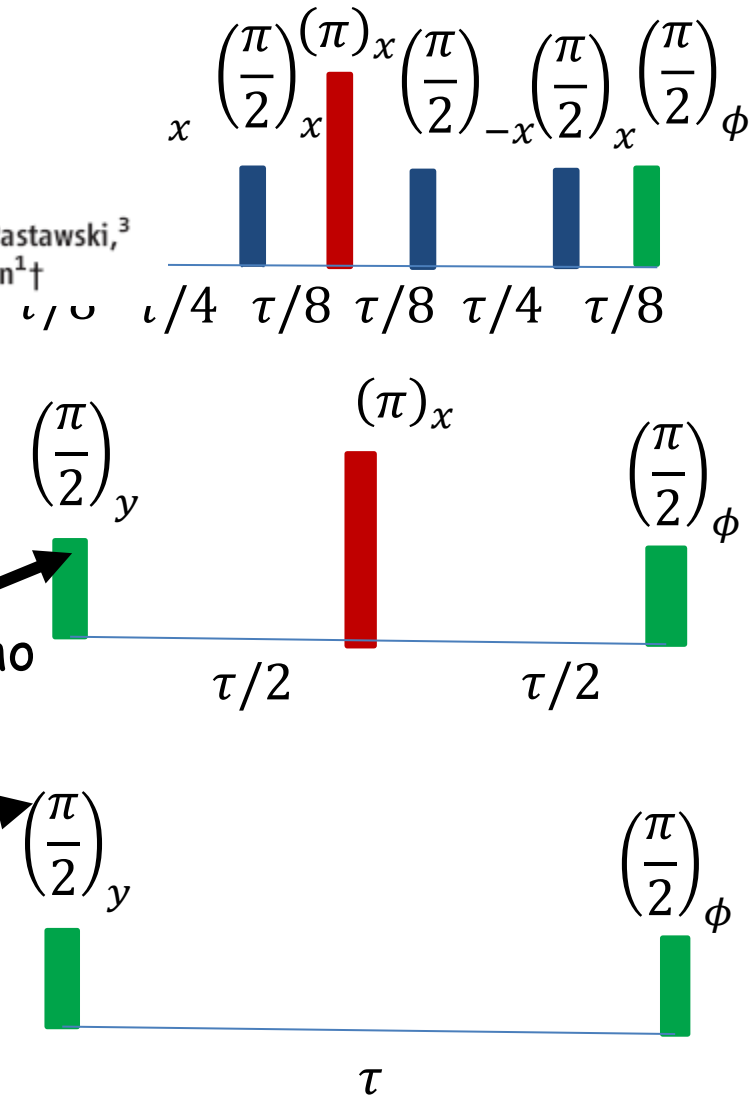
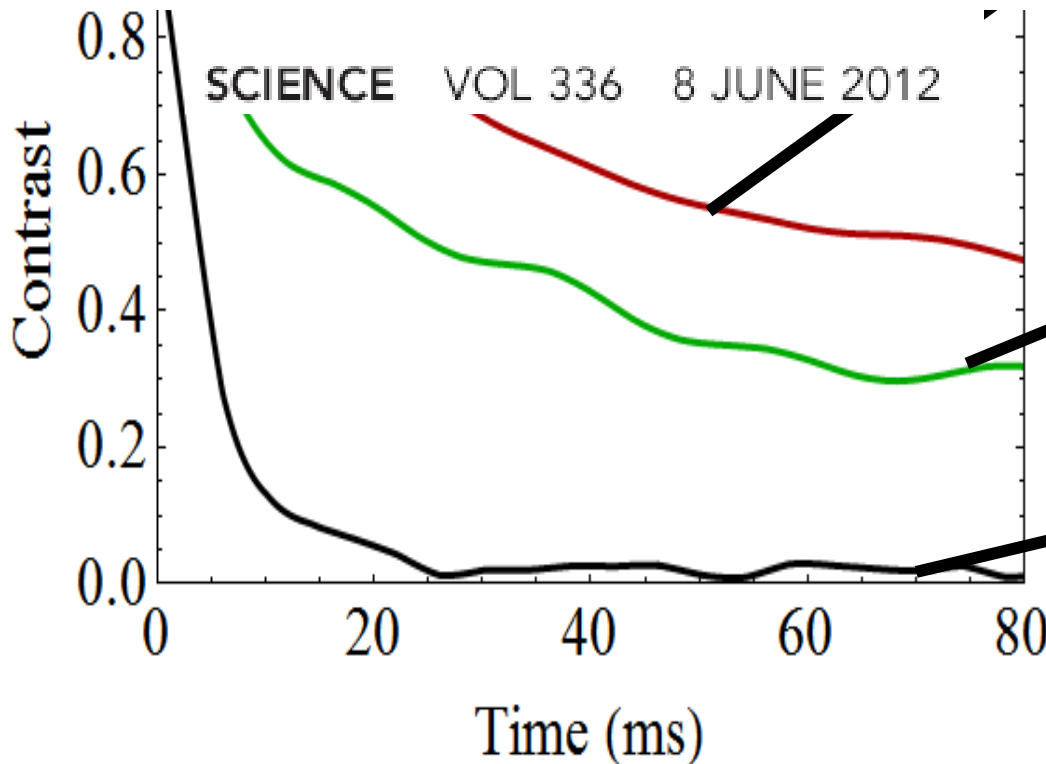


# Dynamical decoupling

Learn from NMR: By applying the proper pulse sequence it is possible to eliminate dipolar interactions.

## Room-Temperature Quantum Bit Memory Exceeding One Second

P. C. Maurer,<sup>1\*</sup> G. Kucsko,<sup>1\*</sup> C. Latta,<sup>1</sup> L. Jiang,<sup>2</sup> N. Y. Yao,<sup>1</sup> S. D. Bennett,<sup>1</sup> F. Pastawski,<sup>3</sup> D. Hunger,<sup>3</sup> N. Chisholm,<sup>4</sup> M. Markham,<sup>5</sup> D. J. Twitchen,<sup>5</sup> J. I. Cirac,<sup>3</sup> M. D. Lukin<sup>1†</sup>



# Conclusions

- Ultra-cold polar matter offers a unique controllable laboratory for the exploration of many-body physics

## Strongly interacting open driven quantum systems

- Manifestation of quantum magnetism observable even in a non-quantum degenerate gas
- Rich physics a lot to be understood

Thanks