

# 半導体中の飛行量子ビット

## Flying qubits in semiconductors

Yasuhiro Tokura (NTT Basic Research Laboratories)

- Introduction -flying qubit-
- Topics
  - Effect of statistics
  - Entanglement generation and detection
  - Single electron emission and collection
  - Qubit entangler
- Conclusions

# Self-introduction

- 相関理化学という分野で修士課程修了。
- 1985年 NTT入社 基礎研究所所属
- 半導体物性、メゾスコピック、ナノサイエンスに従事
- 1998年 オランダ・デルフト工科大 客員研究員
- 2004年 東京理科大 客員教授
- 2005年 量子光物性研究部 部長
  
- *興味のある研究分野*
  - 量子輸送現象、非平衡現象、量子情報処理
- *趣味等*
  - 音楽、バドミントン、旅行

# NTT 物性科学基礎研究所 の裏山 (2011.4)

*Haruka Tanji*

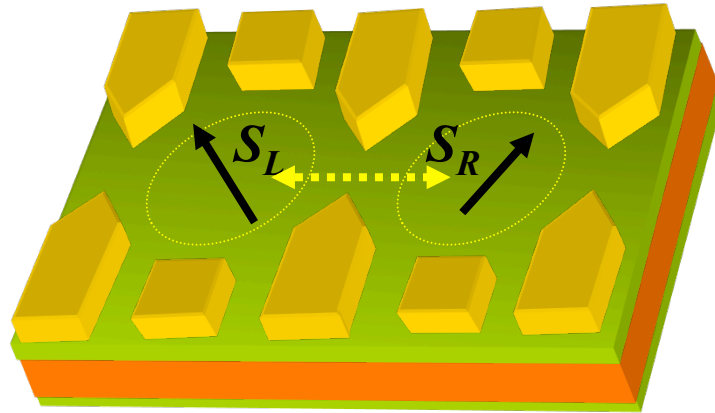
*Nobuyuki Matsuda*

*Hiromitsu Imai*

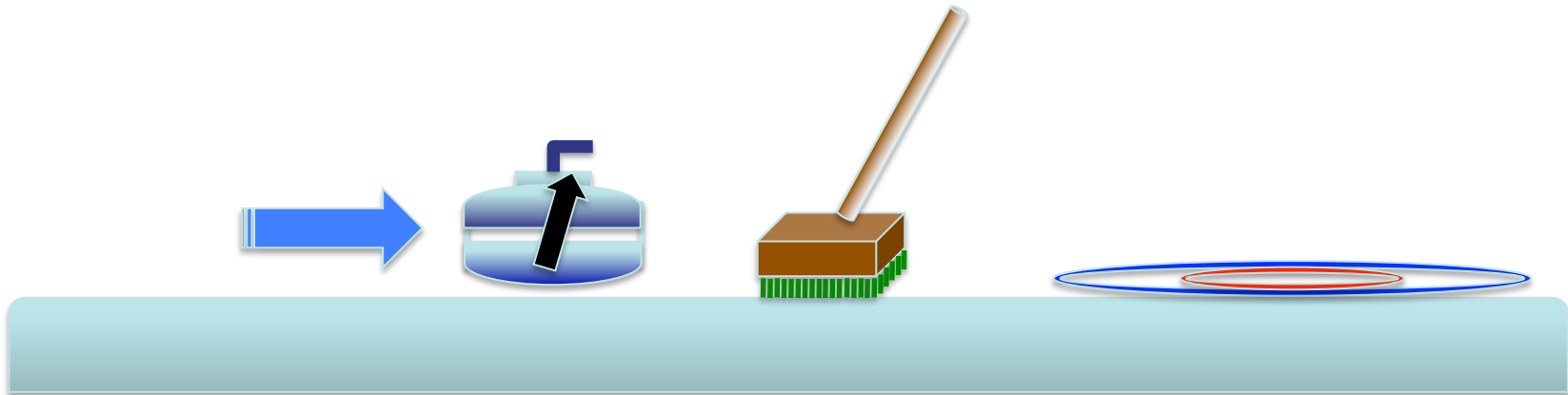
*Quantum Optical state control research group*



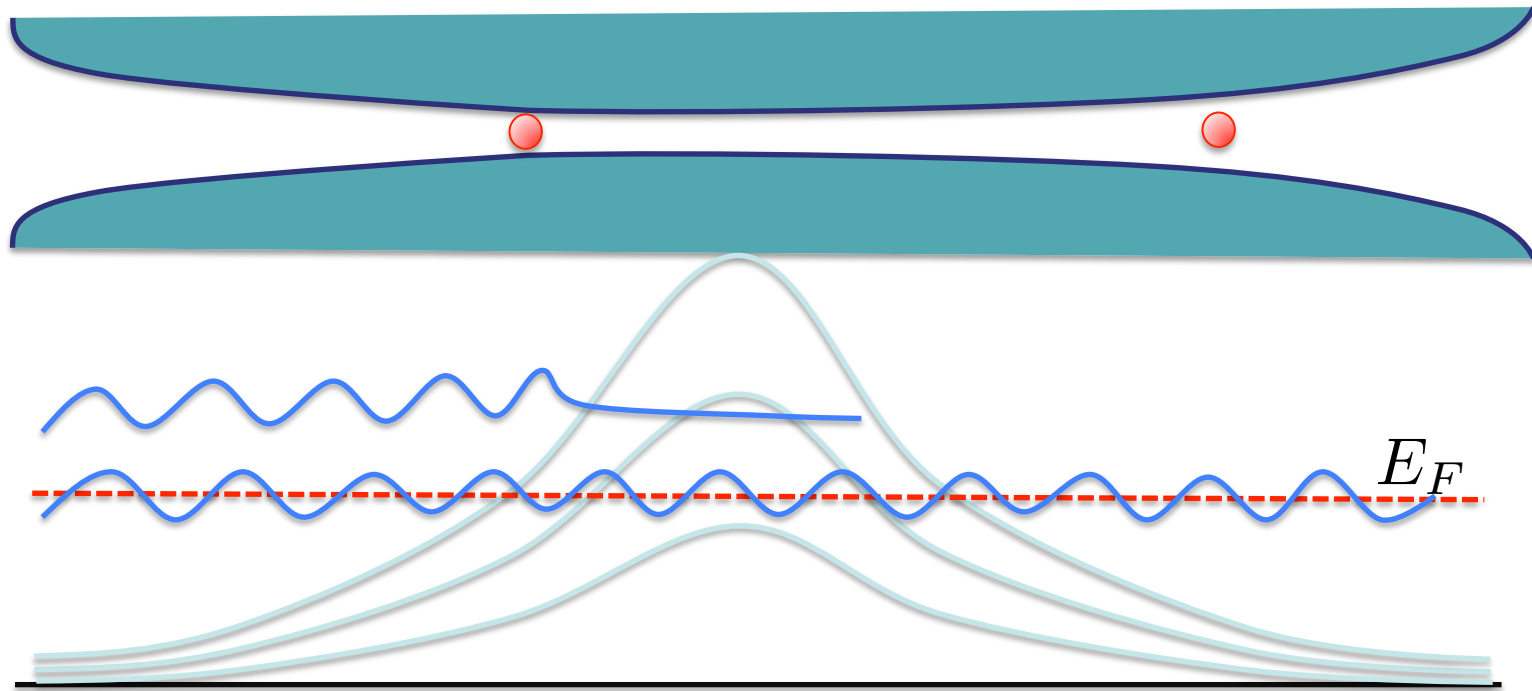
# Static qubits and flying qubits



*Loss and DiVincenzo PRA (98)*



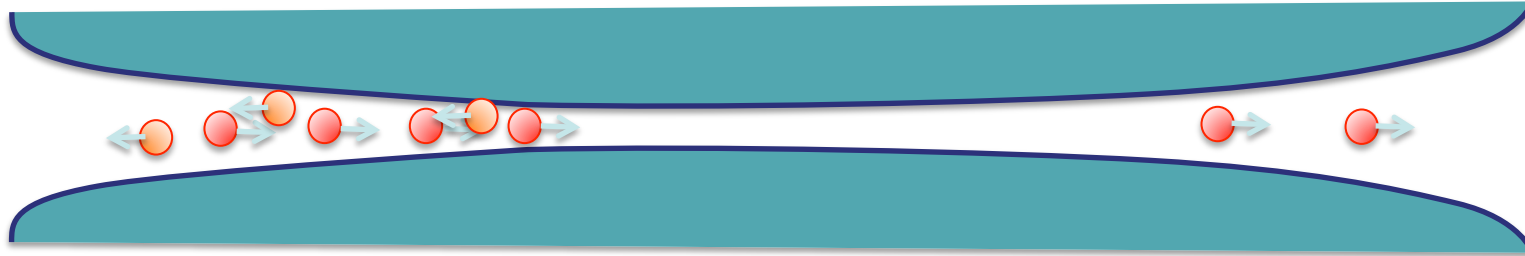
# Quantum wire, quantum point contact



Conductance  $G = \frac{2e^2}{h} \sum_n T_n$  Transmission probability of mode  $n$

$T_n = 1$  Noiseless mode

# Shot noise



For simplicity, only consider single mode,  $eV \gg k_B T$

Input occupation:  $\langle n_{in} \rangle = 1$

Transmitted occupation:  $\langle n_T \rangle = T$

Reflected occupation:  $\langle n_R \rangle = R$

Conservation of electron #

$$n_{in} = n_T + n_R$$

$$\rightarrow 1 = T + R$$

Electron cannot be divided

$$n_T = 0 \text{ or } 1$$

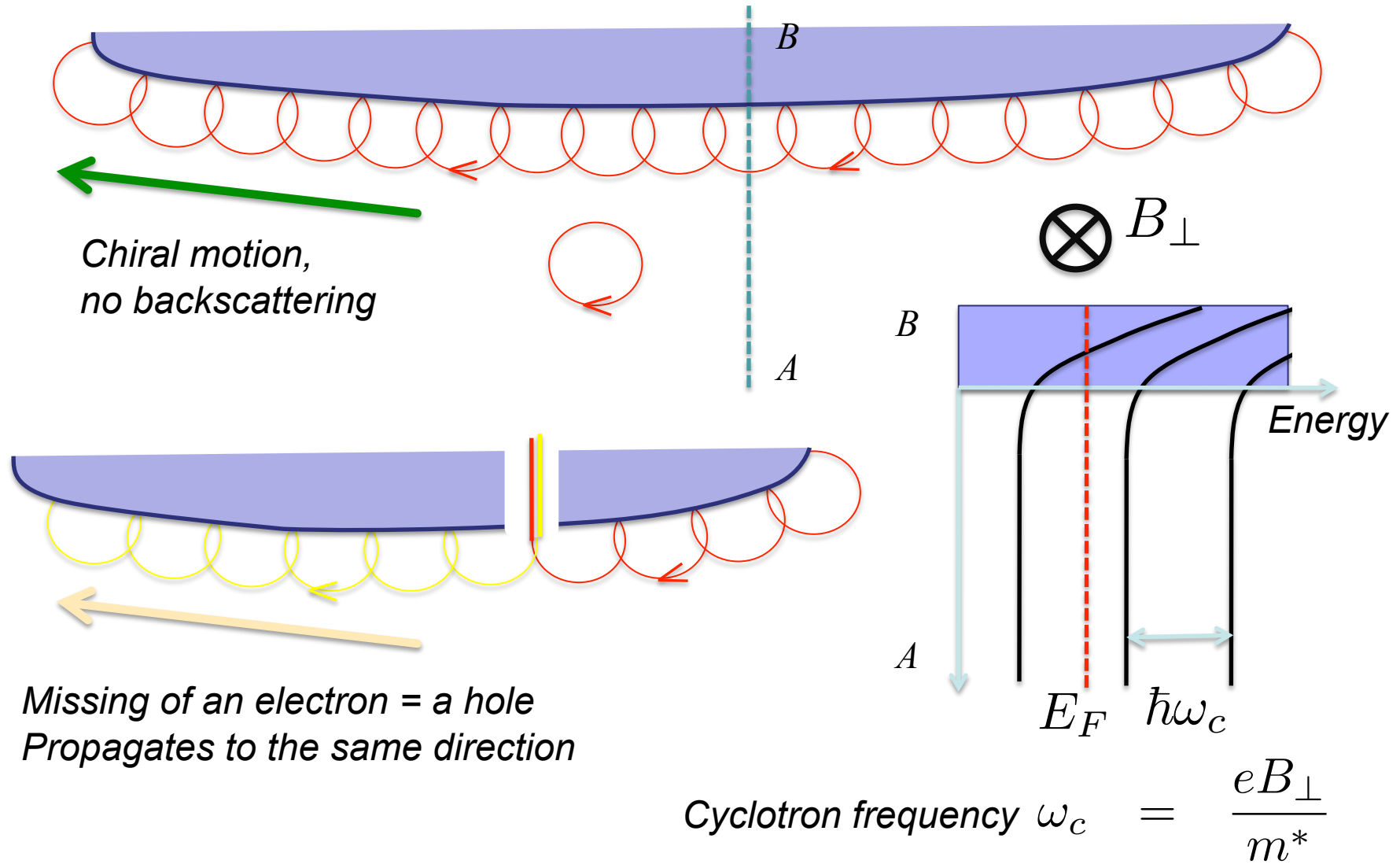
# fluctuation from its average

$$\Delta n_T \equiv n_T - \langle n_T \rangle$$

Shot noise at zero frequency limit:

$$\begin{aligned} S_0 &\propto \langle (\Delta n_T)^2 \rangle = \langle n_T^2 \rangle - \langle n_T \rangle^2 \\ &= \langle n_T \rangle - \langle n_T \rangle^2 = T(1 - T) \end{aligned}$$

# An edge state



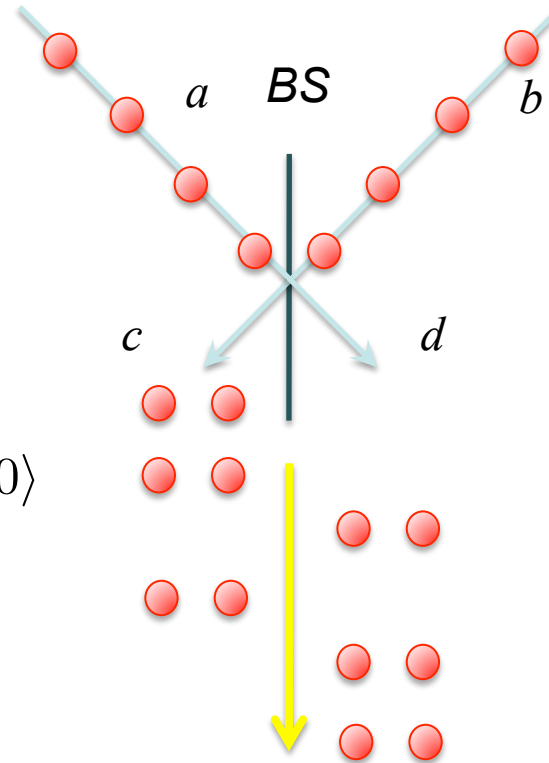
# Photons - bunching

*Ideal beam splitter (BS) unitary matrix ( $T=1/2$ ):*

$$\begin{pmatrix} a \\ b \end{pmatrix} \rightarrow \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} \begin{pmatrix} c \\ d \end{pmatrix}$$

*Collision experiment of photon (Boson)*

$$\begin{aligned} a^\dagger b^\dagger |0\rangle &\rightarrow \frac{1}{\sqrt{2}}(c^\dagger + d^\dagger) \frac{1}{\sqrt{2}}(c^\dagger - d^\dagger) |0\rangle \\ &= \frac{1}{2}(c^{\dagger 2} - d^{\dagger 2}) |0\rangle \end{aligned}$$



*Shot noise in port c:*

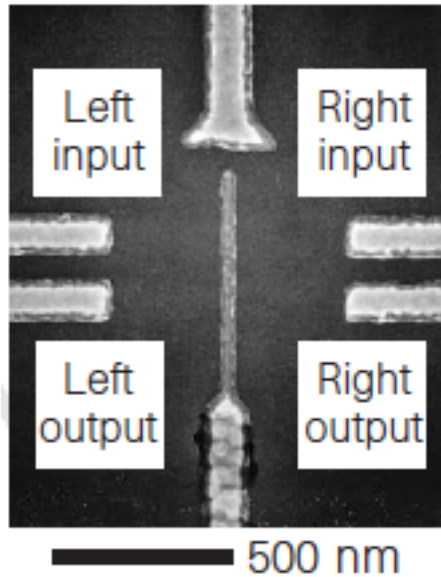
$$\begin{aligned} S_c &\propto \langle (\Delta n_c)^2 \rangle \\ &= \langle n_c^2 \rangle - (\langle n_c \rangle)^2 \\ &= 2 - 1 = 1 \end{aligned}$$

*Classical limit (distinguishable particles)*

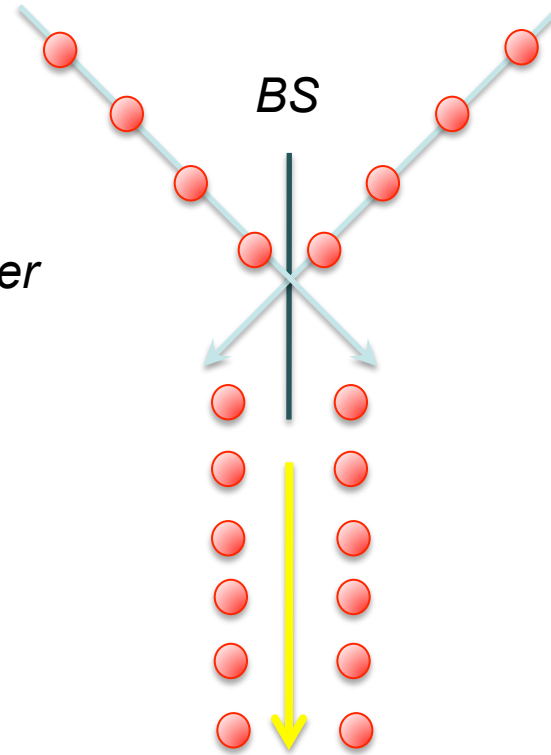
$$\begin{aligned} \langle n_c \rangle &= 0 \times \frac{1}{4} + 1 \times \frac{1}{2} + 2 \times \frac{1}{4} = 1 \\ \langle n_c^2 \rangle &= 0^2 \times \frac{1}{4} + 1^2 \times \frac{1}{2} + 2^2 \times \frac{1}{4} = \frac{3}{2} \\ S_c &\propto \frac{1}{2} \end{aligned}$$



# Electrons - anti-bunching



Scanning electron micrograph of an electron beam splitter device



$$a_{\sigma}^{\dagger} b_{\sigma'}^{\dagger} |0\rangle \rightarrow \frac{1}{2} (c_{\sigma}^{\dagger} c_{\sigma'}^{\dagger} - d_{\sigma}^{\dagger} d_{\sigma'}^{\dagger} - c_{\sigma}^{\dagger} d_{\sigma'}^{\dagger} - c_{\sigma'}^{\dagger} d_{\sigma}^{\dagger}) |0\rangle$$

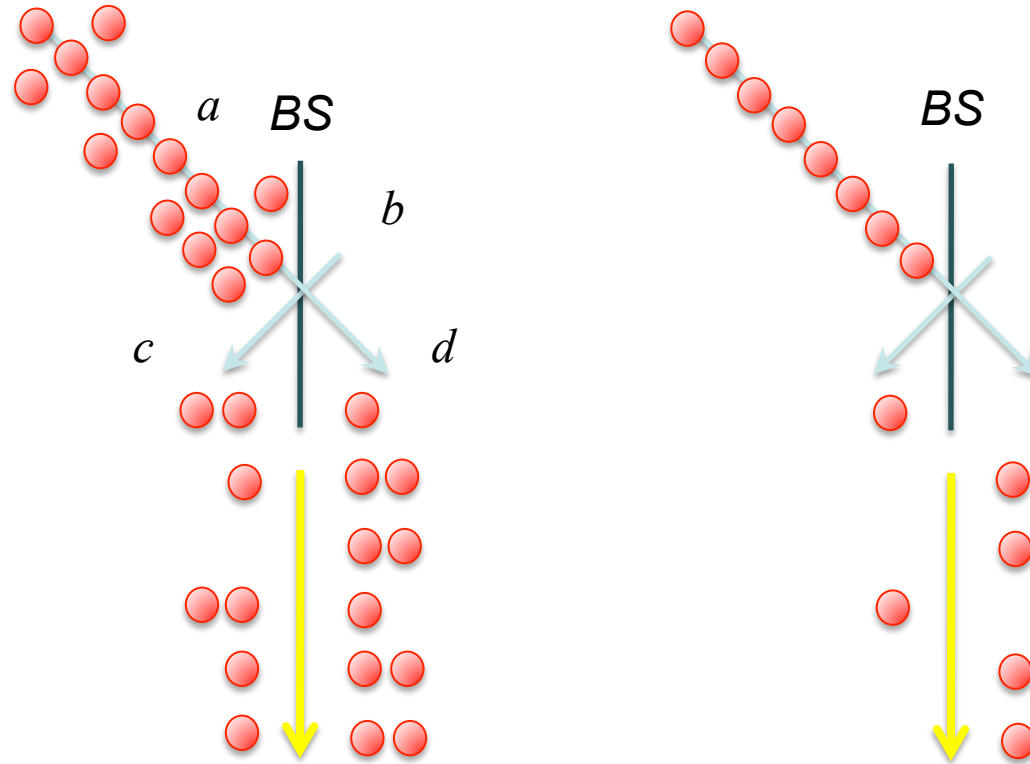
$$S_c \propto \langle (\sum_{\sigma} n_{c\sigma})^2 \rangle - \langle \sum_{\sigma} n_{c\sigma} \rangle^2$$

$$= \frac{5}{4} - 1^2 = \frac{1}{4}$$

For  $\sigma = \sigma'$ ,  $c_{\sigma}^{\dagger} c_{\sigma'}^{\dagger} = 0!$

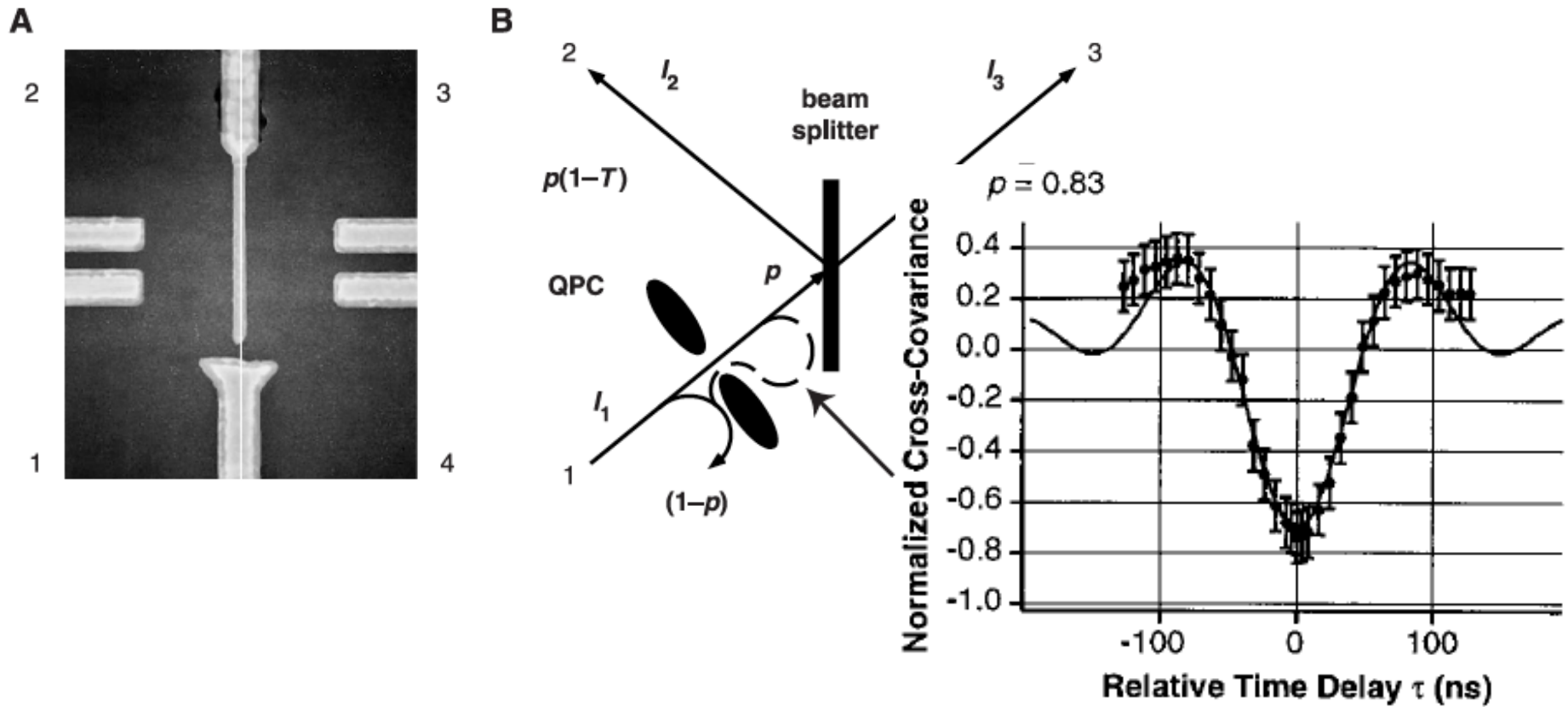
R.C. Liu, B. Odom, Y. Yamamoto, & S. Tarucha,  
Nature 391, 263 (1998).

# Cross correlation in two ports



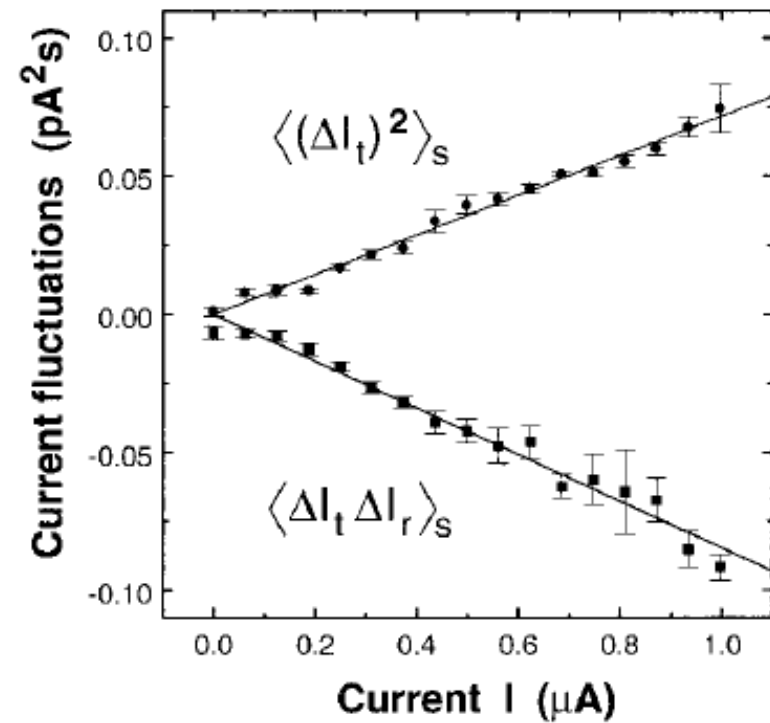
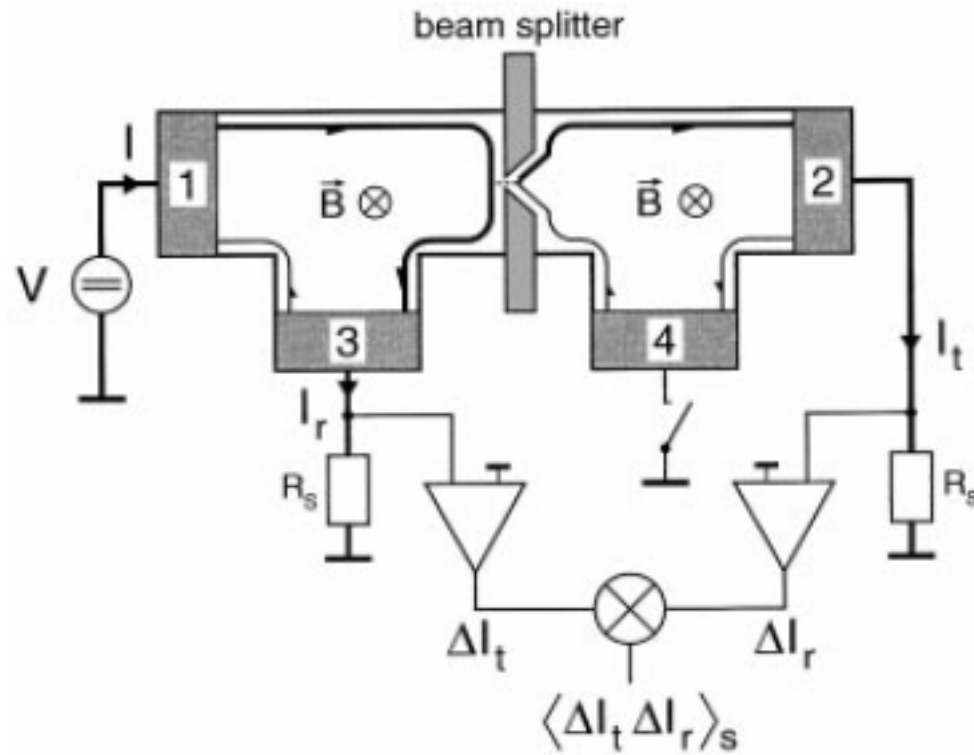
Statistics	Boson	Classical	Fermion
$S_{cross}$	Positive (for $n_a \gg 1$ )	0	Negative
$= \langle \Delta I_c \Delta I_d \rangle$			
For spin polarized electrons:		$S_{cross} \propto \langle (n_c - \frac{1}{2})(n_d - \frac{1}{2}) \rangle$	
Cf. $S_c \propto \langle (n_c - \frac{1}{2})^2 \rangle = \langle n_c^2 \rangle - \frac{1}{2^2} = \frac{1}{4}$		$= \langle n_c n_d \rangle - \frac{1}{2^2} = -\frac{1}{4}$	

# Hanbury Brown and Twiss



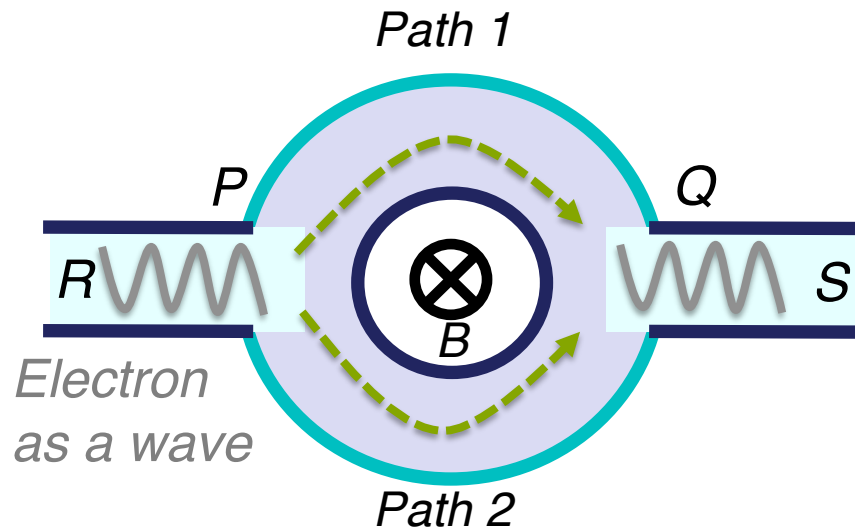
*W. D. Oliver, J. Kim, R. C. Liu, Y. Yamamoto,  
Science 284, 296 (1999).*

# HBT experiment with edge states



*M. Henny, et al. Science 284, 296 (1999).*

# Quantum coherence: AB interference



*Onsager's law*

(  $G_{RS}$  : linear conductance from P to Q )

$G_{RS}(B) = G_{SR}(B)$  : Current conservation

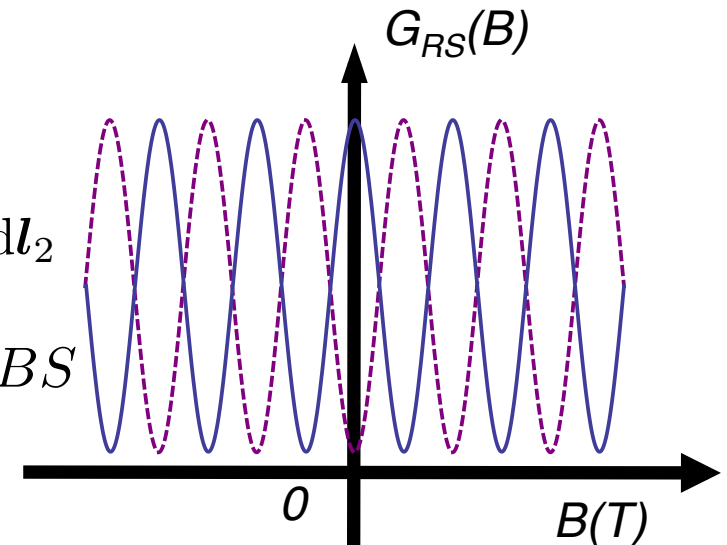
$G_{RS}(B) = G_{SR}(-B)$  : Time reversal symmetry



$$G_{RS}(B) = G_{RS}(-B)$$

*Two-terminal Aharonov-Bohm ring*

$$\begin{aligned} \varphi_1 - \varphi_2 &= \int_P^Q \left( \mathbf{k} - \frac{e}{\hbar} \mathbf{A} \right) \cdot d\mathbf{l}_1 - \int_P^Q \left( \mathbf{k} - \frac{e}{\hbar} \mathbf{A} \right) \cdot d\mathbf{l}_2 \\ &= \oint \mathbf{k} \cdot d\mathbf{l} - \frac{e}{\hbar} \oint \mathbf{A} \cdot d\mathbf{l} = \oint \mathbf{k} \cdot d\mathbf{l} - \frac{e}{\hbar} BS \end{aligned}$$



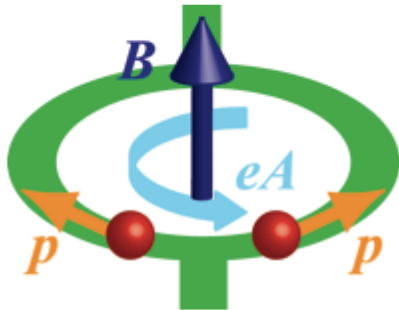
*T. Hatano, T. Kubo, Y. Tokura, S. Amaha, S. Teraoka, and S. Tarucha, Phys. Rev. Lett. 106, 076801 (2011).*

# Geometric phases

## Aharonov-Bohm (AB) phase

$$P = -i\hbar\nabla + e\mathbf{A} \quad \leftarrow \text{Vector potential}$$

$$\phi_{AB} = \frac{1}{\hbar} \oint e\mathbf{A} \cdot d\mathbf{l} = 2\pi \frac{\Phi}{\Phi_0}, \quad \Phi_0 = \frac{h}{e}$$

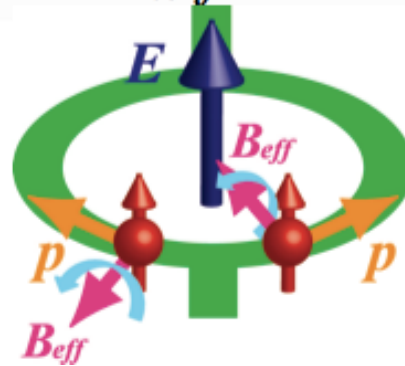


Y. Aharonov, 2010

## Aharonov-Casher (AC) phase

$$P = -i\hbar\nabla + e\mathbf{A}_{SO}, \quad \mathbf{A}_{SO} = \frac{1}{2}\mu\boldsymbol{\sigma} \times \mathbf{E} \quad \leftarrow \text{Effective spin vector potential}$$

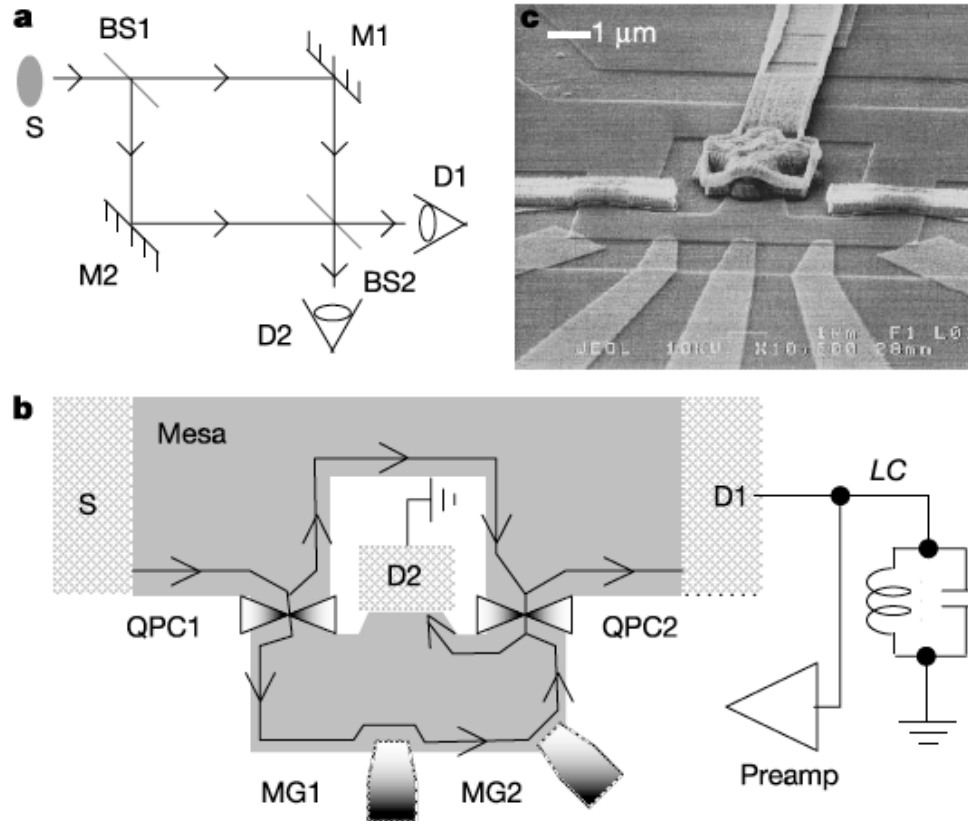
$$\phi_{AC} = \frac{1}{\hbar} \oint e\mathbf{A}_{SO} \cdot d\mathbf{l} = \frac{2\pi r m^* \alpha_{SO}}{\hbar^2}$$



A. Casher, 2010

# AB interferometer with edge states

*Y. Ji, et al., Nature 422, 415 (2003).*



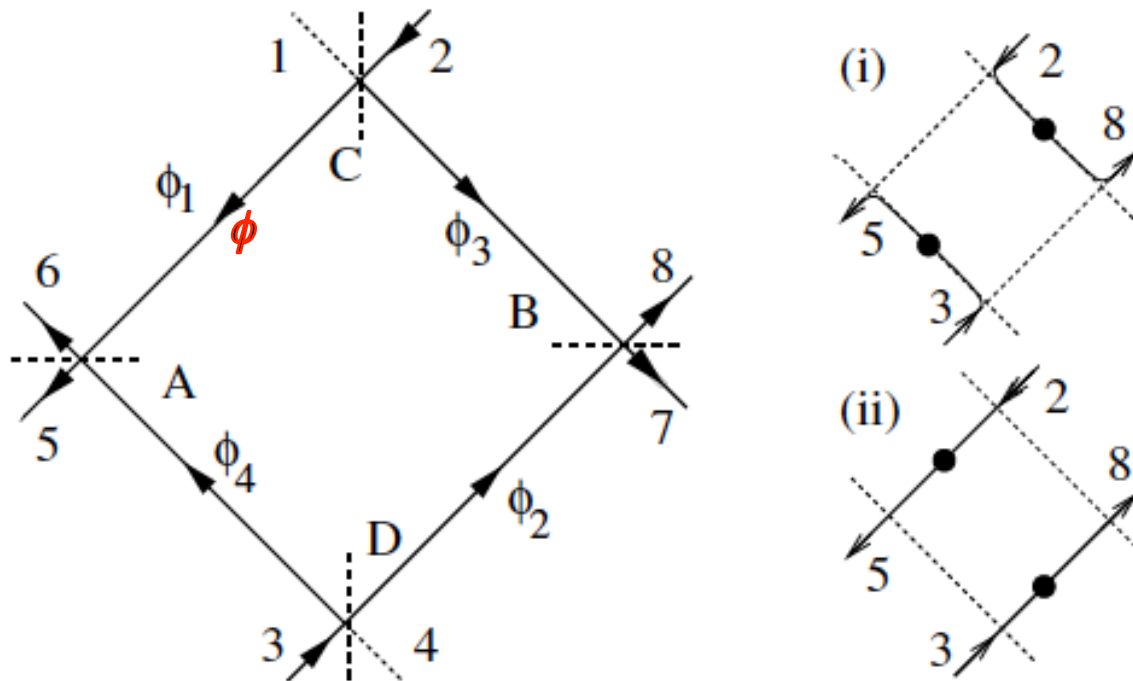
*Two half mirrors are made of  $T=1/2$  QPCs. Air-bridge technology is essential.*

*Phase coherence length is estimated from the visibility of the AB oscillations*

$$L_{\phi} \sim 24 \mu\text{m} @ 20 \text{ mK}$$

*P. Roulleau, et al., Phys. Rev. Lett. 100, 126802 (2008).*

# Two-electron interference

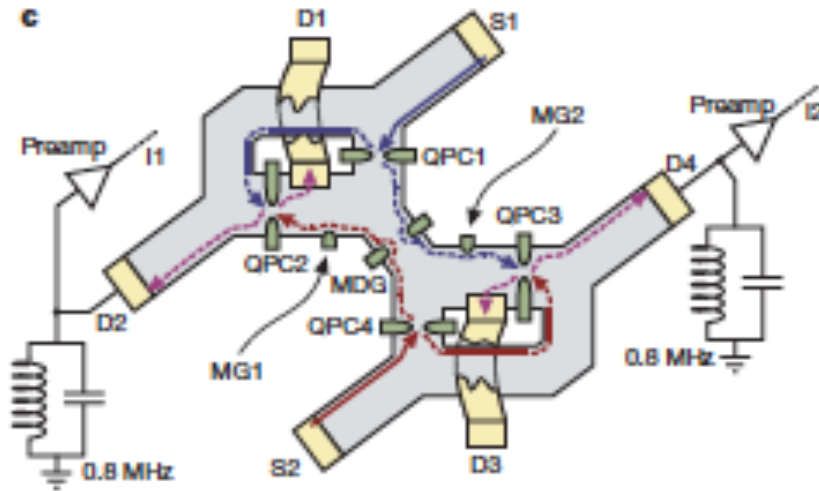


*Single electron current is independent of the flux  $\phi$ , but current correlations are dependent on  $\phi$ .*

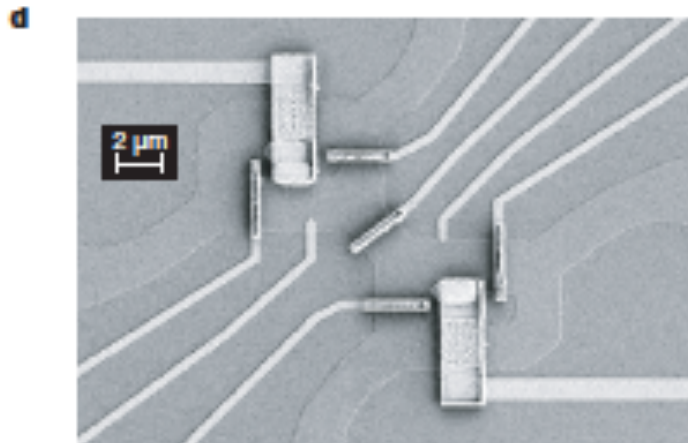
*P. Samuelsson, E. V. Sukhorukov, and M. Buttiker, Phys. Rev. Lett. 92, 026805 (2004).*



# HBT experiments II

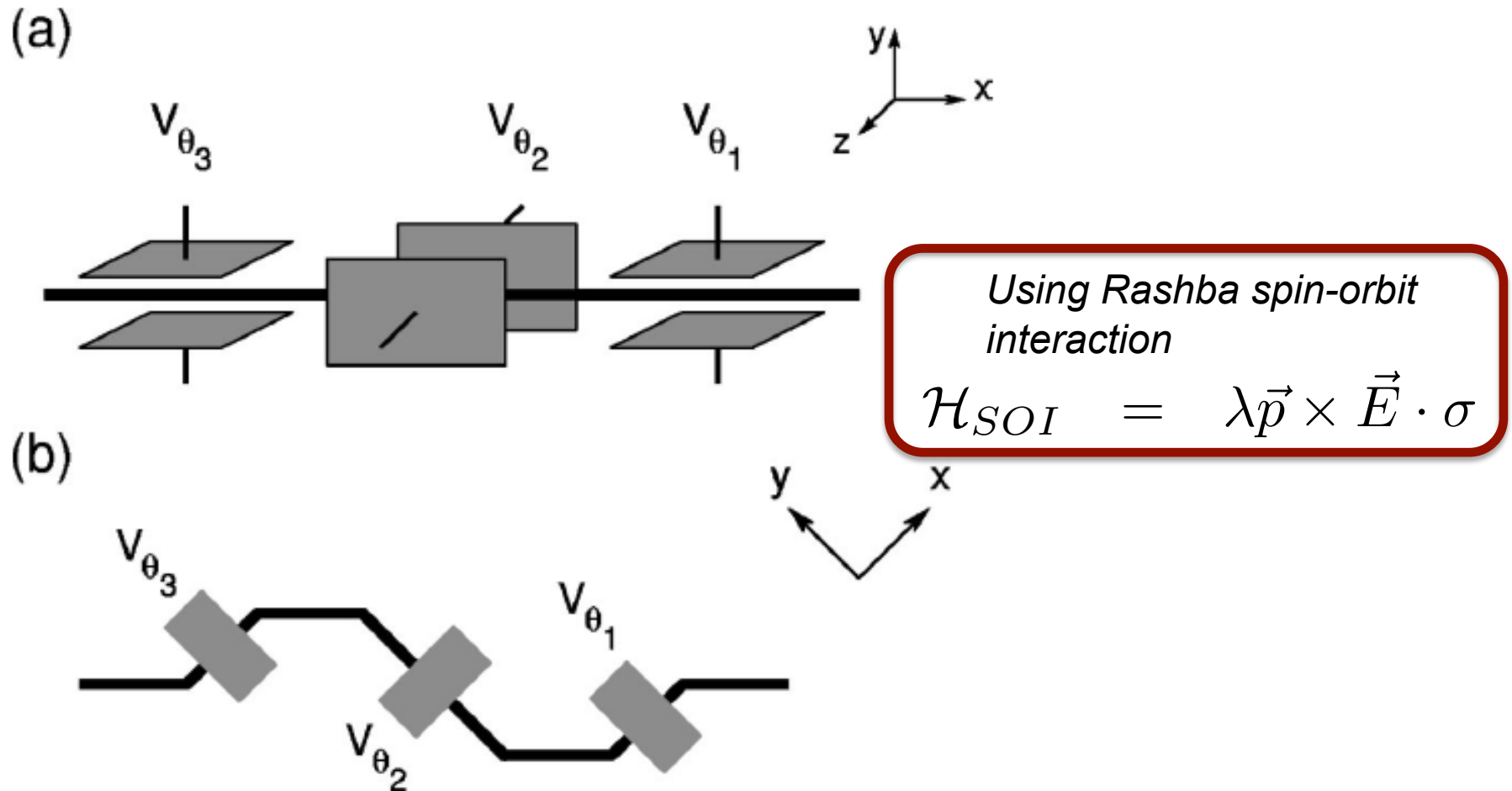


*Experimental confirmation of two-electron interference.*



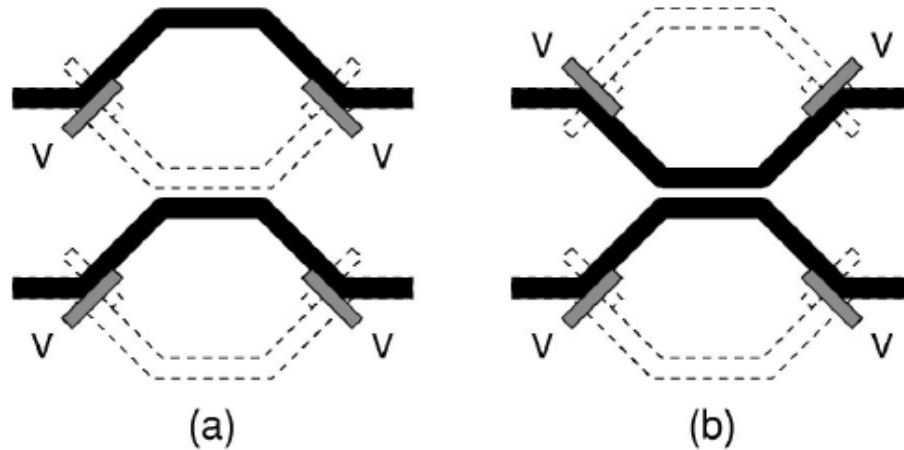
*I. Neder, et al., Nature 448, 333 (2007).*

# Alternative SU(2) control of spin qubit



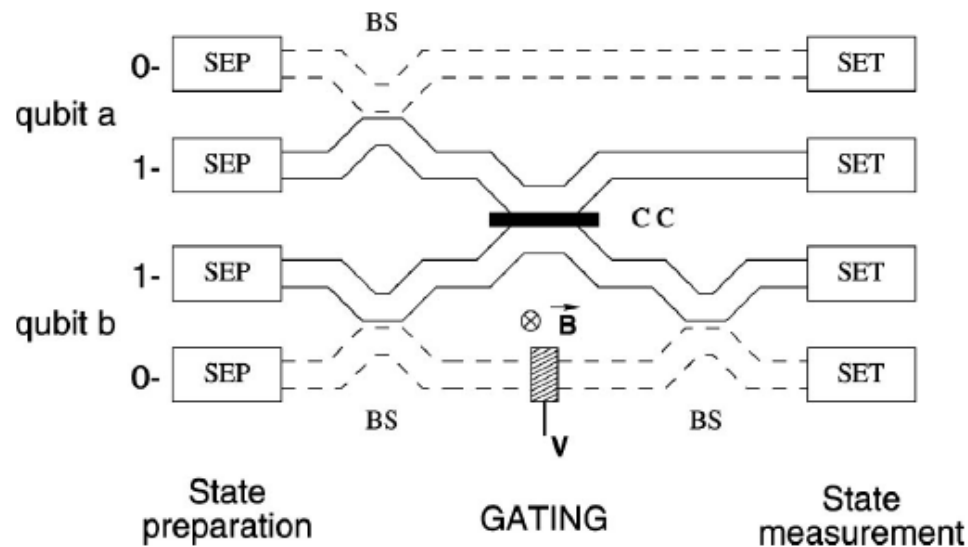
*A. E. Popescu and R. Ionicioiu,  
Phys. Rev. B 69, 245422 (2004).*

# Two qubit interaction and C-NOT



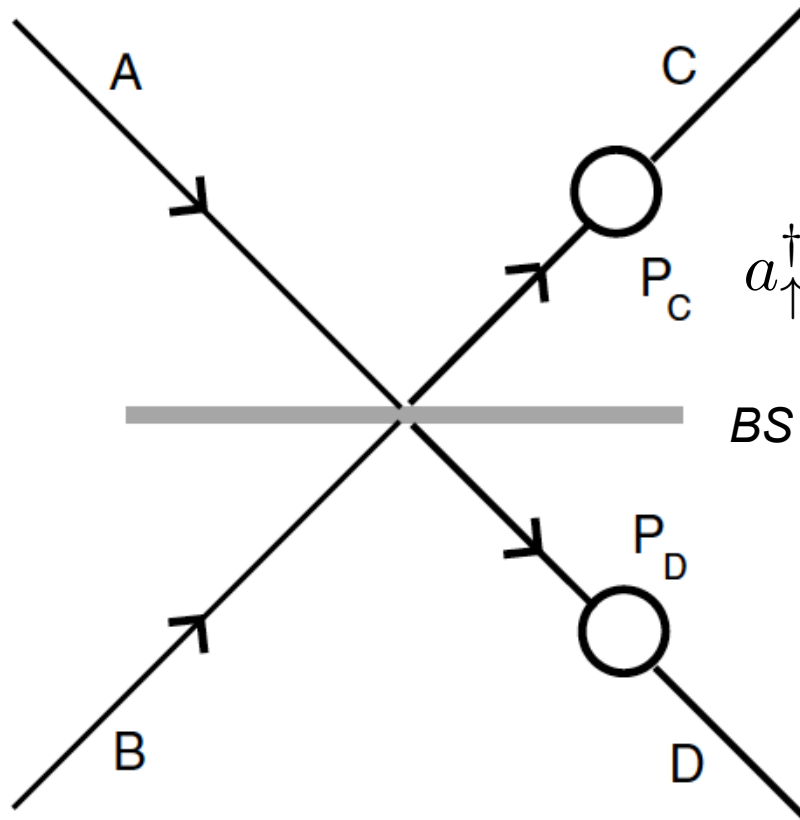
Using exchange interaction

$$\mathcal{H}_{ex} = J \vec{S}_1 \cdot \vec{S}_2$$



*R. Ionicioiu, P. Zanardi, and F. Rossi,  
Phys. Rev. A 63 050101(R) (2001).*

# Entanglement gen. with post selection



*Beam splitter*

$$a_{\uparrow}^{\dagger} b_{\downarrow}^{\dagger} |0\rangle \rightarrow \frac{1}{2} (c_{\uparrow}^{\dagger} c_{\downarrow}^{\dagger} - d_{\uparrow}^{\dagger} d_{\downarrow}^{\dagger} - c_{\uparrow}^{\dagger} d_{\downarrow}^{\dagger} - c_{\downarrow}^{\dagger} d_{\uparrow}^{\dagger}) |0\rangle$$

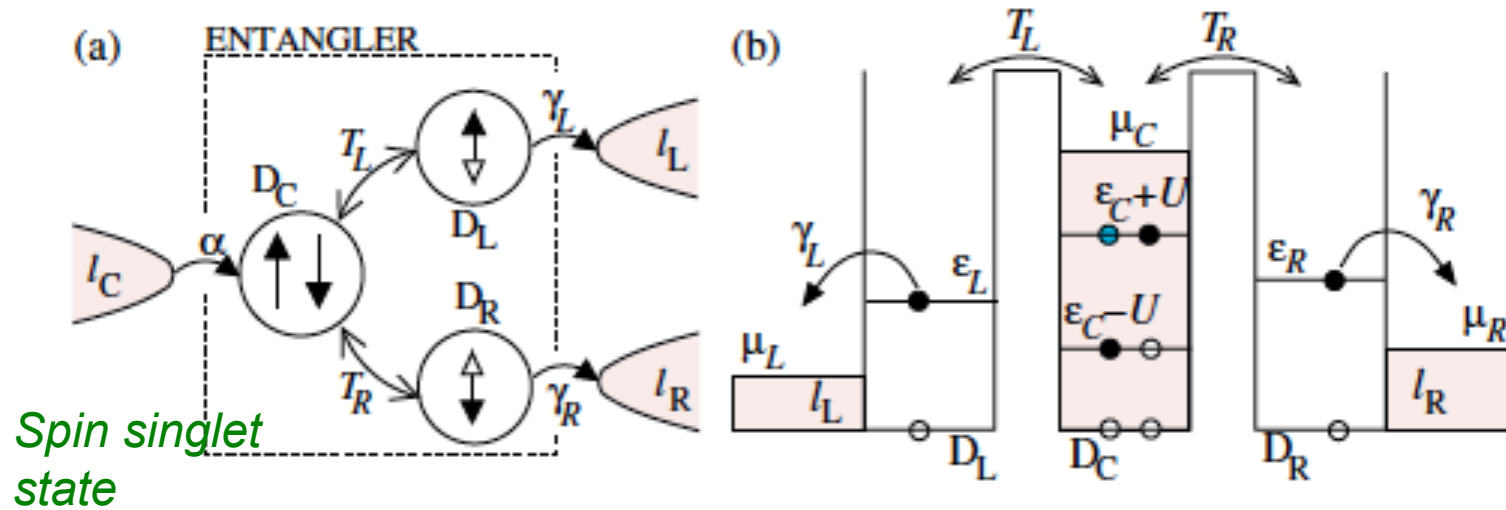
$$\rightarrow -\frac{1}{\sqrt{2}} |T_0\rangle$$

*Post selection  
(only singlet  
electrons in  
each path)*

*Spin triplet  
state*

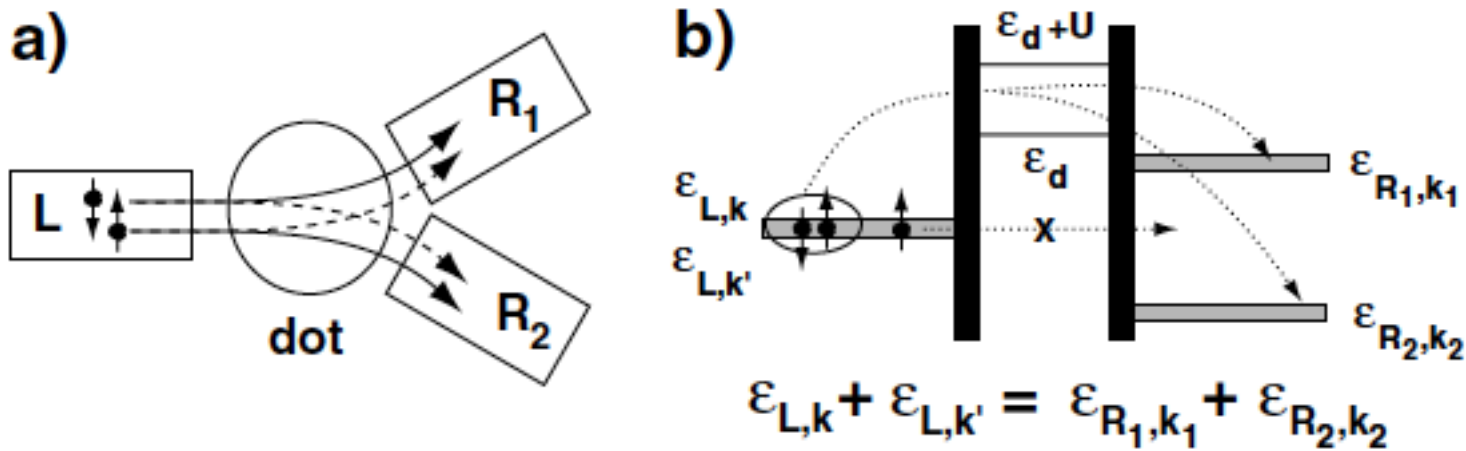
*S. Bose and D. Home, Phys. Rev. Lett. 88, 050401 (2002).*

# Entangle source of triple quantum dots



*D. S. Saraga and D. Loss, Phys. Rev. Lett. 90, 166803 (2003).*

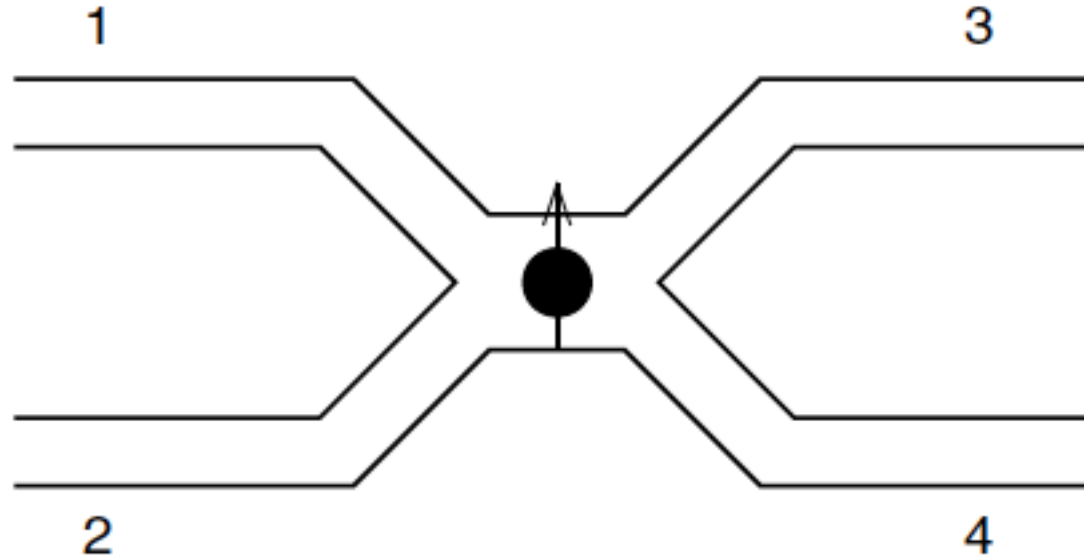
# Entangler with QD and narrow-width chs.



*The channels' band width should be narrow enough.*

*W. D. Oliver, F. Yamaguchi, and Y. Yamamoto, Phys. Rev. Lett. 88, 037901 (2002).*

# Robust entangler with localized spin



*s-d T matrix in Born approx.*

$$\mathcal{T} = J \sum_{l=1,2} \sum_{k,k'} \{ S^+ a_{lk\downarrow}^\dagger a_{lk'\uparrow} + S^- a_{lk\uparrow}^\dagger a_{lk'\downarrow} + S^z [a_{lk\uparrow}^\dagger a_{lk'\uparrow} - a_{lk\downarrow}^\dagger a_{lk'\downarrow}] \}$$

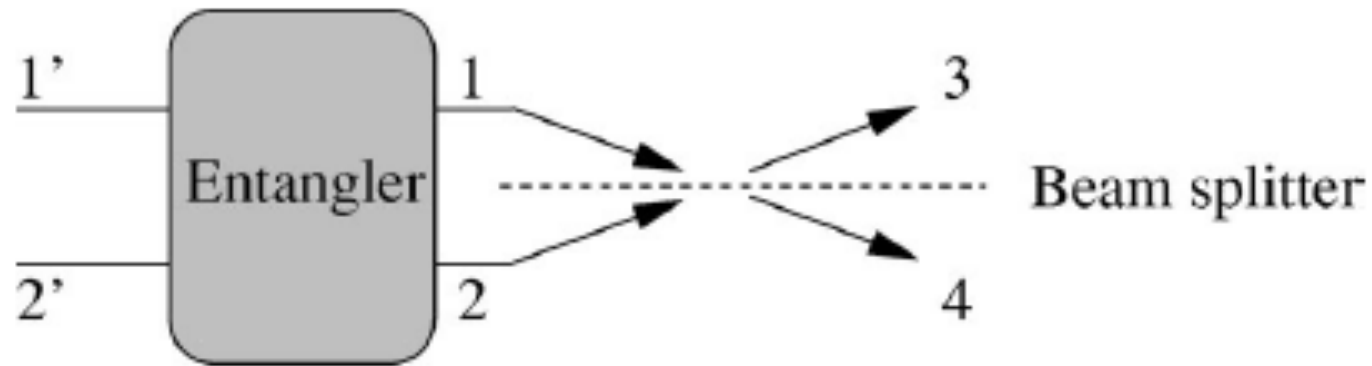
$$a_{1k_F\uparrow}^\dagger a_{2k_F\uparrow}^\dagger |0\rangle \otimes |\downarrow\rangle_S$$

$$\rightarrow -2\sqrt{2}i\pi J\rho |T_0\rangle \otimes |\uparrow\rangle_S$$

$\rho$ : density of states

*A. T. Costa, Jr. and S. Bose, Phys. Rev. Lett. 87, 277901 (2001).*

# Verification of entanglement



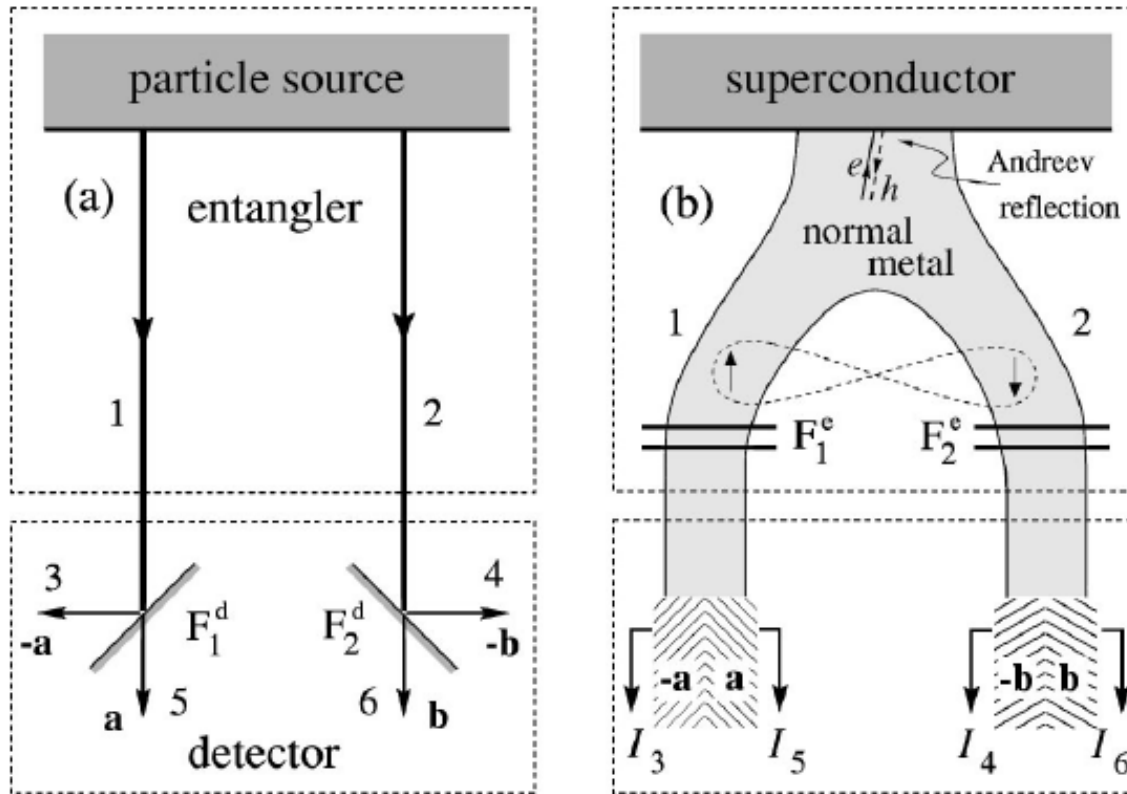
$$\frac{1}{\sqrt{2}}(a_{\uparrow}^{\dagger}b_{\downarrow}^{\dagger} + a_{\downarrow}^{\dagger}b_{\uparrow}^{\dagger})|0\rangle \rightarrow -\frac{1}{\sqrt{2}}(c_{\uparrow}^{\dagger}d_{\downarrow}^{\dagger} + c_{\downarrow}^{\dagger}d_{\uparrow}^{\dagger})|0\rangle$$

$$S_{cross} = \langle \Delta I_3 \Delta I_4 \rangle > 0$$

*G. Burkard, D. Loss, and E. V. Sukhorukov,  
Phys. Rev. B 61, R16303 (2000).*



# Bell inequality analysis



Bell's inequality:  $E(a, b) + E(a', b) + E(a, b') - E(a', b') < 2$

$$E(a, b) = \frac{S_{56} + S_{34} - S_{36} - S_{45}}{S_{56} + S_{34} + S_{36} + S_{45}}$$

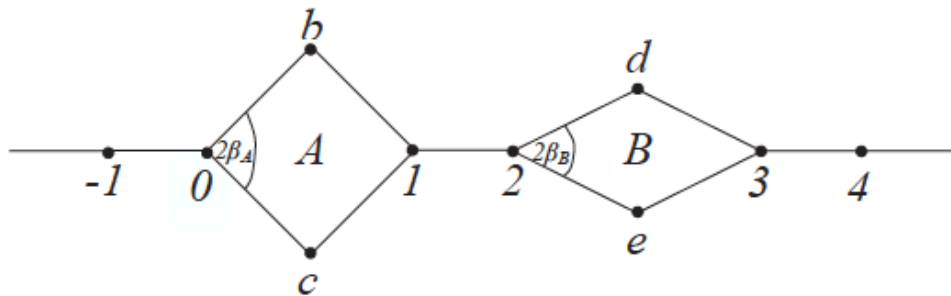
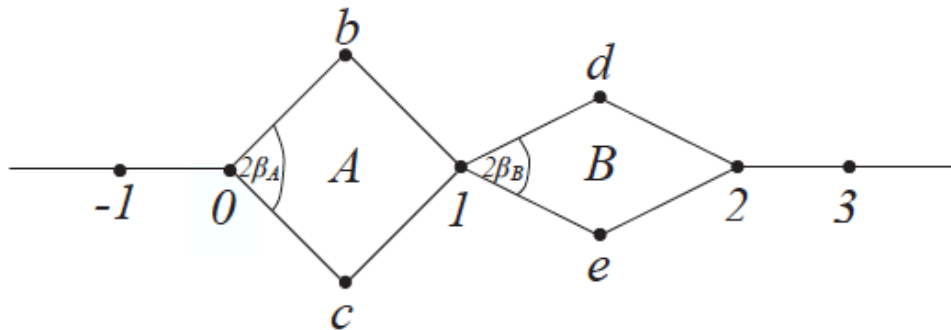
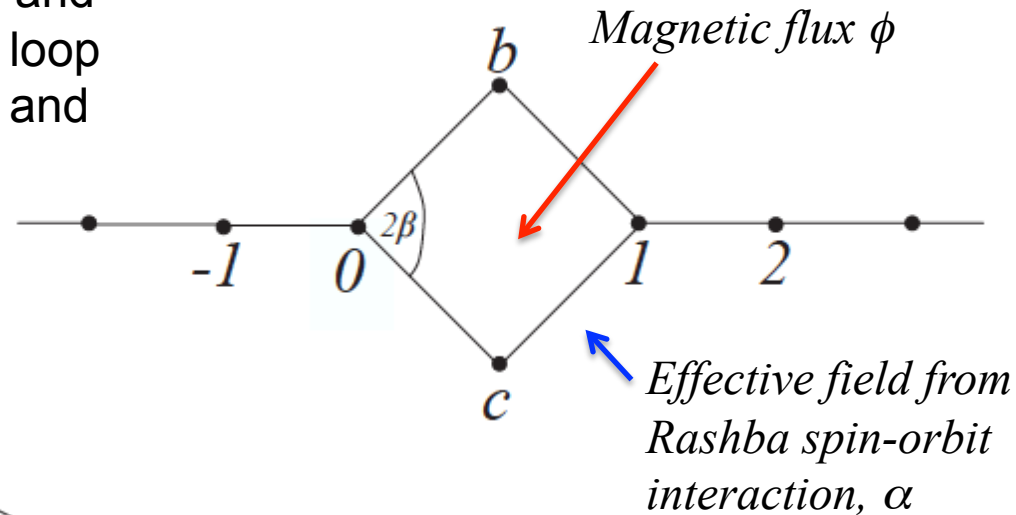
Need spin analyzer/filter.

*S. Kawabata, J. Phys. Soc. Jpn 70, 1210 (2001). N. M.*

*Chtchelkatchev, et al., Phys. Rev. B 66, 161320(R) (2002).*

# Perfect spin filter

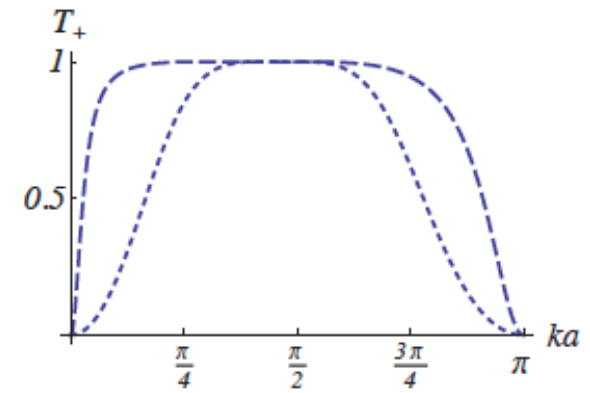
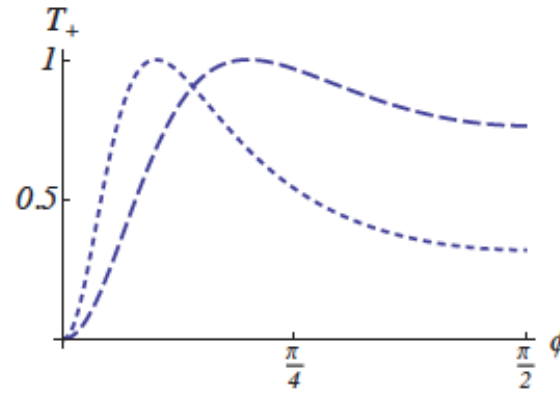
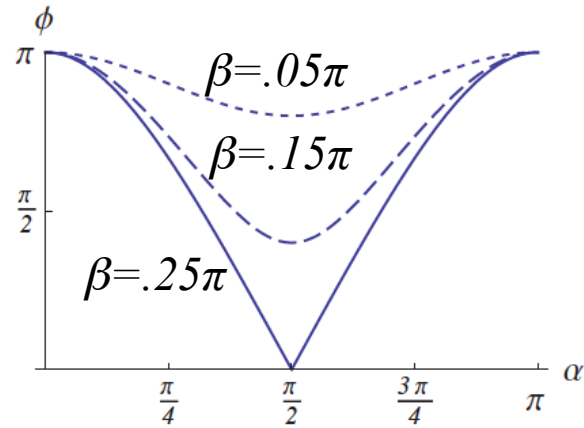
Controlled spin-orbit interaction and magnetic flux in a diamond-like loop  
 - works as an emitter, rotator, and detector of flying spin qubits



Coupled diamonds offer more flexible, and ideal realization of Datta-Das spin transistor

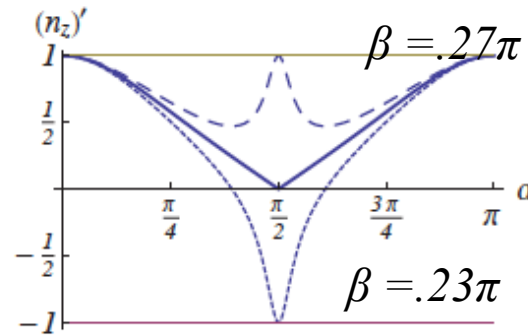
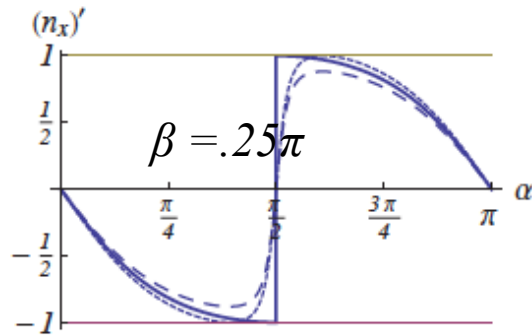
*A. Aharony, Y. Tokura, Guy Z. Cohen, O. Entin-Wohlman, and S. Katsumoto, Phys. Rev. B 84, 035323 (2011).*

# Model calculations



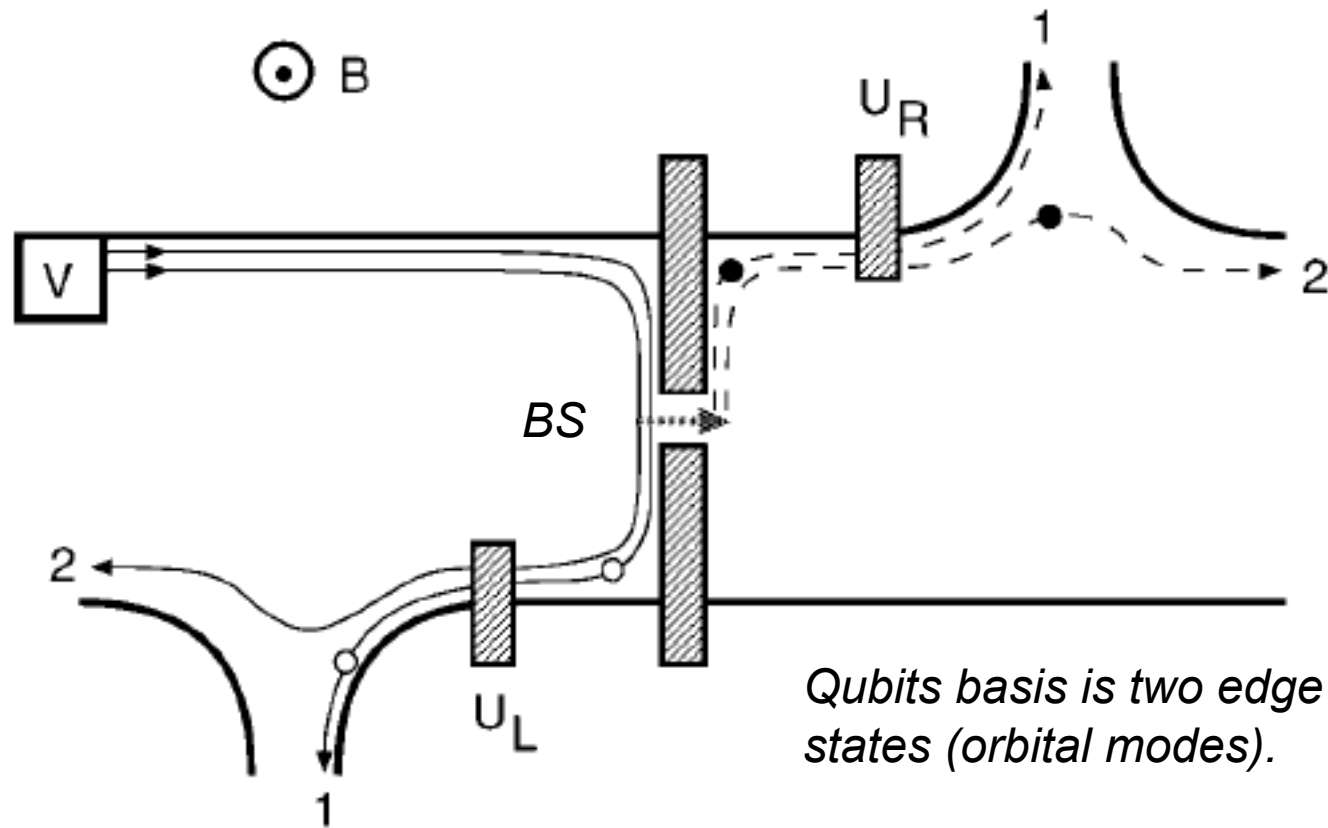
Condition of full fibetween ltering the AB flux  $\phi$  and the Rashba SOI strength  $\alpha$

Transmission of the polarized electrons,  $T_+$ . LHS: in the band center ( $\varepsilon = 0$ ) versus the AB flux  $\phi$ . RHS: versus  $ka$ .



Outgoing spin components as a function of the Rashba SOI strength  $\alpha$ . The lower panel shows the actual spin directions in the xz-plane for  $\beta = \pi/4$ , as  $\alpha$  increases from zero to  $\pi$  (left to right).

# Electron-hole entanglement



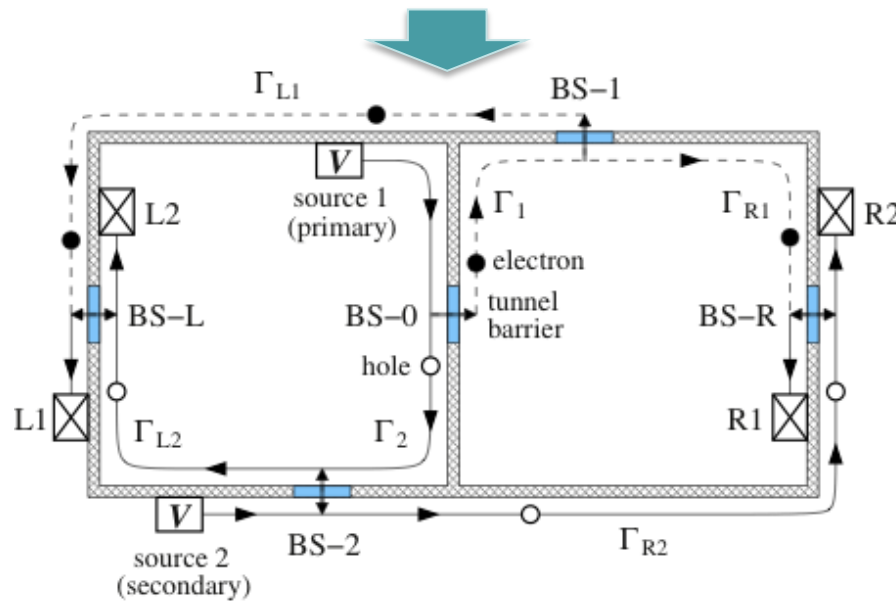
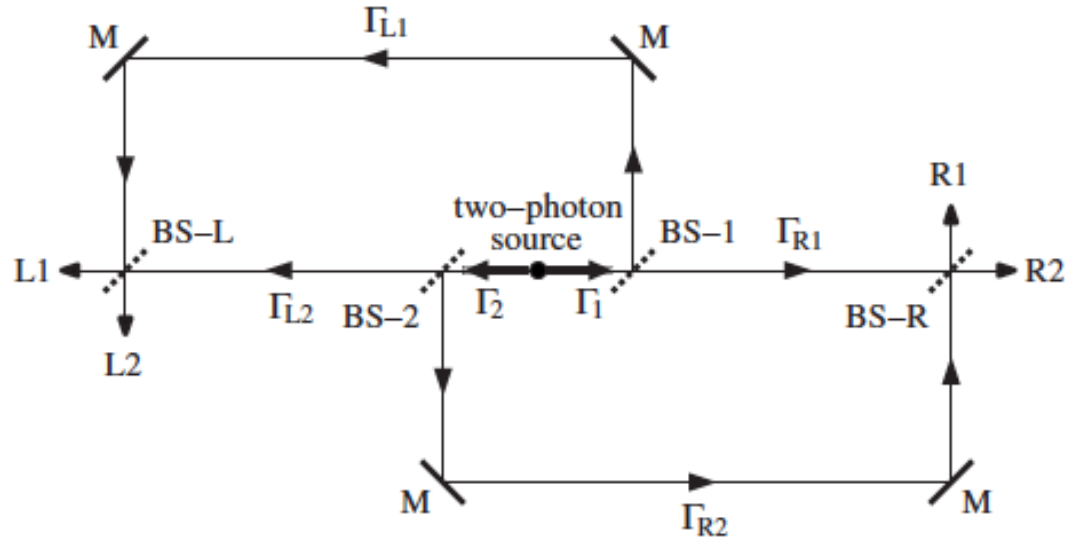
$U_R$  and  $U_L$  are used for the analysis of Bell-inequality

$$\varepsilon = E(U_L, U_R) + E(U'_L, U_R) + E(U_L, U'_R) - E(U'_L, U'_R),$$

$$\varepsilon_{max} = 2\sqrt{1 + C^2} \quad C: \text{concurrence}$$

*C. W. J. Beenakker, C. Emary, M. Kindermann, and J. L. van Velsen, Phys. Rev. Lett. 91, 147901 (2003).*

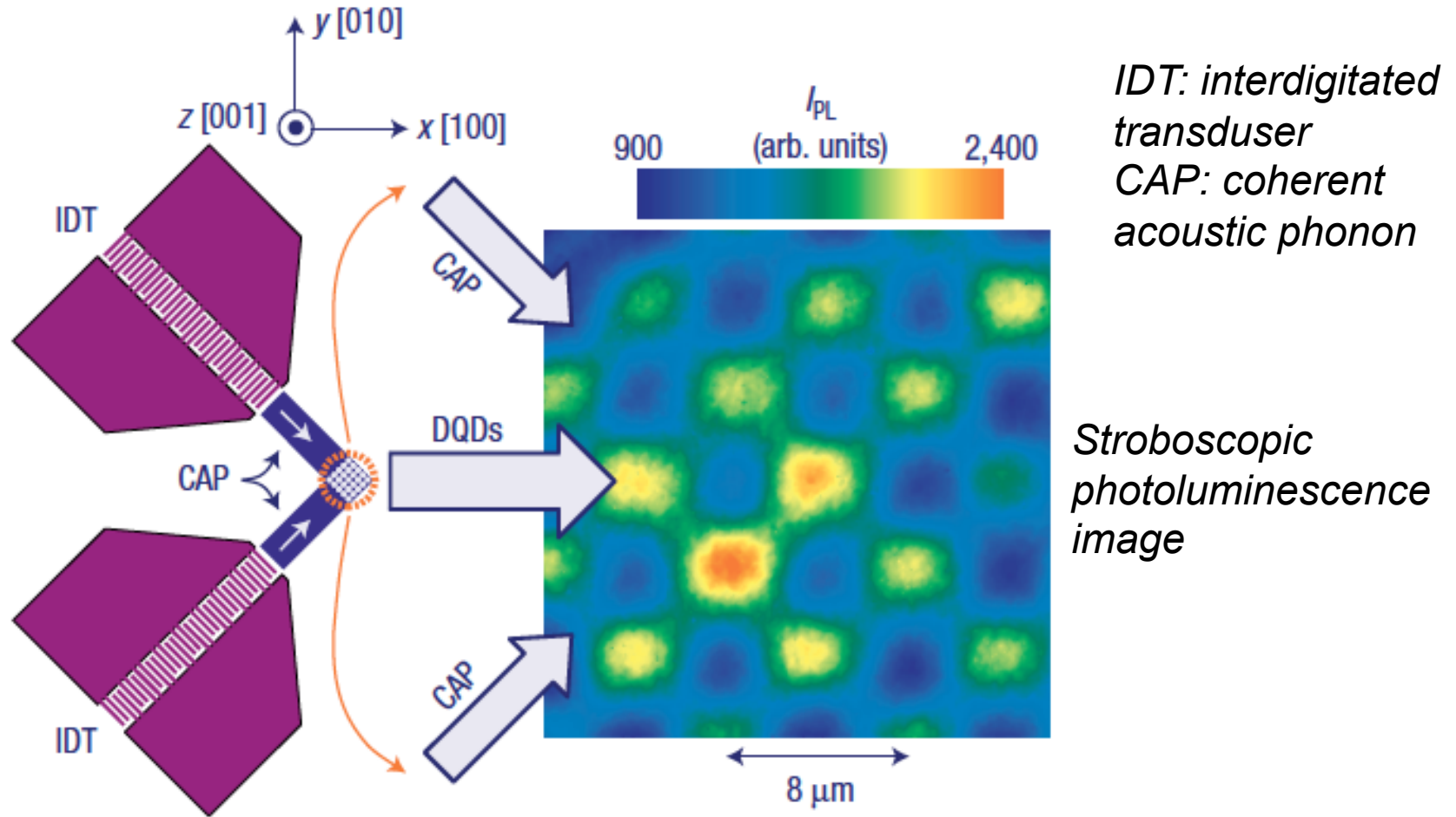
# Electron-hole interferometer



*Proposed device using  
single edge state*

*D. Frustaglia and A. Cabello, Phys. Rev.  
B 80, 201312R (2009).*

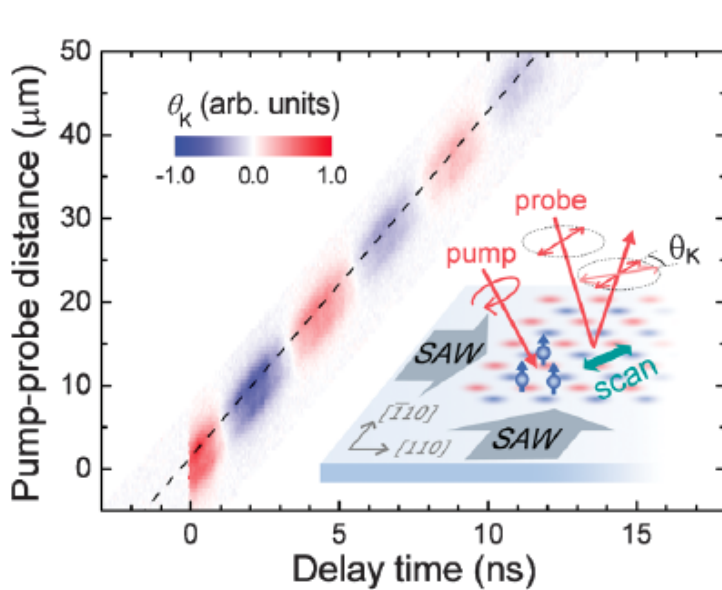
# Encapsulated flying qubits



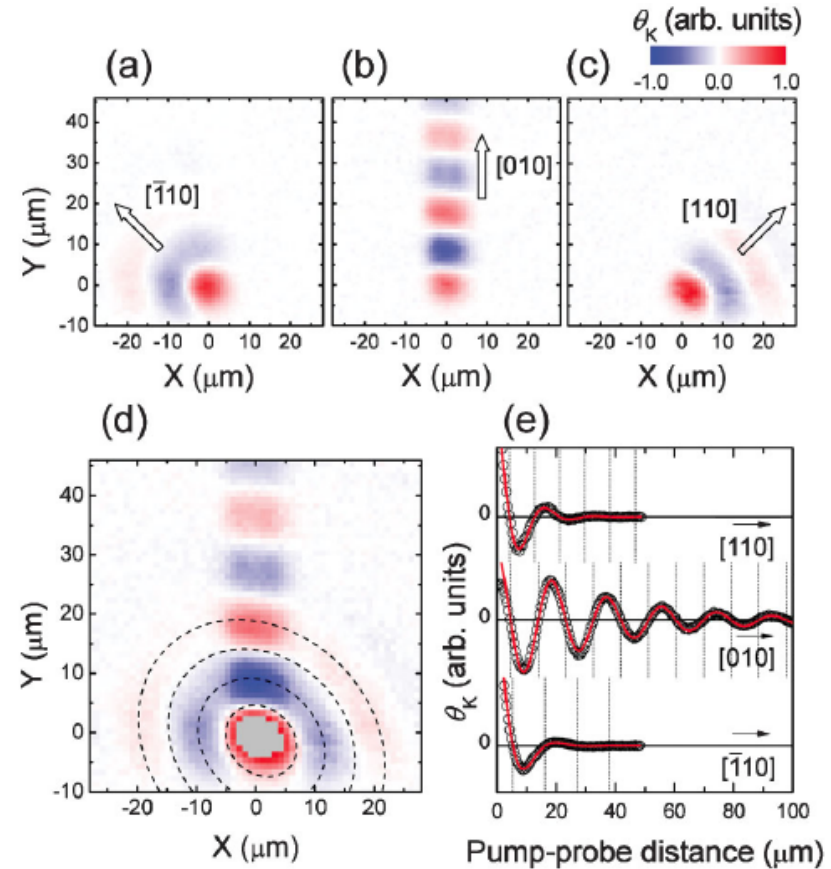
*Piezo-electric material, like GaAs, forms moving (dynamic) quantum dots (DQDs) by the surface acoustic waves (SAWs).*

*J. A. H. Stotz, R. Hey, P. V. Santos and K. H. Ploog, Nature Materials 41, 585 (2005).*

# Spin rotates



*Spatiotemporal evolution of the magneto-optic Kerr Rotation signal*

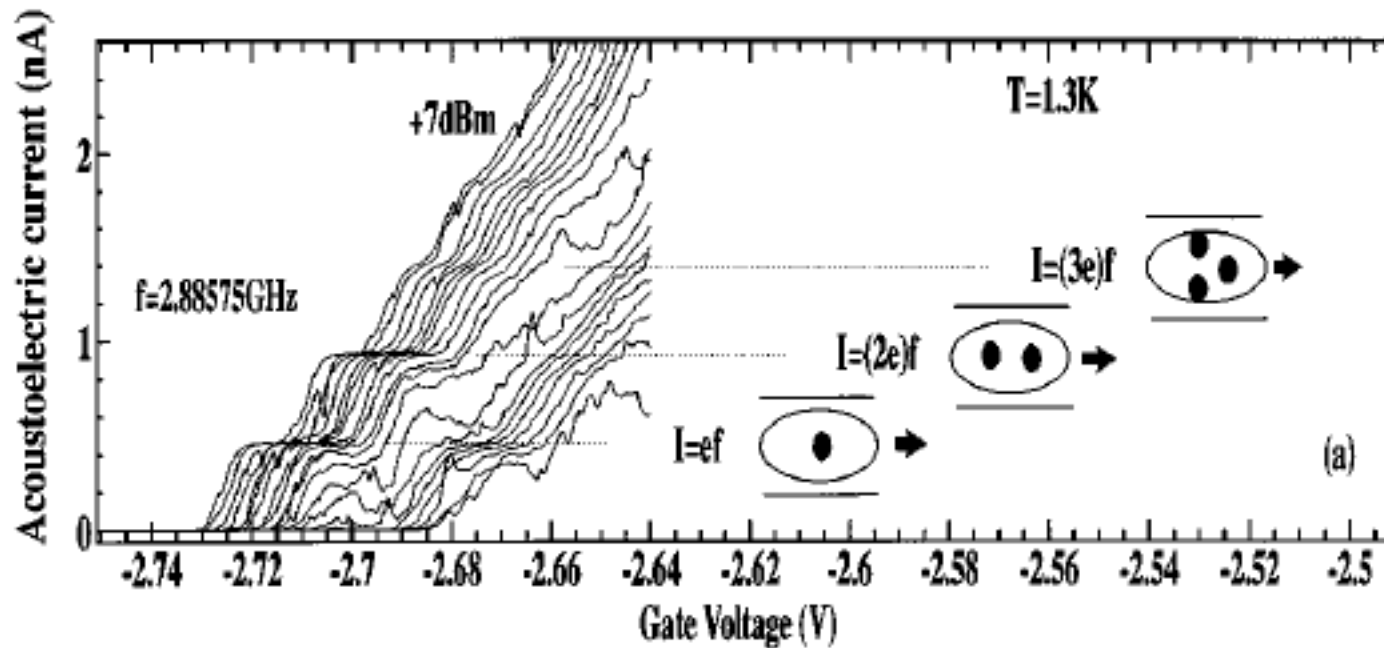


*The spin rotation is induced from the internal magnetic field originating from the spin-orbit interactions.*

*Spin coherence length > 100 μm!*

*H. Sanada, et al., Phys. Rev. Lett. 106, 216602 (2011).*

# Quantized current by SAW



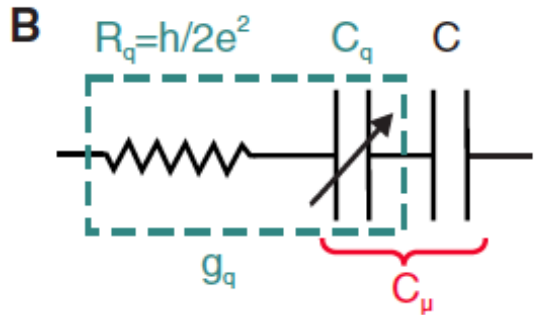
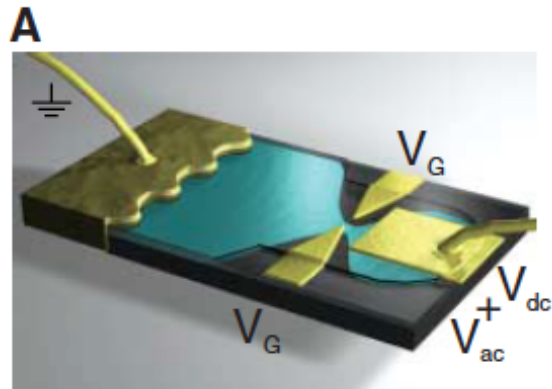
*SAW can accommodate a few electrons per period.*

$$I = nef$$

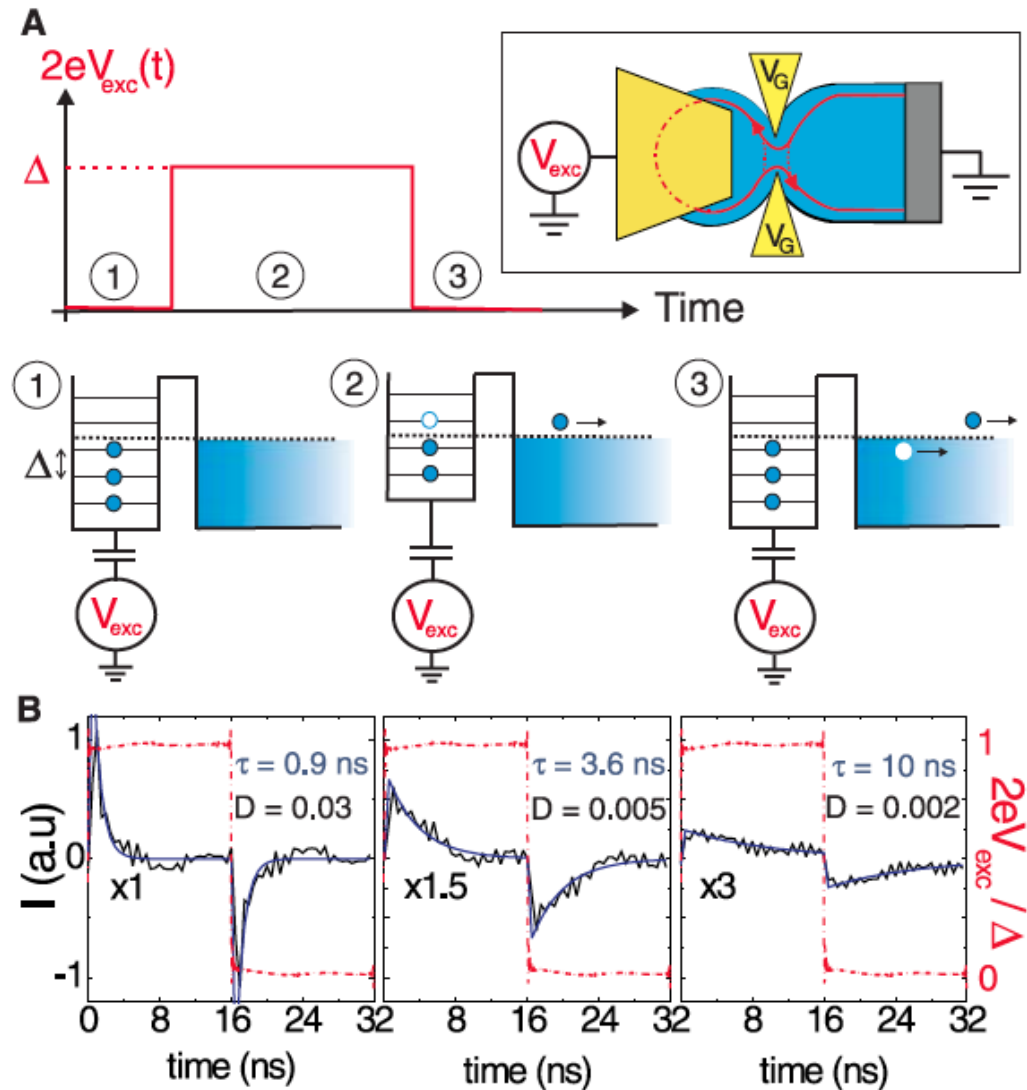
*V. I. Talyanskii, et al., Phys. Rev. B 56, 15180 (1997).*



# Single electron source

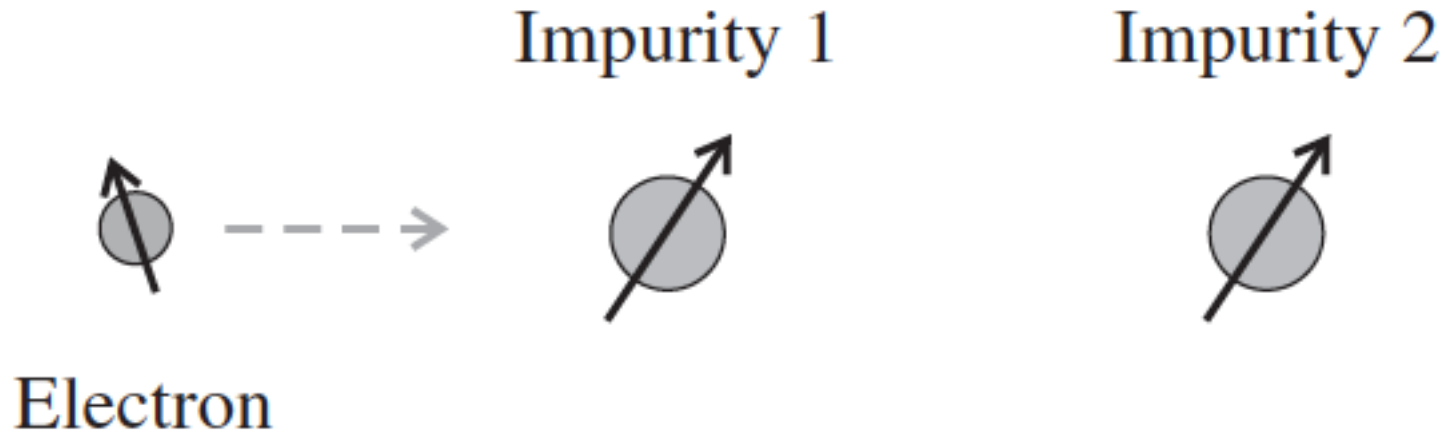


Pulse signal to the gate electrodes, release single electron/hole to the reservoir



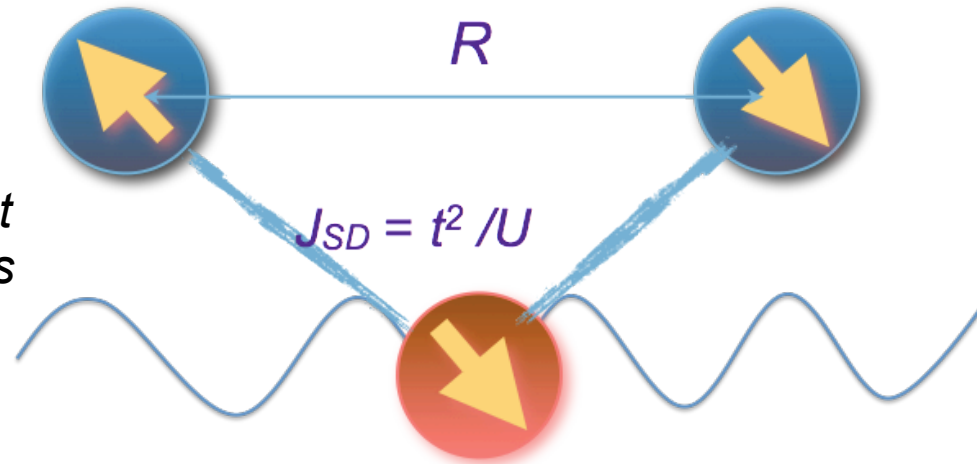
*J. Gabelli, et al., Science 313, 499 (2006).*  
*G. Feve, et al., ibid 316, 1169 (2007).*

# Flying qubit as an entangler



M. A. Ruderman and C. Kittel, *Phys. Rev.* **96**, 99 (1954).  
T. Kasuya, *Prog. Theor. Phys.* **16**, 45 (1956).  
K. Yoshida, *Phys. Rev.* **106**, 893 (1957).

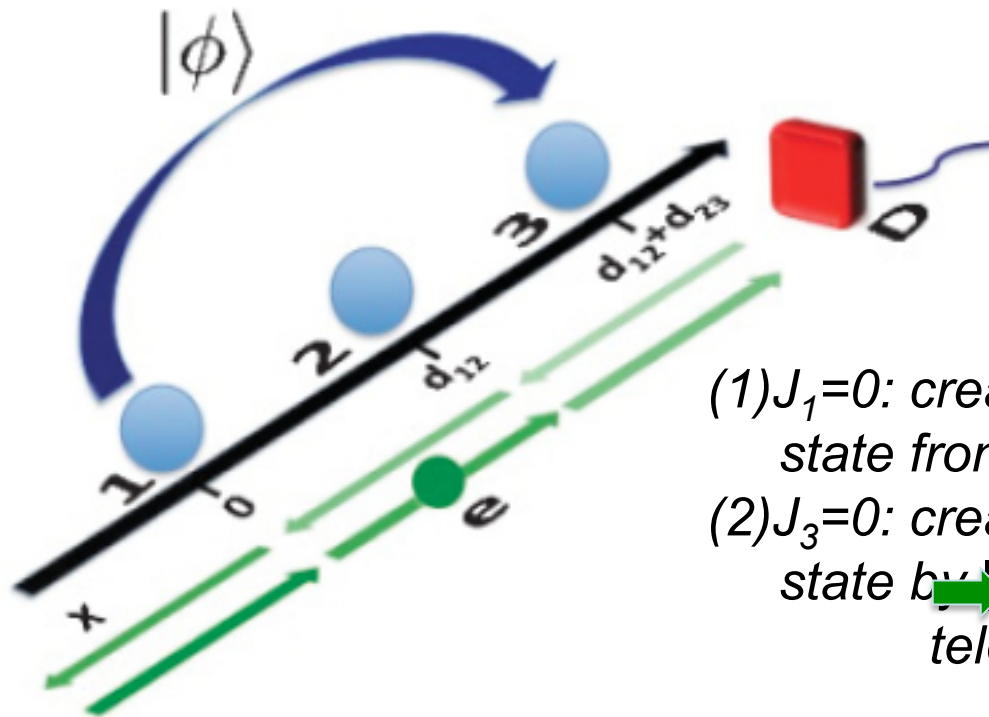
*RKKY interaction is an example of entanglement by flying qubits (electrons in the reservoirs).*



*Y. Avishai and Y. Tokura, *Phys. Rev. Lett.* **87**, 9703 (2001).*

*A. T. Costa, Jr., S. Bose, and Y. Omar, *Phys. Rev. Lett.* **96**, 230501 (2006).*

# Quantum teleportation with flying qubits



- (1)  $J_1=0$ : create maximally entangled state from  $|u\rangle_2$  and  $|d\rangle_3$ .
- (2)  $J_3=0$ : create maximally entangled state by  $|\phi\rangle_1$  and  $|\psi\rangle_2$   
teleportation  $|\phi\rangle_1 \rightarrow |\phi\rangle_3$

$$\mathcal{H} = \{J_1\vec{S}_1 + J_2\vec{S}_2 + J_3\vec{S}_3\} \cdot \vec{\sigma}$$

Trick: for (1) and  $J_2=J_3$ , no dynamics by  $H=J(S_2+S_3)\sigma$  for spin singlet!

Usage of SAW would be promising.

*F. Ciccarello, S. Bose, and M. Zarcone, Phys. Rev. A 81, 042318 (2010).*

# Conclusions

- *I reviewed recent progress on the research of realizing flying qubits in semiconductor systems.*
- *There are many proposals to generate entangled flying qubits, but not yet experimentally confirmed.*
- *Singlet electron sources and spin filters are proposed and start being demonstrated.*
- *Surface acoustic wave is a promising technology since it generates encapsulated flying qubits with amazingly long spin coherence length.*
- *Using flying qubits and an entangler of localized qubits is another interesting direction of the research.*

# Thank you.

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