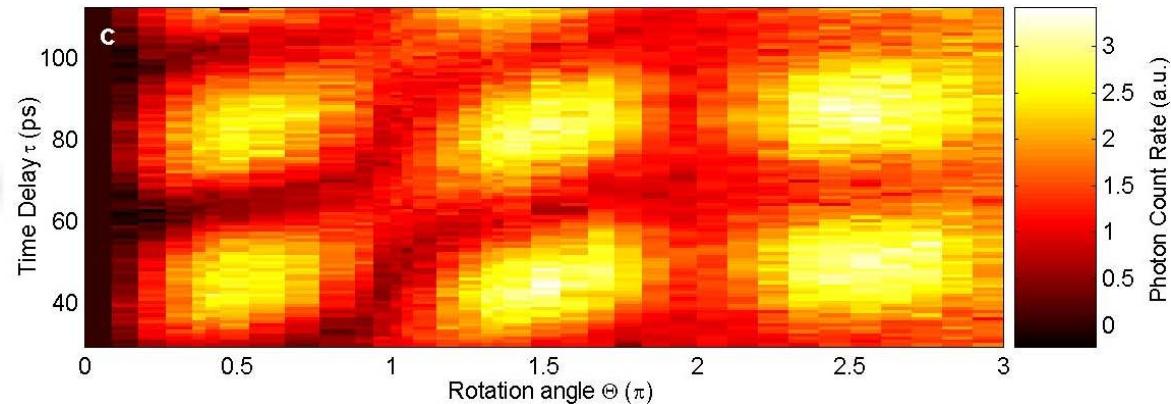
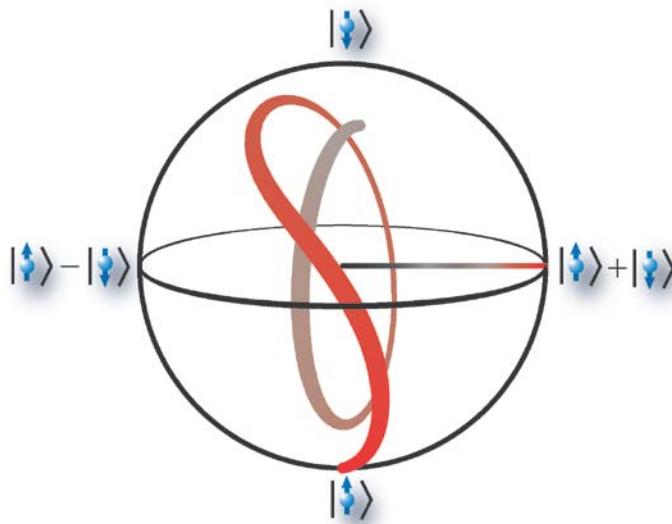


# Ultrafast Optical Control of Semiconductor Spin Qubits toward Surface Code Quantum Computing



Yoshihisa Yamamoto  
Stanford University & National Institute of Informatics

FIRST最先端研究開発支援プログラム 量子情報処理プロジェクト  
第1回夏期研修会（沖縄、2010年8月18日～8月28日）

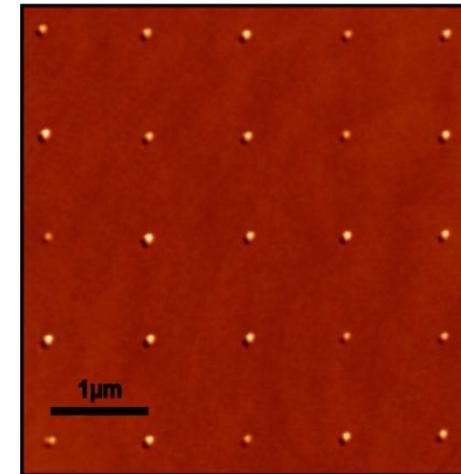
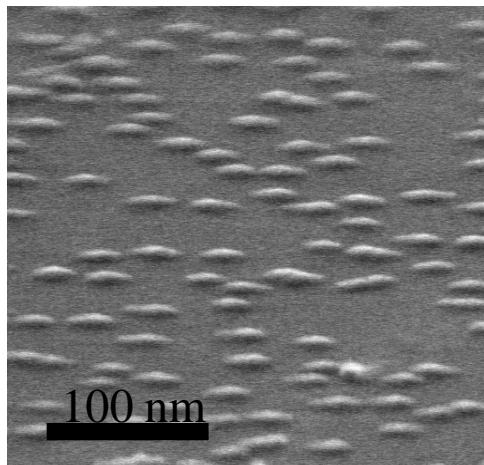
# Outline

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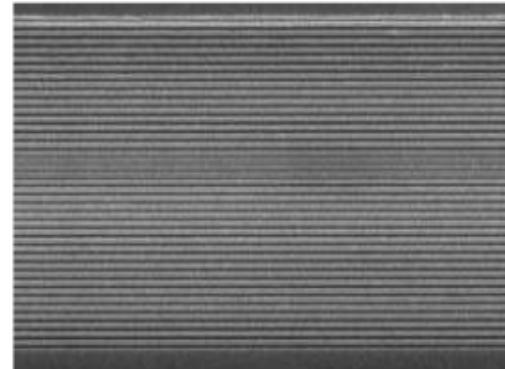
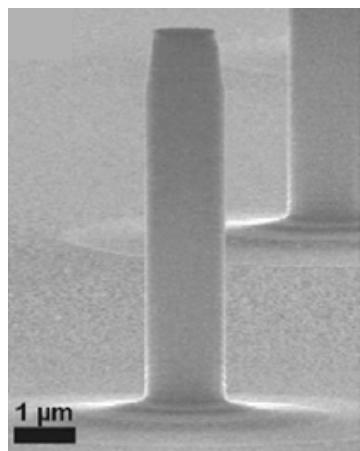
- Physical qubits – Quantum dot spins in planar microcavity –
- Goal – Fault tolerant quantum information processing –
- Qubit initialization and measurement
- Single qubit gate
- Two qubit gate
- Decoherence time
- Indistinguishable single photons and entanglement distribution
- Topological surface code architecture

# Physical Qubits

## — Cavity QED Systems with Single-Electron-Doped Quantum Dots —



“Random” → “Scalable”



A post-microcavity with top and bottom DBRs  
and self-assembled InGaAs QDs

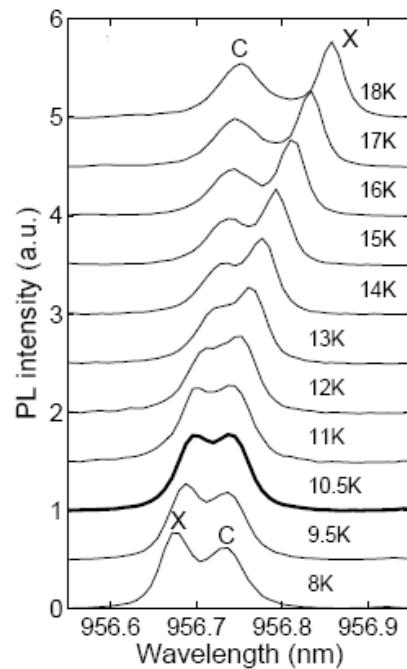
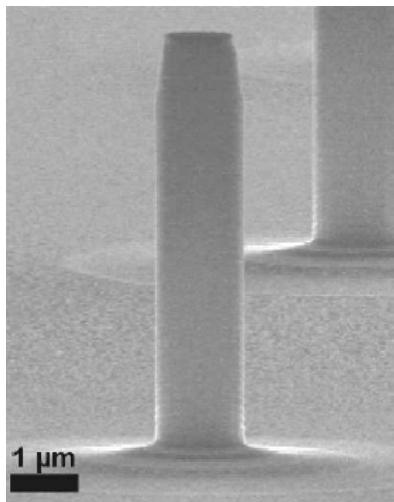
D. Press, S. Gotzinger, S. Reitzenstein, C. Hofmann, A. Löffler,  
M. Kamp, A. Forchel, and Y. Yamamoto, *PRL* **98**, 117402 (2007).

A simple planar microcavity with  
2D lattice of site-controlled QDs

C. Schneider, M. Strauss, T. Sunner,  
A. Huggenberger, D. Wiener, S. Reitzenstein, M. Kamp,  
S. Höfling and A. Forchel *APL* **92**, 183101 (2008)

# Single QD Cavity QED System with Enhanced Spontaneous Emission

D. Press et al. Phys. Rev. Lett. 98, 117402 (2007)



InAs QD exciton lifetime in free space 620ps



Reduced lifetime in resonant cavity 11.3ps



$$\text{Purcell (cooperativity) factor } F_p = \frac{\gamma}{\gamma_x} - 1 = 61$$

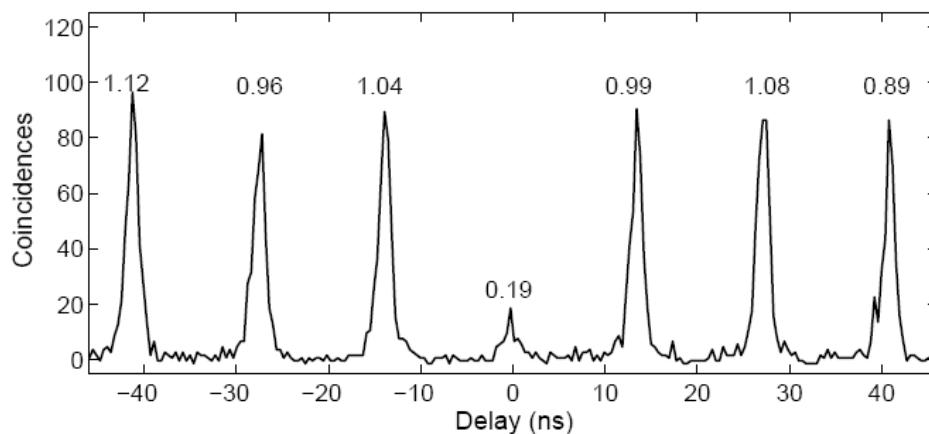
$$\text{Quantum efficiency} = \frac{F_p}{F_p + 1} \times \frac{\gamma_c}{\gamma_c + \gamma_x} = 97\%$$

$g^{(2)}(0) = 0.19$  under resonant pumping



Direct proof of a single QD cavity QED system

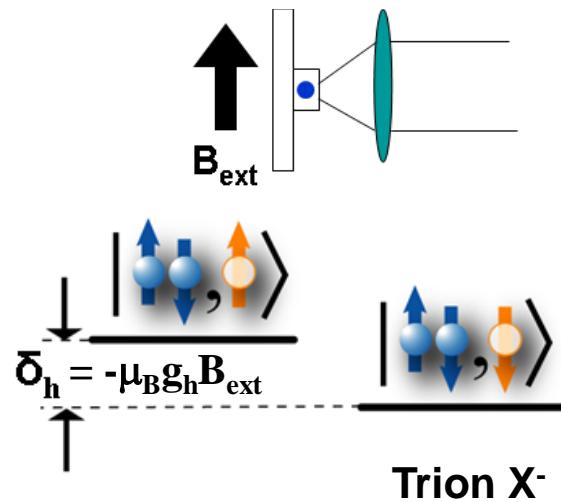
(Also see K. Hennessy et al., Nature 445, 896 (2007))



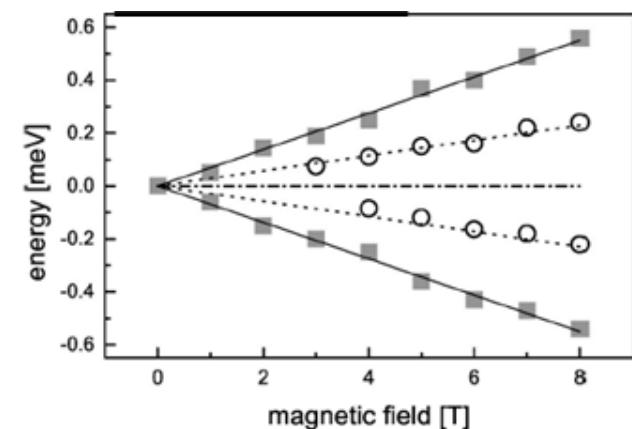
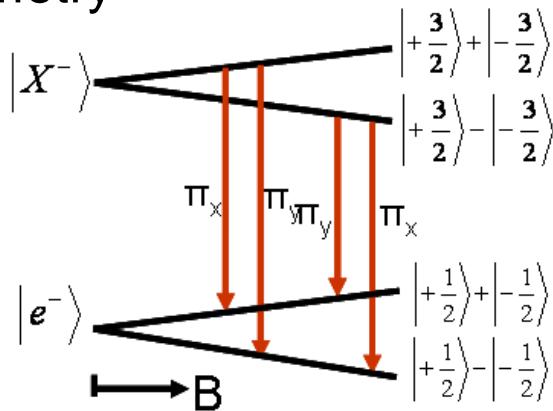
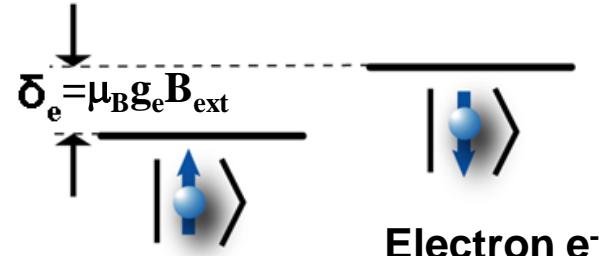
# Magnetic Spectrum of Charged Exciton (Trion) in InAs Quantum Dot

## — Artificial Three-Level Atom in Lambda Configuration —

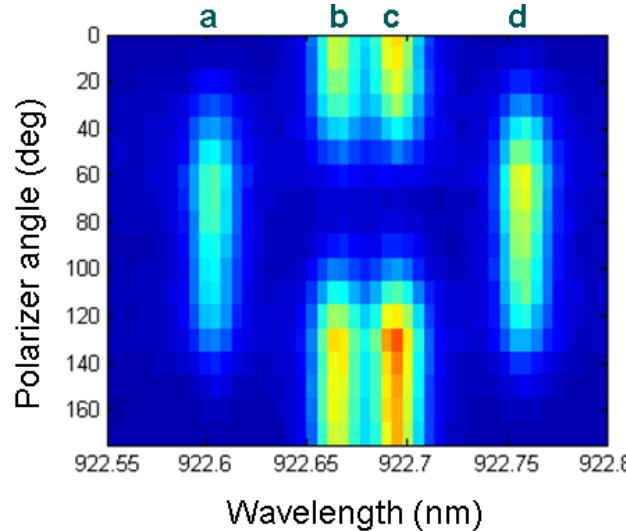
Magnetic field in Voigt geometry



Electron spins in singlet  
Spin is governed by heavy hole



M. Bayer et al., Phys. Rev. B 65, 195305 (2002)



D. Press et al., Nature 456, 218 (2008)

# Outline

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- Physical qubits – Quantum dot spin lattice in planar microcavity –
- Goal – Fault tolerant quantum information processing –
- Qubit initialization and projective measurement
- Single qubit gate
- Two qubit gate
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- Indistinguishable single photons and entanglement distribution
- Topological surface code architecture

# Motivation – Why Optically Controlled QDs as Physical Qubits? –

## Fault-tolerant quantum information processing systems

- Long distance quantum repeaters based on nested purification protocol  
Concept: H.J. Briegel, W. Dür, J.I. Cirac and P. Zoller, *PRL* **81**, 5932 (1998)  
Fault-tolerant Implementation with QD spins: T.D. Ladd, P. van Loock, K. Nemoto,  
W.J. Munro and Y. Yamamoto, *NJP* **8**, 184 (2006)
- One-way quantum computers based on topological surface codes  
Concept: R. Raussendorf and J. Harrington, *PRL* **98**, 190504 (2007)  
Fault-tolerant Implementation with QD spins: R. Van Meter, T.D. Ladd, A.G. Fowler and  
Y. Yamamoto, quant-ph/0906271 (2009)

## Unique features of QDs as “artificial atoms”

- i ) Large oscillator strength:  $f_{\text{exciton}} \geq 10-100 \times f_{\text{atom}}$   
→ Ultrafast optical control with small optical power, large Purcell (cooperativity) factor
- ii ) Permanent placement of 2D spin lattice in monolithic planar microcavity  
→ Scalable system (Unique mode spot size and cavity mediated one/two-qubit gate)
- iii) Excitonic transition wavelength tailored to  $\lambda=1.3/1.5 \mu\text{m}$   
→ Natural interface to long-distance optical communication networks

# Outline

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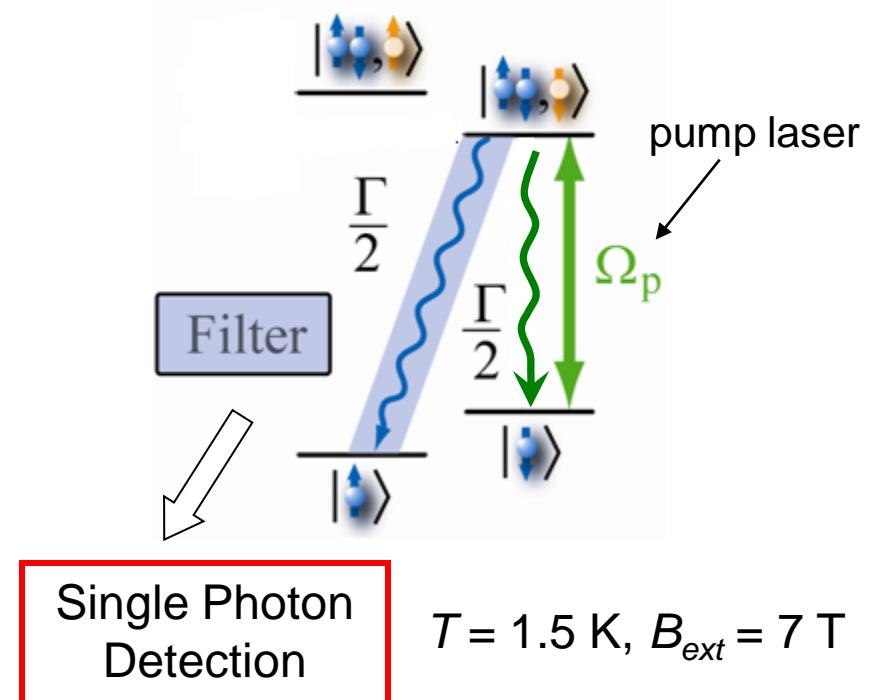
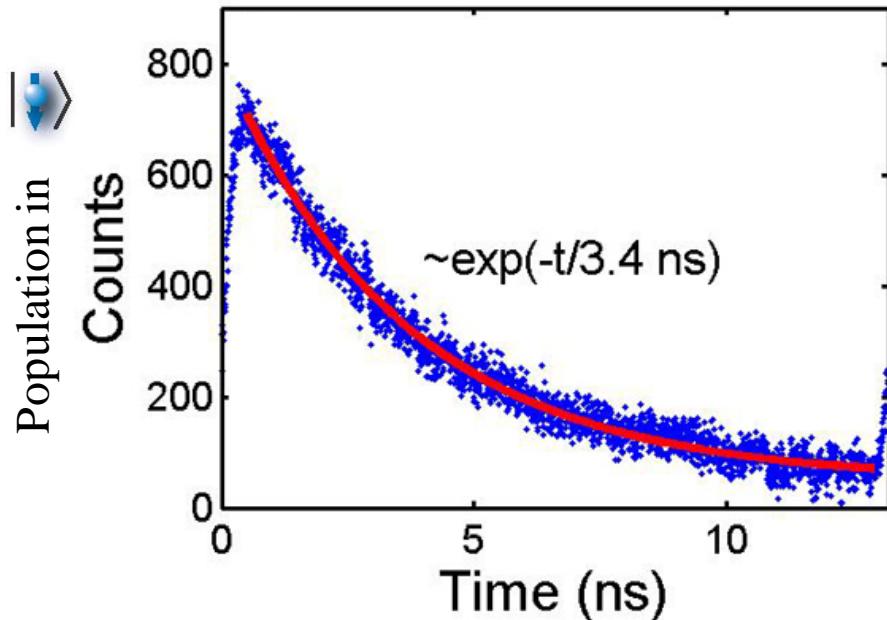
- Physical qubits – Quantum dot spin lattice in planar microcavity –
- Motivation – Fault tolerant quantum information processing –
- **Qubit initialization and measurement**
- Single qubit gate
- Two qubit gate
- Decoherence time
- Indistinguishable single photons and entanglement distribution
- Topological surface code architecture

# Initialization and Measurement of Electron Spins

Ensemble of spins: K.M. Fu et al., Nature Physics 4, 780 (2008)

Single spin: D. Press et al., Nature 456, 218 (2008)

Optical pumping + Rotation pulse of  $\Theta = \pi$



Initialization fidelity:  
 $F_0 = 92 \pm 7\%$

Time for initialization:  
10<sup>-3</sup>sec (thermalization scheme) → 10<sup>-9</sup>sec (optical pumping)

# Outline

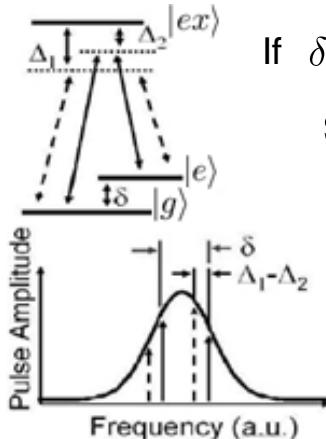
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- Physical qubits – Quantum dot spin lattice in planar microcavity –
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# Spin Rotation with Single Optical Pulse

S. Clark et al., Phys. Rev. Lett. 99, 040501 (2007)

- A single broadband optical pulse can implement an arbitrary one-bit gate with fidelity of 0.999.



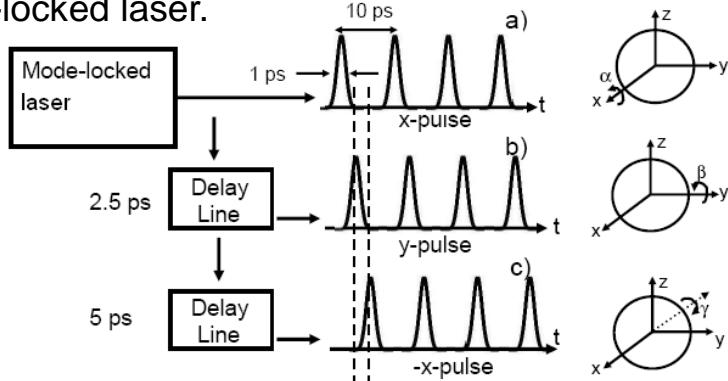
If  $\delta \ll \Omega_0, \Omega_1 \ll \Delta$ , an effective Rabi frequency

$$\Omega_{\text{eff}} = \frac{\Omega_0 \Omega_1^*}{2\Delta} \simeq \frac{|\Omega(t)|^2}{2\Delta}$$

$$\Omega(t) = \frac{\mu E(t)}{\hbar}$$

rotation angle  $\int \Omega_{\text{eff}} dt$  is proportional to pulse energy

- A system clock is provided by the pulse arrival time from the mode-locked laser.

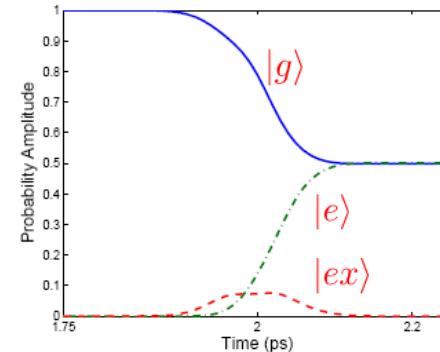


Arbitrary single qubit gates SU(2) can be implemented in one-half of Larmor oscillation period.

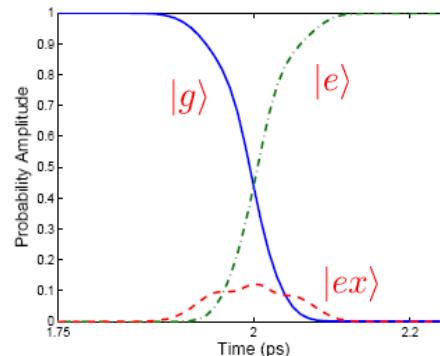
Numerical simulation based on the three-level master equation

$$\tau \ll T_1, T_2$$

100fs  $\pi/2$  - pulse



100fs  $\pi$  - pulse



Experiment with an ensemble of donor spins : K.M. Fu et al., Nature Physics 4, 780 (2008)

# Single Spin Experiment: Coherent Rabi Oscillation

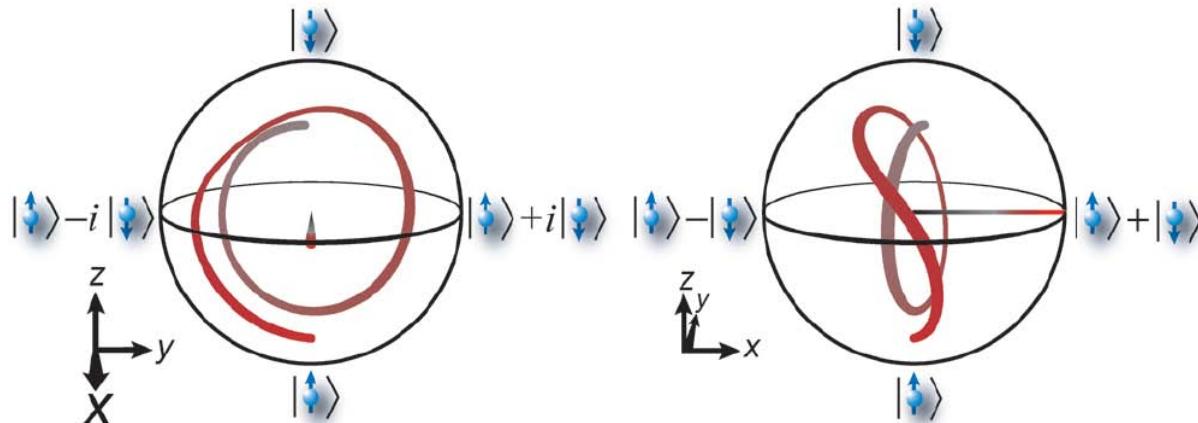
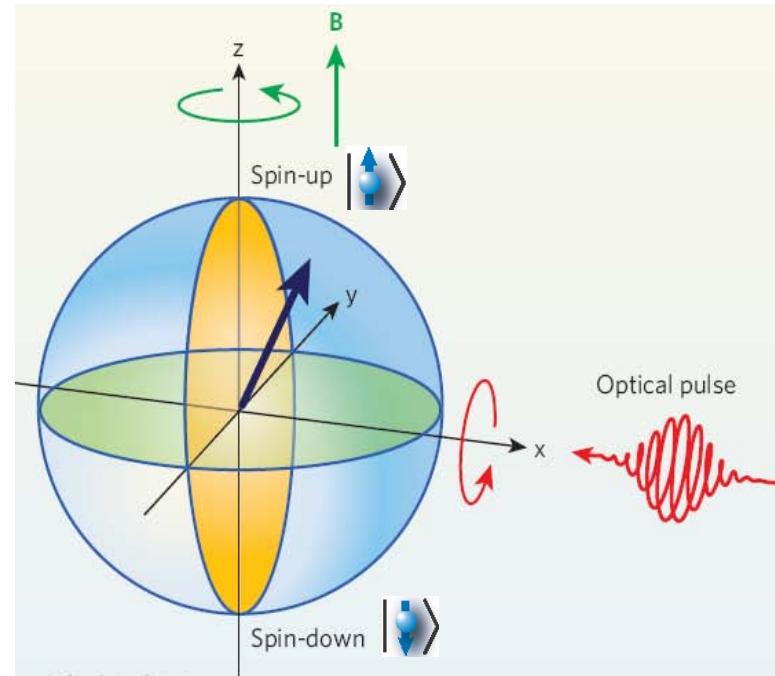
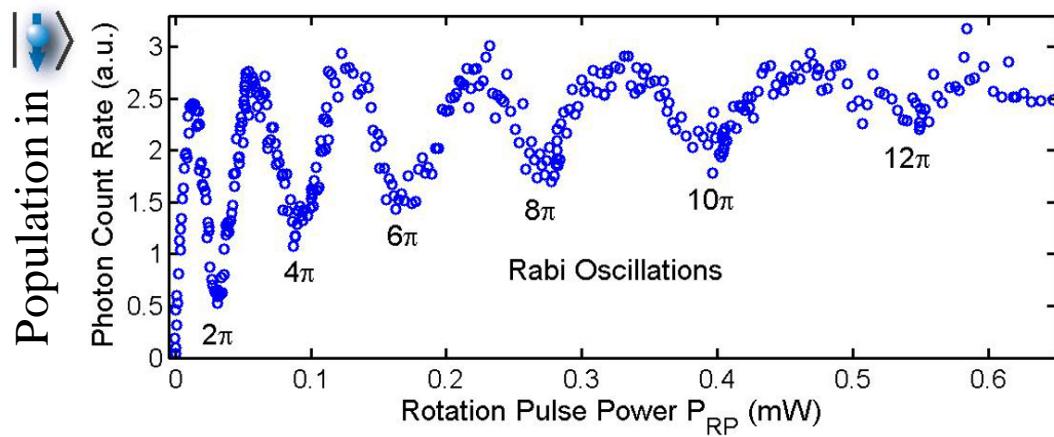
D. Press et al., Nature 456, 218 (2008)

Circularly-polarized 4 ps Rotation Pulse

$$\delta_e = 26 \text{ GHz}$$

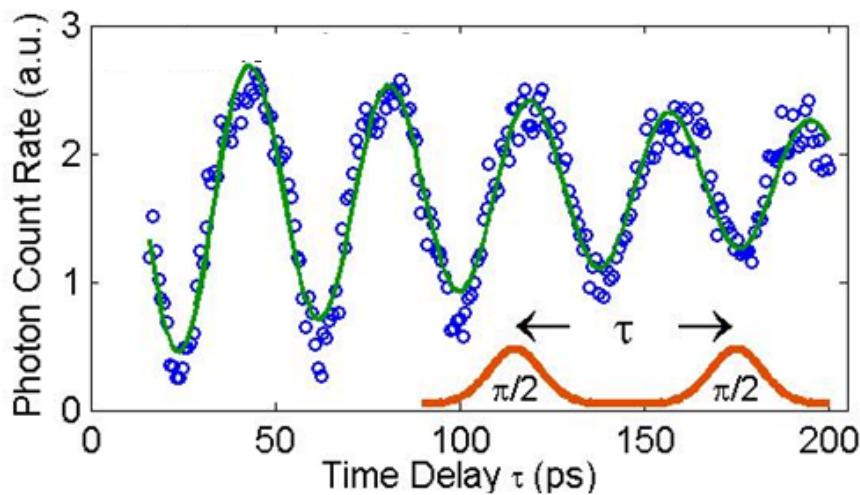
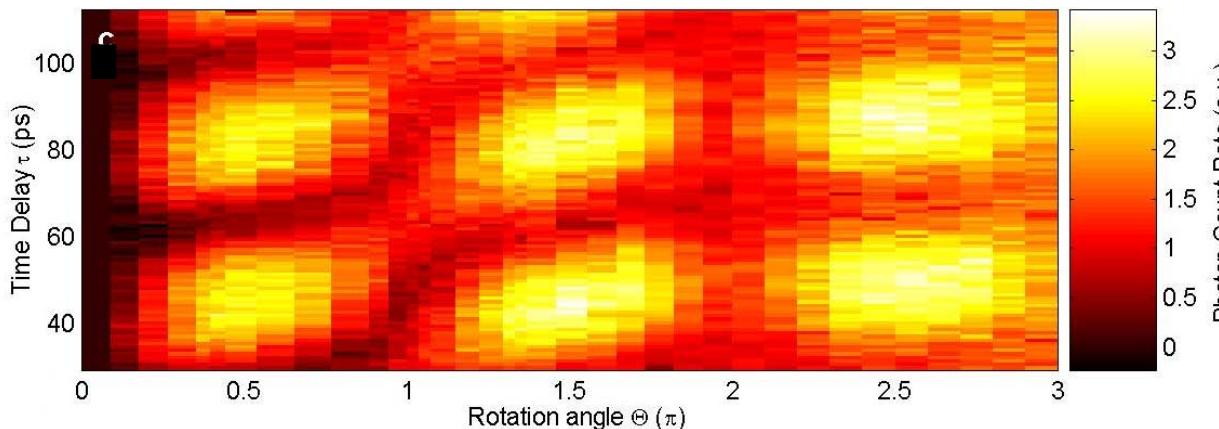
$$\text{BW} = 110 \text{ GHz}$$

$$\Delta = 270 \text{ GHz}$$

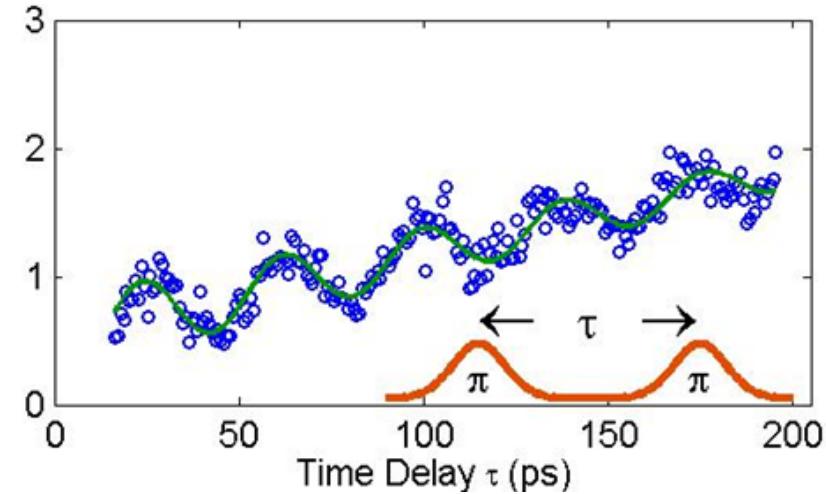


(cf. J. Berezovsky et al.,  
Science 320, 349 (2008))

# Two-Pulse Experiment: Ramsey Interference



$\pi/2$ -pulse fidelity:  $F_{\pi/2} \sim 94\%$



$\pi$ -pulse fidelity:  $F_\pi \sim 91\%$

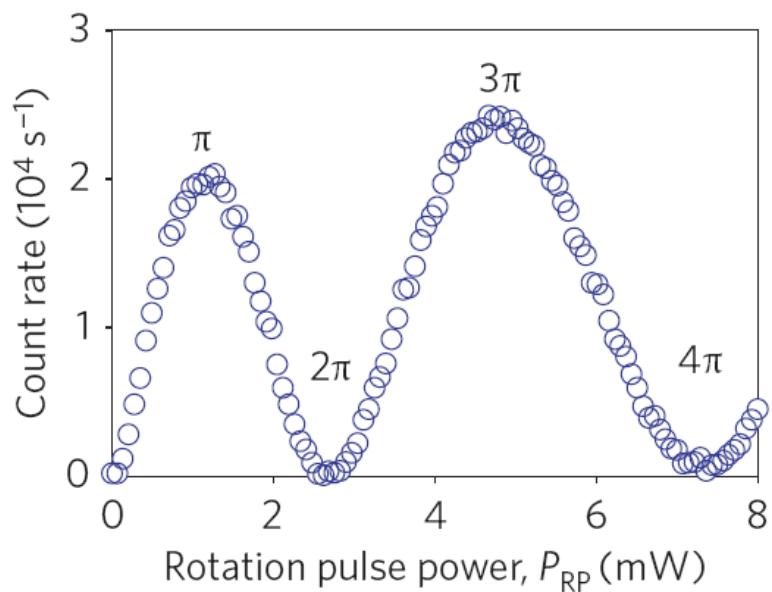
Total time for SU(2) single qubit gates ( $\lesssim$  one-half of Larmor period)

D. Press *et al.*, Nature 456, 218 (2008)

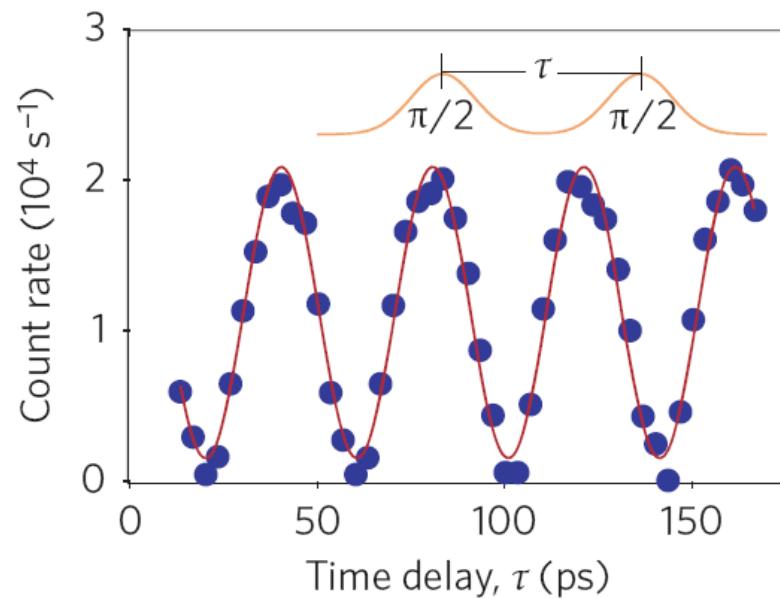
# Improved Gate Fidelity for a Single Spin in a Microcavity

D. Press et al., Nature Photonics 4, 367 (2010)

Coherent Rabi oscillation experiment



Ramsey Interference experiment



Single qubit gate fidelity:  $F=98\sim99\%$

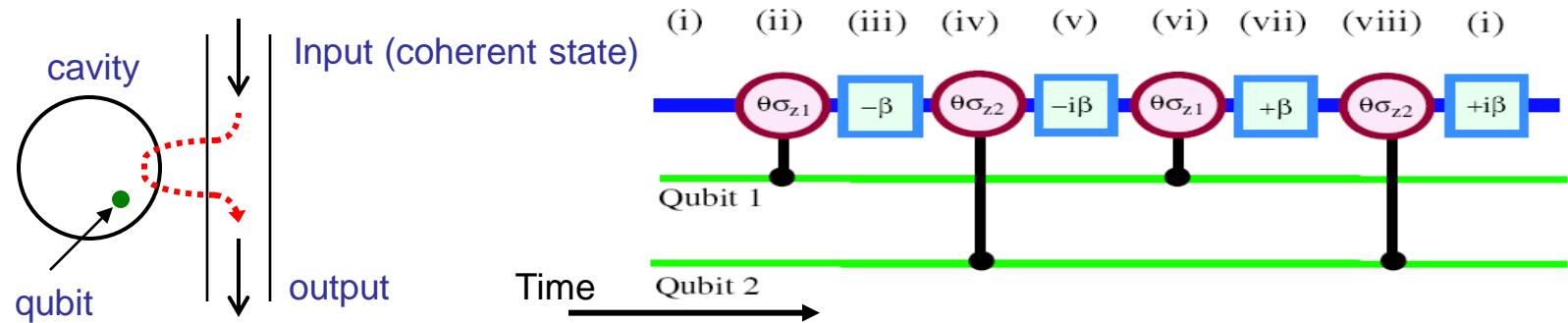
# Outline

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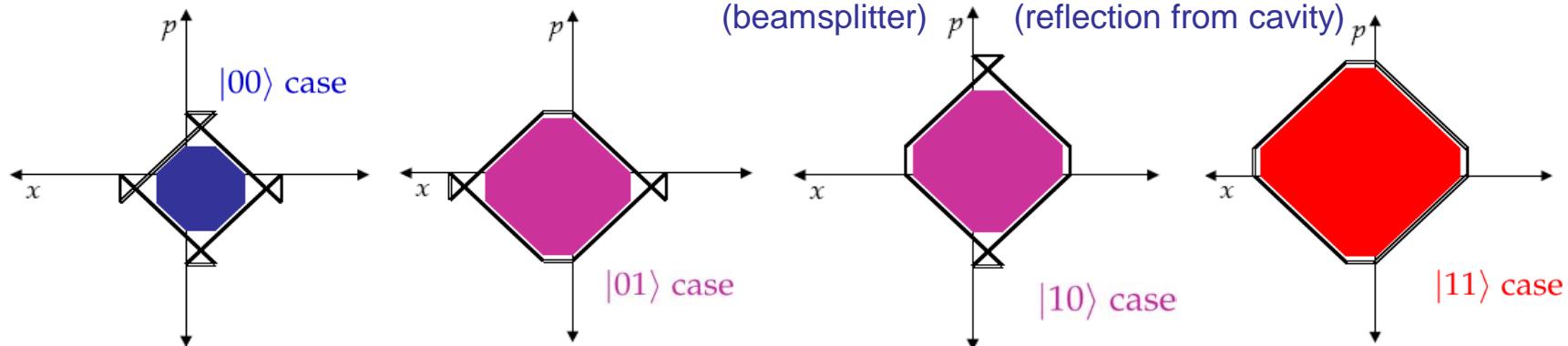
# Two Qubit Gate based on Topological Phase

T. Spiller et al., New J. Phys. 8, 30 (2006)



$$\hat{U} = D(i\beta)e^{-in\theta\hat{z}_2/2}D(\beta)e^{-in\theta\hat{z}_1/2}D(-i\beta)e^{-in\theta\hat{z}_2/2}D(-\beta)e^{-in\theta\hat{z}_1/2}$$

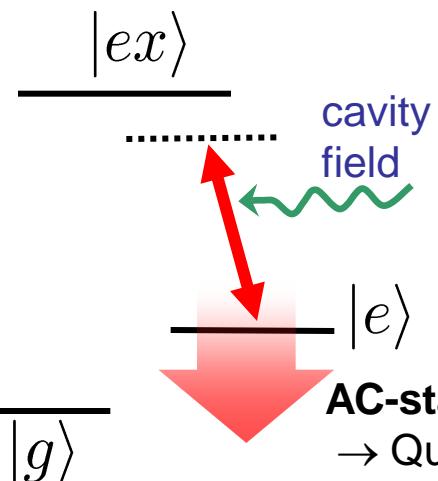
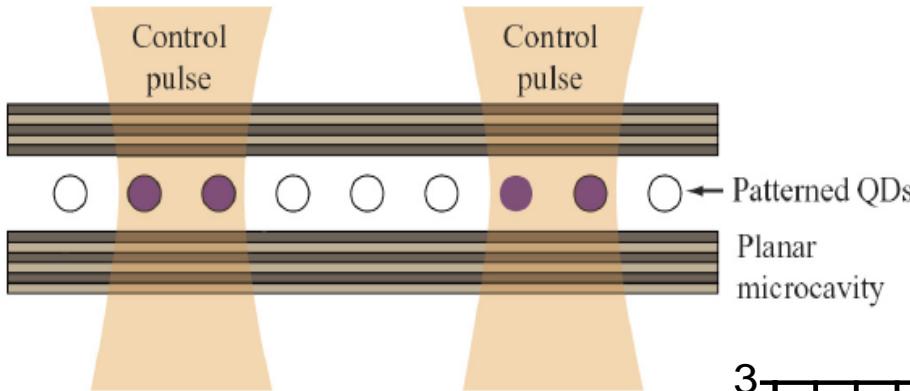
$$\beta = \sqrt{2}\alpha e^{-i\pi/4}$$



- After the entire sequence, the probe is disentangled from the two qubits.  
→ No measurement and post-selection required.
- An overall phase develops proportional to area (topological phase),  $\Phi \simeq 4\alpha^2\theta^2$ .  
→ A desired phase shift of  $\pi$  achieved with  $\alpha\theta \simeq 1$ .

# Two Qubit Gate in Dissipative Planar Microcavity

Y. Yamamoto et al., Phys. Scr. T137, 014010 (2009)



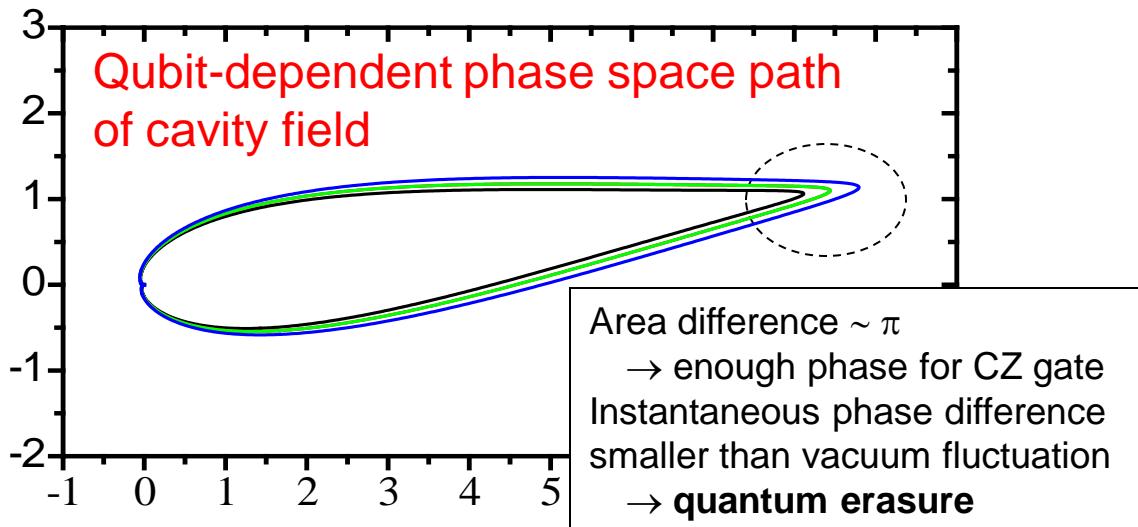
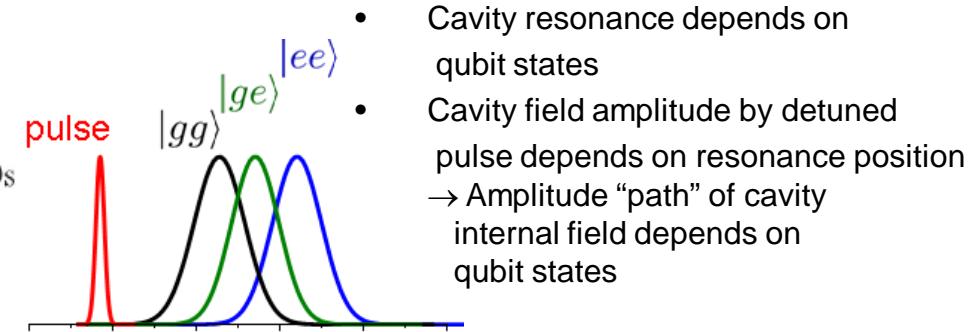
**AC-stark shift depends on cavity field amplitude**

→ Qubits therefore alter each other's phase

→ CZ gate for surface code creation

→ Master equation simulations indicate fidelity > 99% with  $Q=10^5$

$\tau \sim 10\text{nsec}$  (purely optical),  $\tau \sim 100\text{psec}$  (polaritonic)



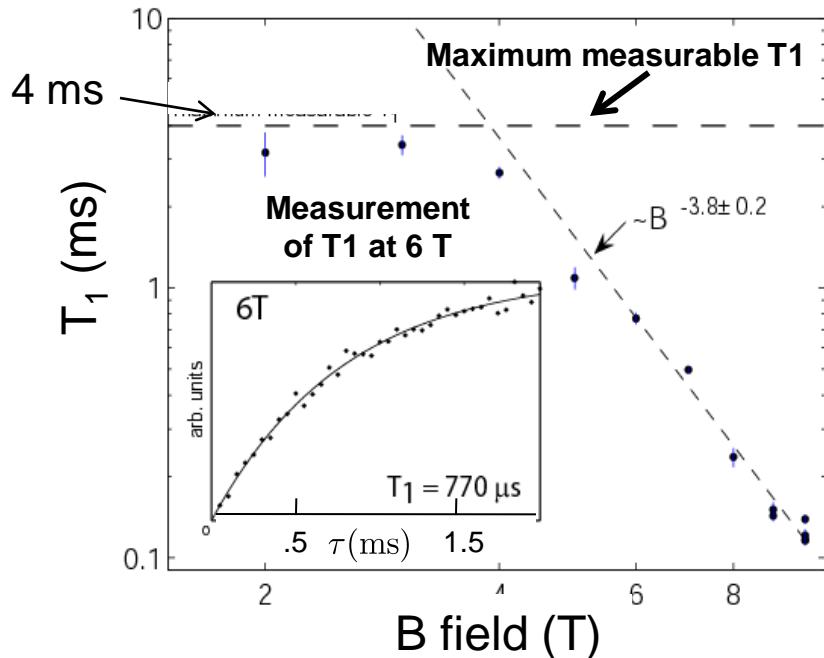
# Outline

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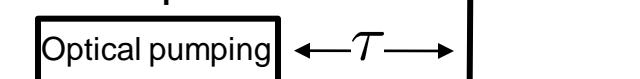
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# $T_1$ and $T_2$ Time of Si:GaAs Donor Electron Spins

$T_1 > 4\text{ msec}$  at  $B < 4\text{ T}$

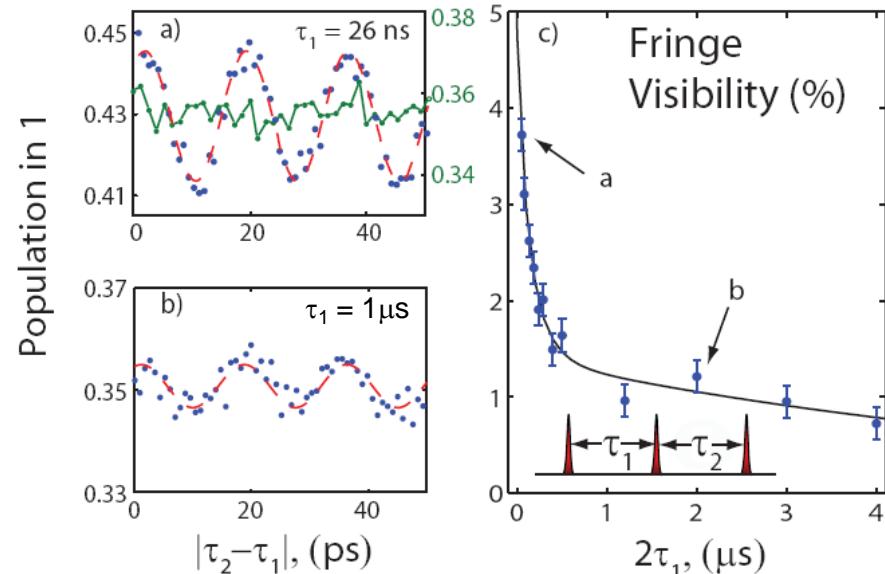


Pulse sequence:



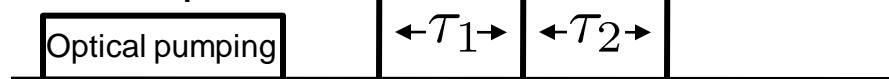
Fu, K.-M. C. et al. PRB 74, 121304 (2006).

$T_2 \sim 7\mu\text{sec}$  at  $B=10\text{ T}$  and  $T=1.5\text{ K}$   
(small angle spin echo)



Exponential decay  $T_2 \sim 7\mu\text{s}$   
(Free induction decay  $T_2^* \sim 1\text{-}2\text{ ns}$ )

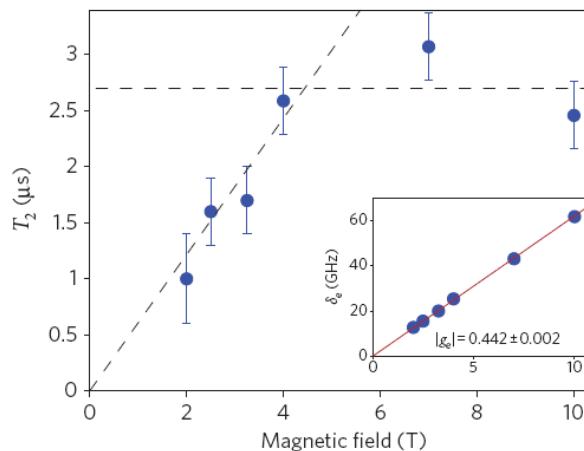
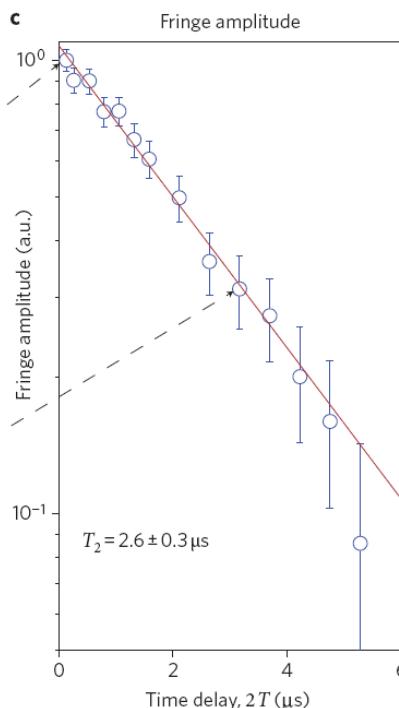
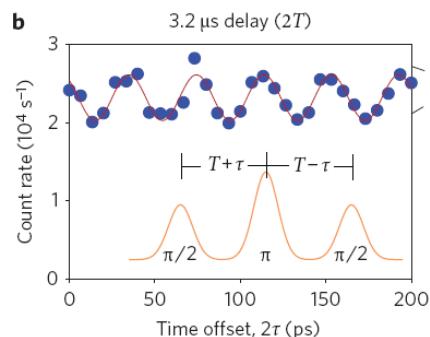
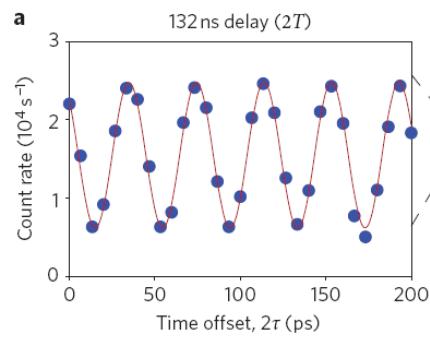
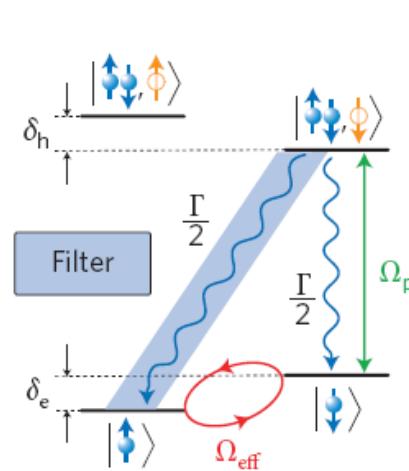
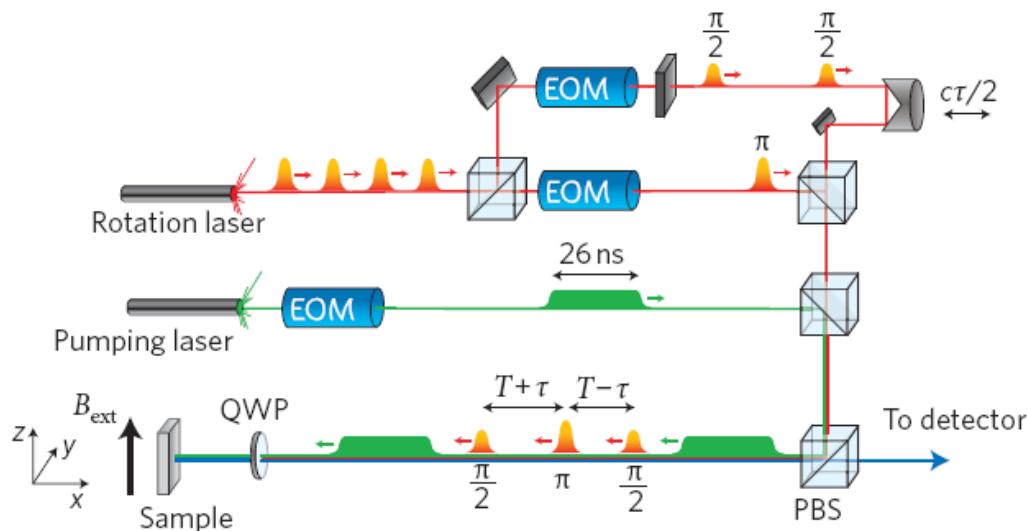
Pulse sequence:



S. Clark. et al. Phys. Rev. Lett. 102, 247601(2009)

# Optical Spin Echo Experiment with a Single Spin in a microcavity

D. Press et al., Nature Photonics 4, 367 (2010)



Shorter  $T_2$  observed at  $B < 4\text{T}$

# $T_2 = 25$ sec of $^{29}\text{Si}$ Nuclear Spins in Natural Crystal Silicon

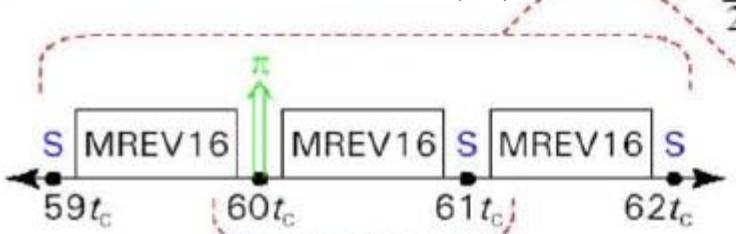
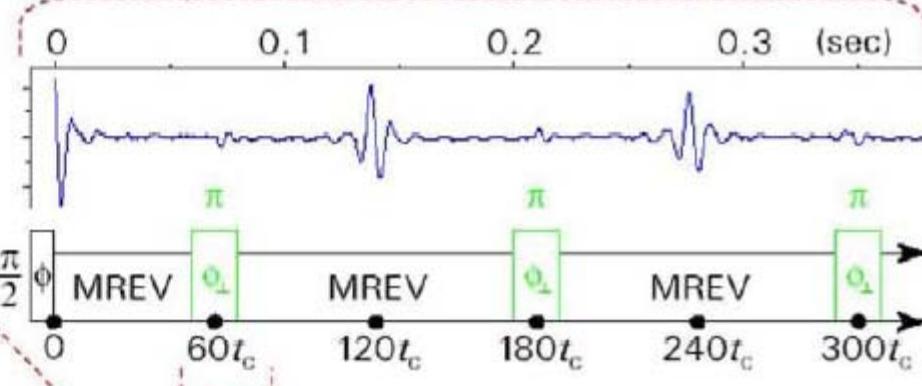
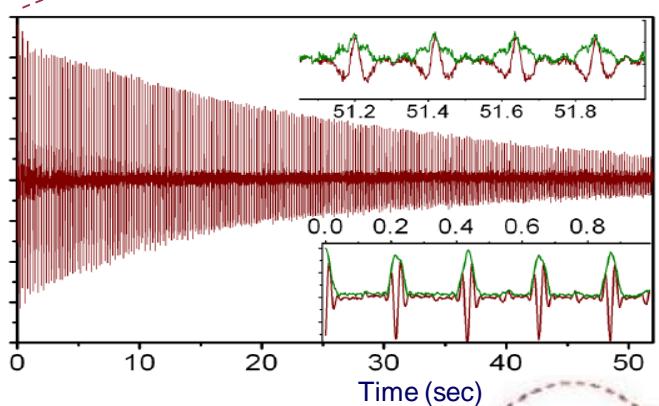
T. I add et al., Phys. Rev. B 71, 014401 (2005)

$$\frac{1}{T_2} = \frac{1}{2T_1} + \frac{\gamma^2}{2} \int_{-\infty}^{\infty} \langle \Delta H_z(t) \Delta H_z(0) \rangle dt + \left[ \left\langle \left[ \hat{\mathcal{H}}_D, \left[ \hat{\mathcal{H}}_D, \hat{I}_x \right] \right] \right\rangle / \langle \hat{I}_x \rangle \right]^{1/2}$$

natural linewidth  
 $(\sim 10^{-4}\text{Hz})$

fluctuating local magnetic field along Z-axis at  $\omega \simeq 0$

dipolar coupling among Iso-nuclear spins



$$t_c = 24\tau$$

# Outline

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# Generation of Indistinguishable Single Photons from a Single QD in a Post-Microcavity

C. Santori et al., Nature 419, 594 (2002)

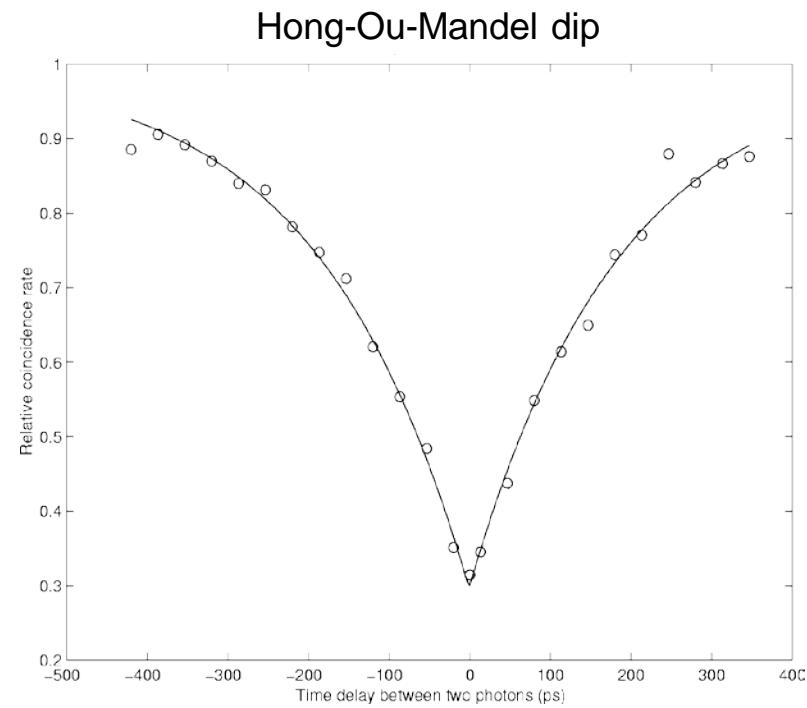
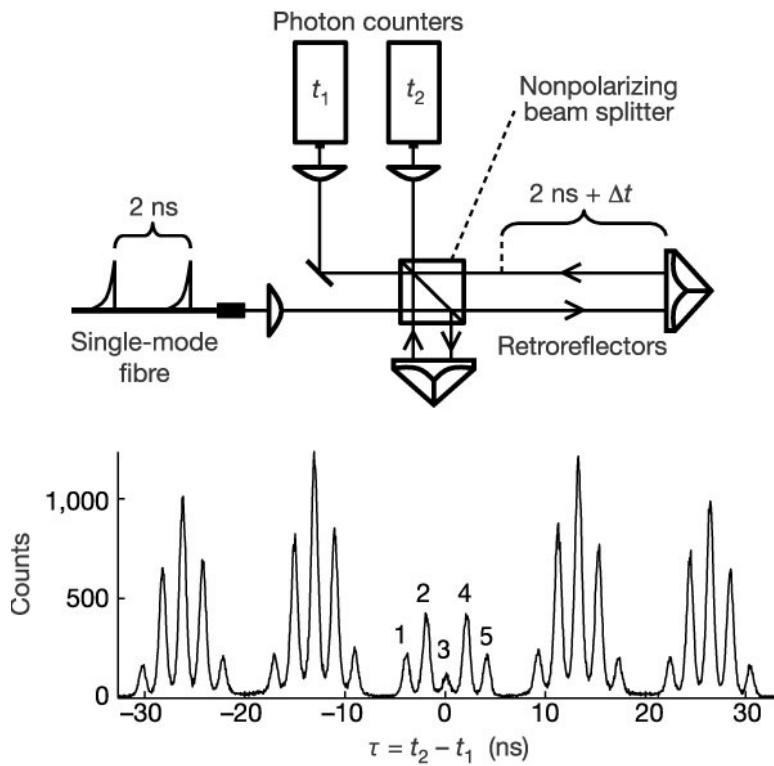


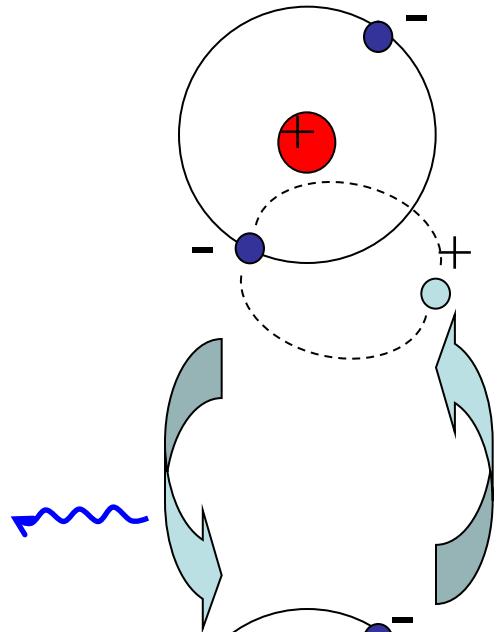
Table 1 Summary of quantum-dot parameters

	$g^{(2)}$	$g$	$\tau_s$ (ps)	$\tau_c$ (ps)	$\tau_m$ (ps)	$V(0)$
Dot 1	0.053	0.039	89	48	80	0.72
Dot 2	0.067	0.027	166	223	187	0.81
Dot 3	0.071	0.025	351	105	378	0.74

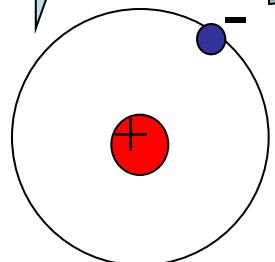
# Quantum Memory: Clean Atomic Systems in Semiconductors

## – Donor Nuclear Spin, Bound Electron Spin ( $D^0$ ) and Bound Exciton ( $D^0X$ ) System –

neutral donor bound exciton



Radiative excitation  
and recombination  
(Interface to qubus)



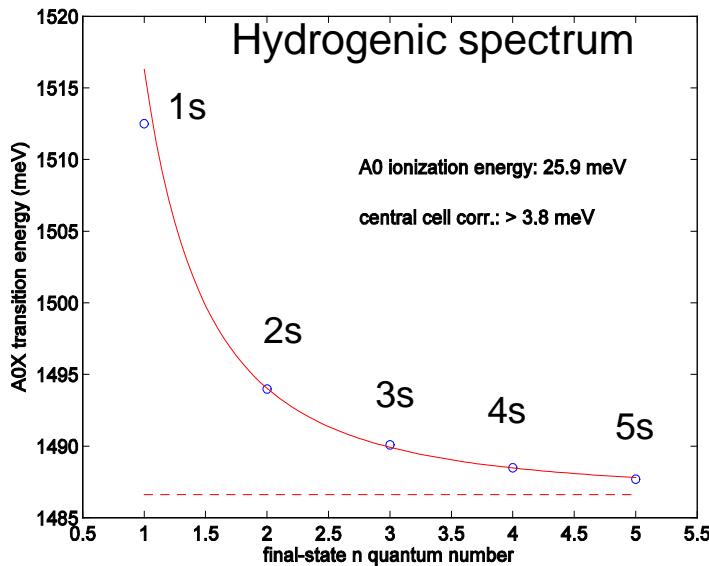
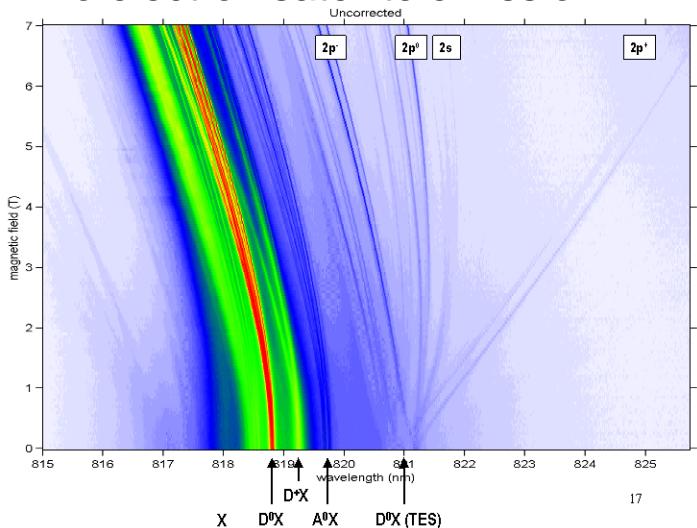
neutral donor

simplest  
nuclear spin  $-1/2$   
(quantum memory)

$^{31}\text{P}$ : Si      electron spin with  
 $^{19}\text{F}$ : ZnSe      homogeneous g-factor  
NV center (quantum processor)

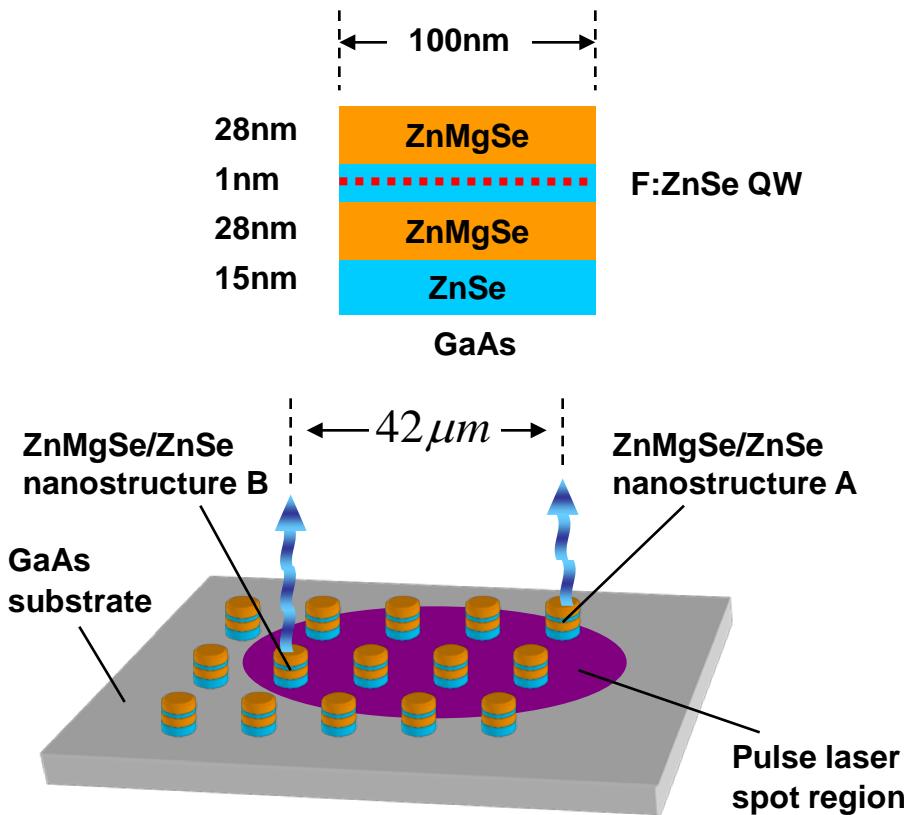
Background nuclear spins  
can be depleted for Si and ZnSe by  
isotope engineering

Diamagnetic shift, Zeeman splitting,  
Two electron satellite emission

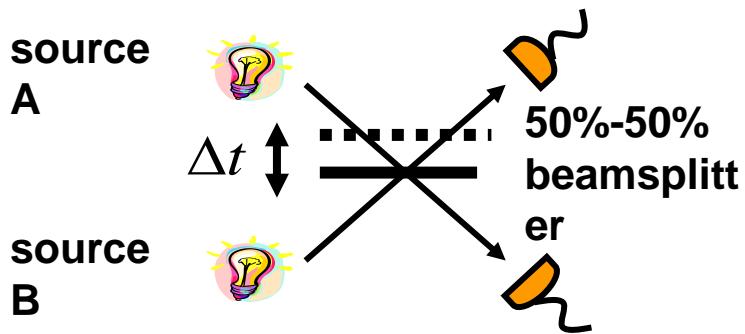
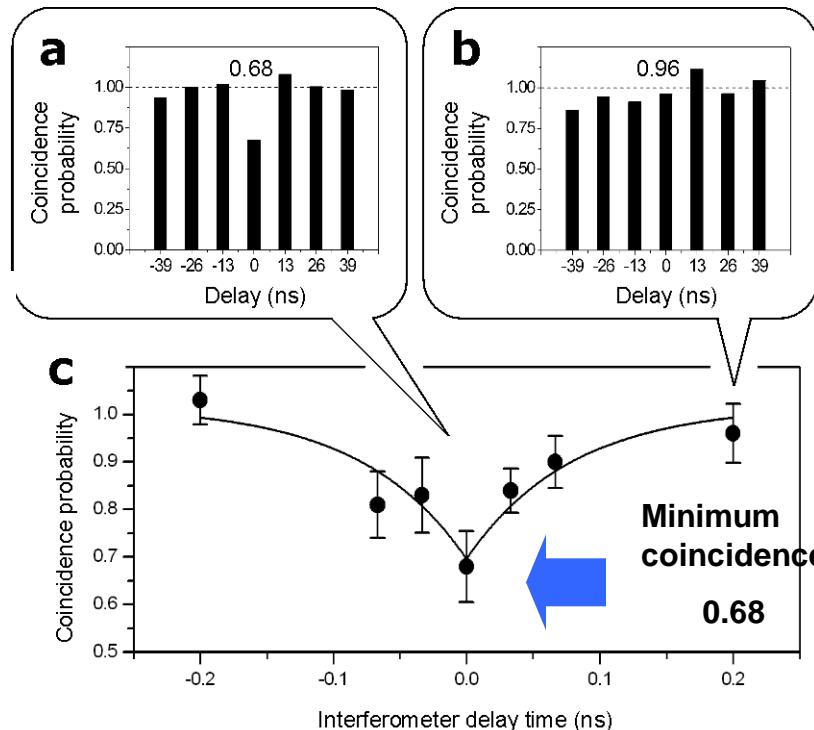


# Indistinguishable Single Photons from Two $^{19}\text{F}:\text{ZnSe}$ Donors

K. Sanaka et al., Phys. Rev. Lett. 103, 053601 (2009)



Coincidence count rates as a function of delay time (Hong-Ou-Mandel dip)



Visibility

$$V = \frac{P_c(0.2\text{ns}) - P_c(0)}{P_c(0.2\text{ns})} = 31[\%]$$

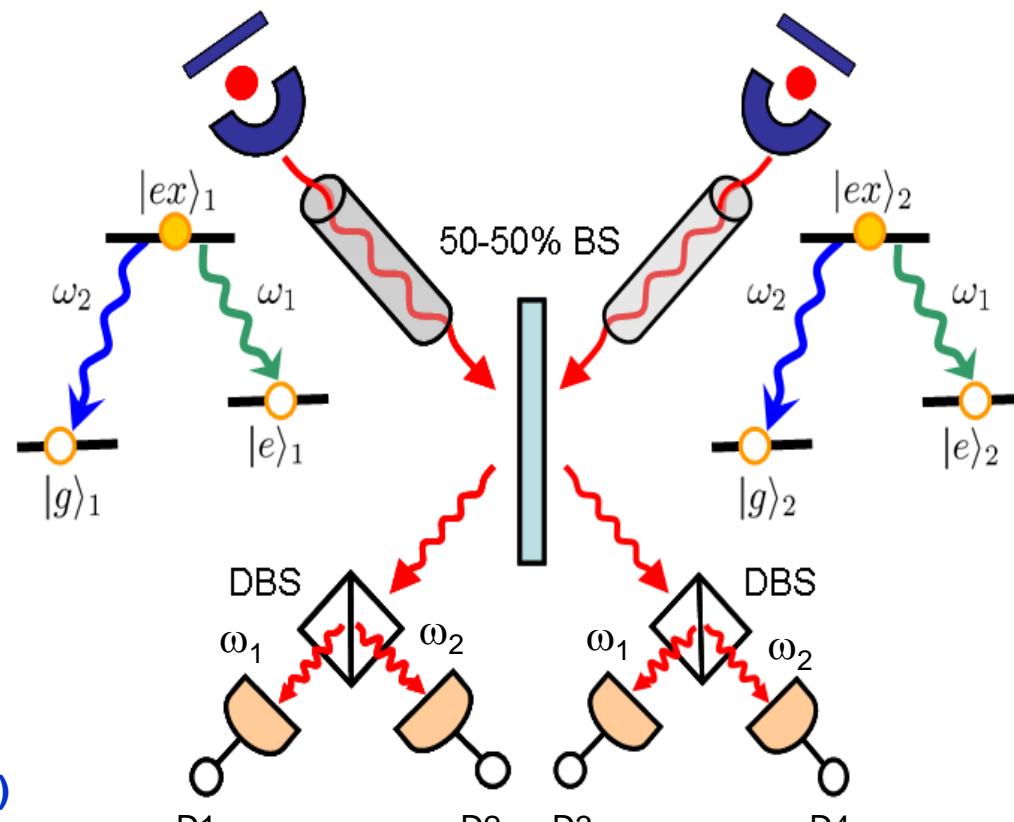
Indistinguishability

$$I = 65 \pm 13 [\%]$$

Coherence time

$$\tau_c = 74 \pm 38 [\text{ps}]$$

# Entanglement Distribution based on Indistinguishable Single Photon Generation and Coincidence Detection



Theory:

C. Simon et al.,  
Phys. Rev. Lett. 91, 110405 (2003)

$$\text{click at D1/D2 or D3/D4} \xrightarrow{\hspace{2cm}} \frac{1}{\sqrt{2}} (|e\rangle_1|g\rangle_2 + |g\rangle_1|e\rangle_2)$$

$$\text{click at D1/D4 or D2/D3} \xrightarrow{\hspace{2cm}} \frac{1}{\sqrt{2}} (|e\rangle_1|g\rangle_2 - |g\rangle_1|e\rangle_2)$$

Experiment with trapped ions:

D.L. Moehring et al., Nature 449, 68 (2007)  
S. Olmschenk et al., Science 323, 486 (2009)

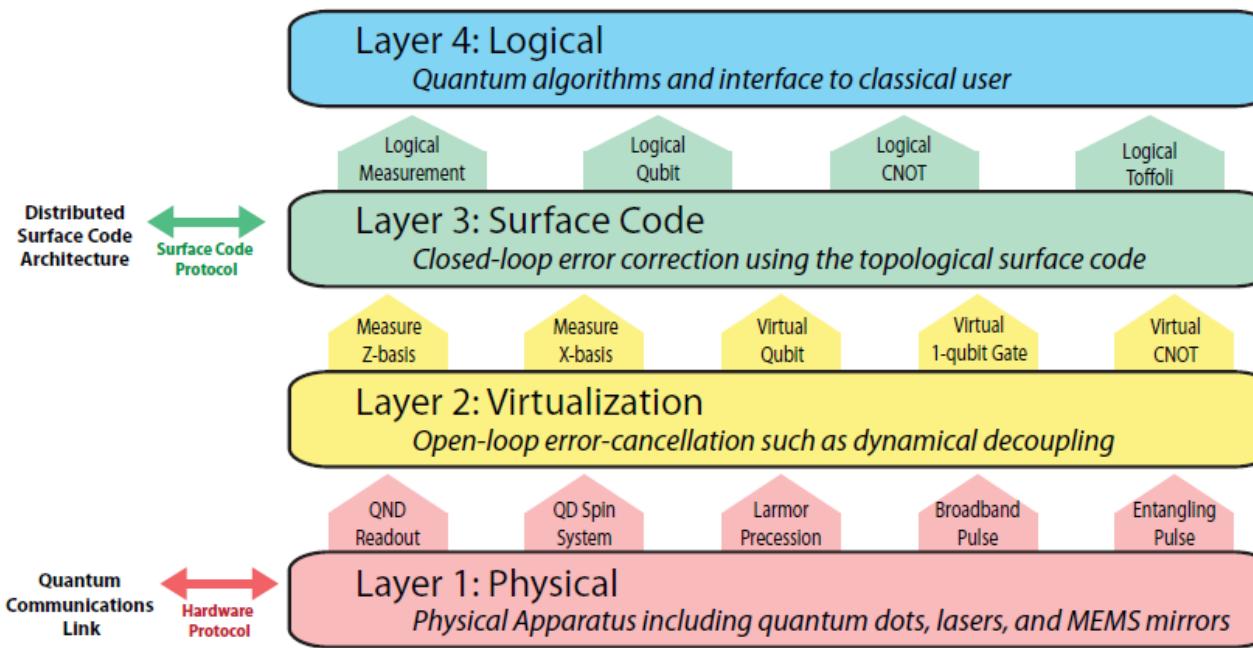
# Outline

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- Physical qubits – Quantum dot spin lattice in planar microcavity –
- Motivation – Fault tolerant quantum information processing –
- Qubit initialization and projective measurement
- Single qubit gate
- Two qubit gate
- Decoherence time
- Indistinguishable single photons and entanglement distribution
- Topological surface code architecture

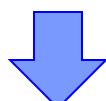
# Layered Architecture for Fault-Tolerant Quantum Computation

## – How to Construct a Perfect Quantum Computer out of Imperfect Quantum Devices –



**QuDOS**  
(Quantum Dots with  
Optically controlled Spins)

- Each layer has a prescribed set of duties to accomplish.
- A lower layer provides the services to the one above it.
- An above layer issues commands to the layer below and processes the results.



**Isolation of design problems in individual layers  
and independent evolution of layers.**

# **Layer 1 : Physical**

**Mission:** Storage and manipulation of unprotected quantum information  
Provides the essential physical resources to satisfy the virtualization layer

## **Tools:**

- Storage – Electron spin state in 2D square array of charged quantum dots in a planar microcavity
- Qubit – Zeeman sub-levels in a transverse magnetic field (Voigt geometry)
- Initialization/Measurement – Single shot QND readout of the spin state ( → Detector array with integrated CMOS processors)
- Single qubit gate – Ultra-fast optical pulse rotates the spin vector
- Two qubit gate – Cavity photon or polariton mediates the nearest neighbor spin-spin coupling ( → Entangling operation)

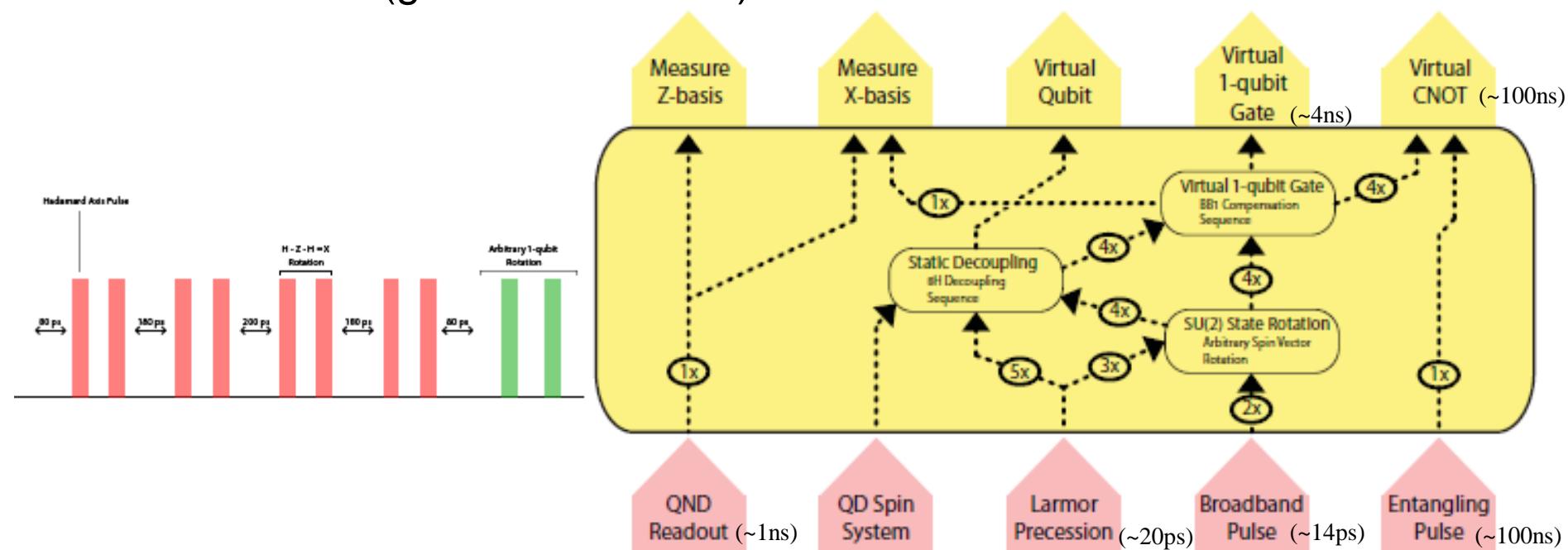
## **Enemies:**

- Decoherence
- Dynamic coherent (systematic) and incoherent (random) errors (gate errors)

## Layer 2 : Virtualization

### Mission: Storage and manipulation of protected quantum information

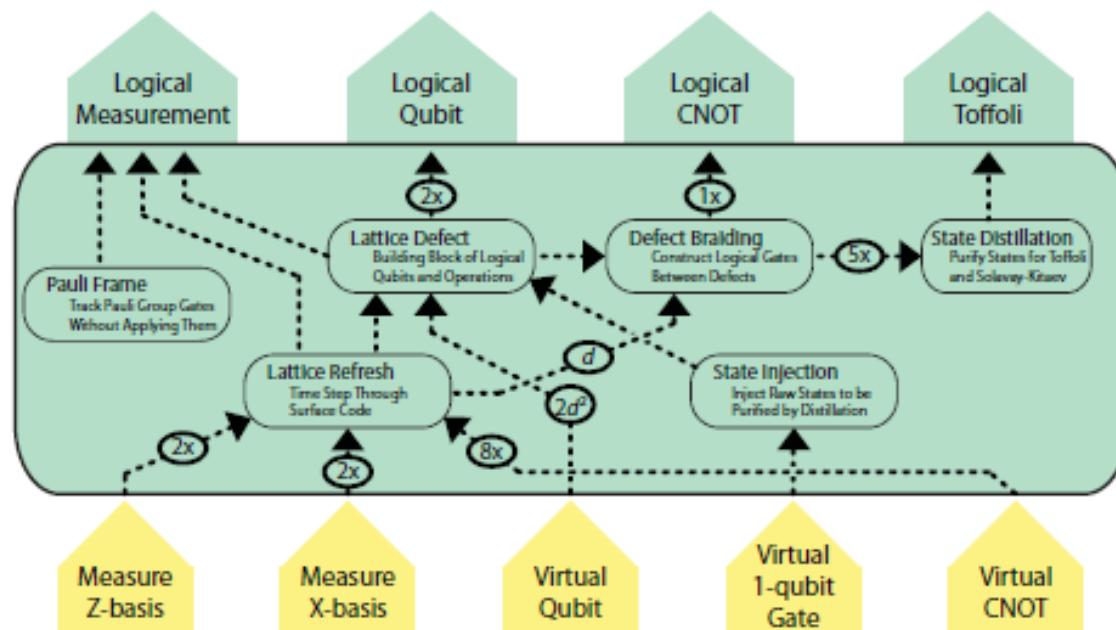
- Open-loop systematic error cancellation – Refocusing and dynamical decoupling
- Virtual qubit above layer 2 appears to be a static qubit
- Virtual gate – Composite pulse sequences realize virtual qubit states with reduced error from layer 1 processes to satisfy the threshold of the surface code (gate error < 0.7%)



# Layer 3 : Surface Code

**Mission: Correct arbitrary errors with quantum error correction**  
[R. Raussendorf, J. Harrington and K. Goyal, NJP 9 (2007)]

- Logical qubit = Defect in the surface code
- Closed loop error correction – Periodically measure an error syndrome and use Pauli frame (X, Y, Z or I) instead of error correction
  - interpretation of final result
- Error threshold for fault-tolerance – 0.75% for virtual qubits and gates
  - Error → determine code size



- Injection of single qubit states
- 2D array of qubits with NN coupling (CNOT)
- Measurement in X and Z bases

# Size and Operation Time of Surface Code

## Shor's factoring algorithm for 2048-bit integer

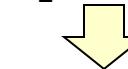
Parameter	Symbol	Value
Threshold error per virtual gate	$\epsilon_{thresh}$	$7.5 \times 10^{-3}$
Error per virtual gate	$\epsilon_V$	$1 \times 10^{-3}$
Number of logical gates	$K$	$9 \times 10^{12}$
Number of logical qubits	$Q$	12288
Error per logical gate	$\epsilon_L$	$9 \times 10^{-20}$
Surface code distance	$d$	53
Virtual qubits per logical qubit		19600

# of logical qubits  $Q \sim 6N$   
 Success probability of quantum algorithm

~99.99%



$\epsilon_L \leq 10^{-4}/KQ$



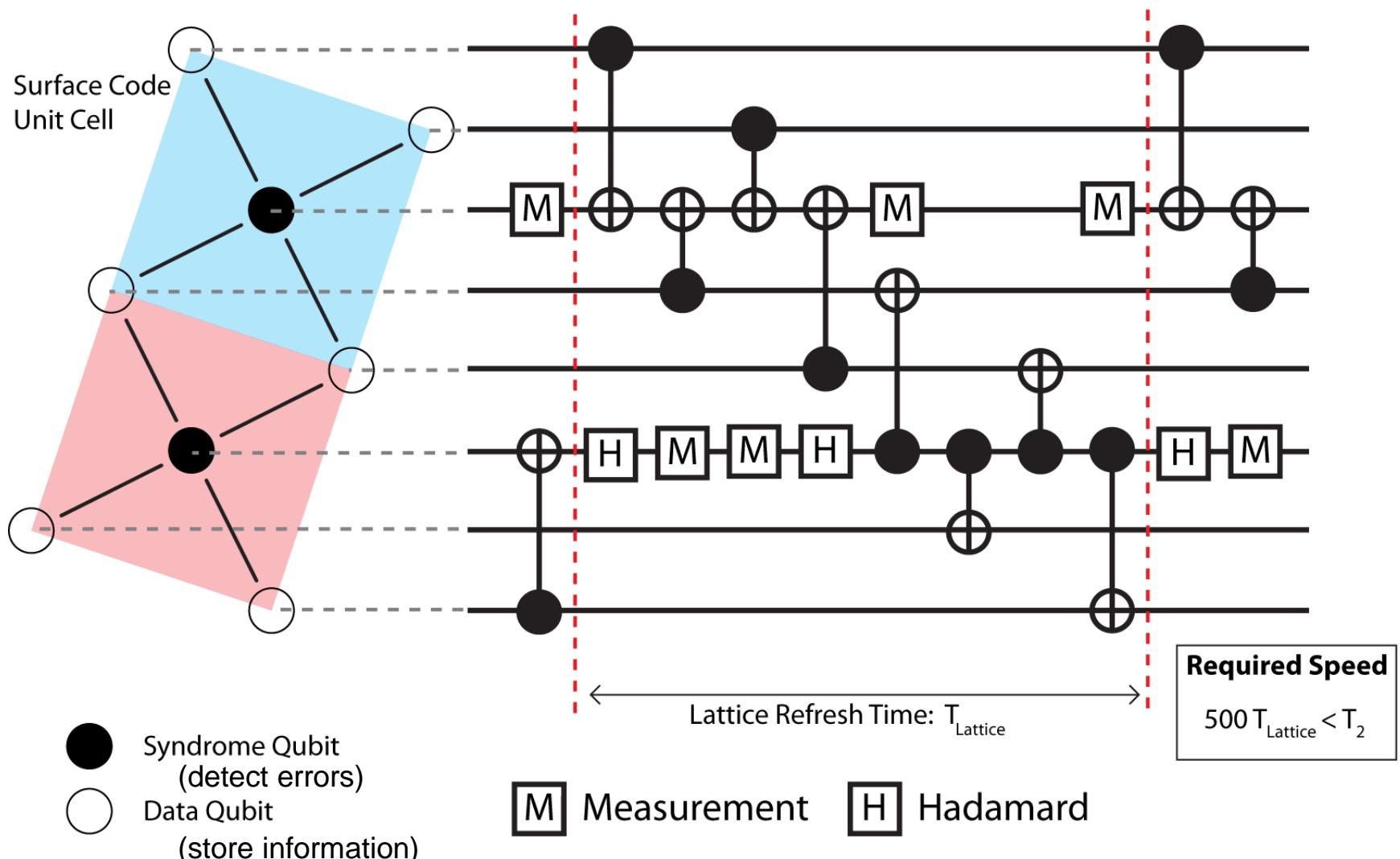
code distance 53  
 total number of physical qubits

$2 \times 10^8$  (minimum)

~  $10^9$  (sufficient)

Operation	Label	Composition	Max Duration
Lattice Refresh with Alternating Phase Masks	LatticeRefresh	$2 \times (IZ \cdot 4 \times CNOT \cdot MZ \cdot IX \cdot 4 \times CNOT \cdot MX)$	$1.61 \mu s$
Defect Braiding	DefectBraid	$30 \times \text{LatticeRefresh}$	$48.4 \mu s$
Logical CNOT	LogicalCNOT	$3 \times \text{DefectBraid}$	$145 \mu s$
State Distillation	StateDistill	$5 \times \text{DefectBraid}$	$242 \mu s$
Logical Toffoli Gate	LogicalToffoli	$14 \times \text{DefectBraid}$	$678 \mu s$

# Virtual Gates in a Surface Code Refresh Step

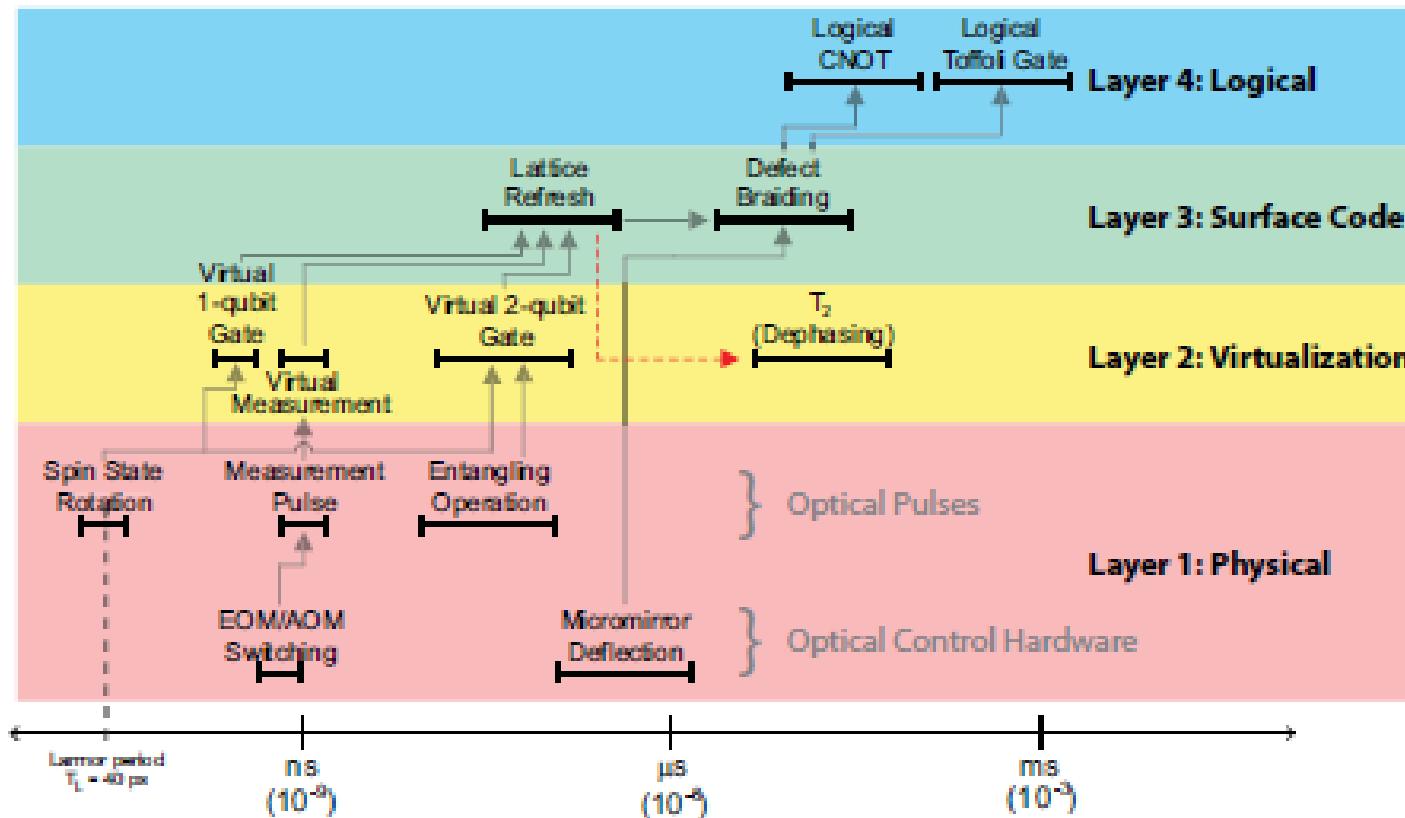


A lattice refresh cycle of the surface code can be performed in parallel across the entire 2D array of virtual qubits.

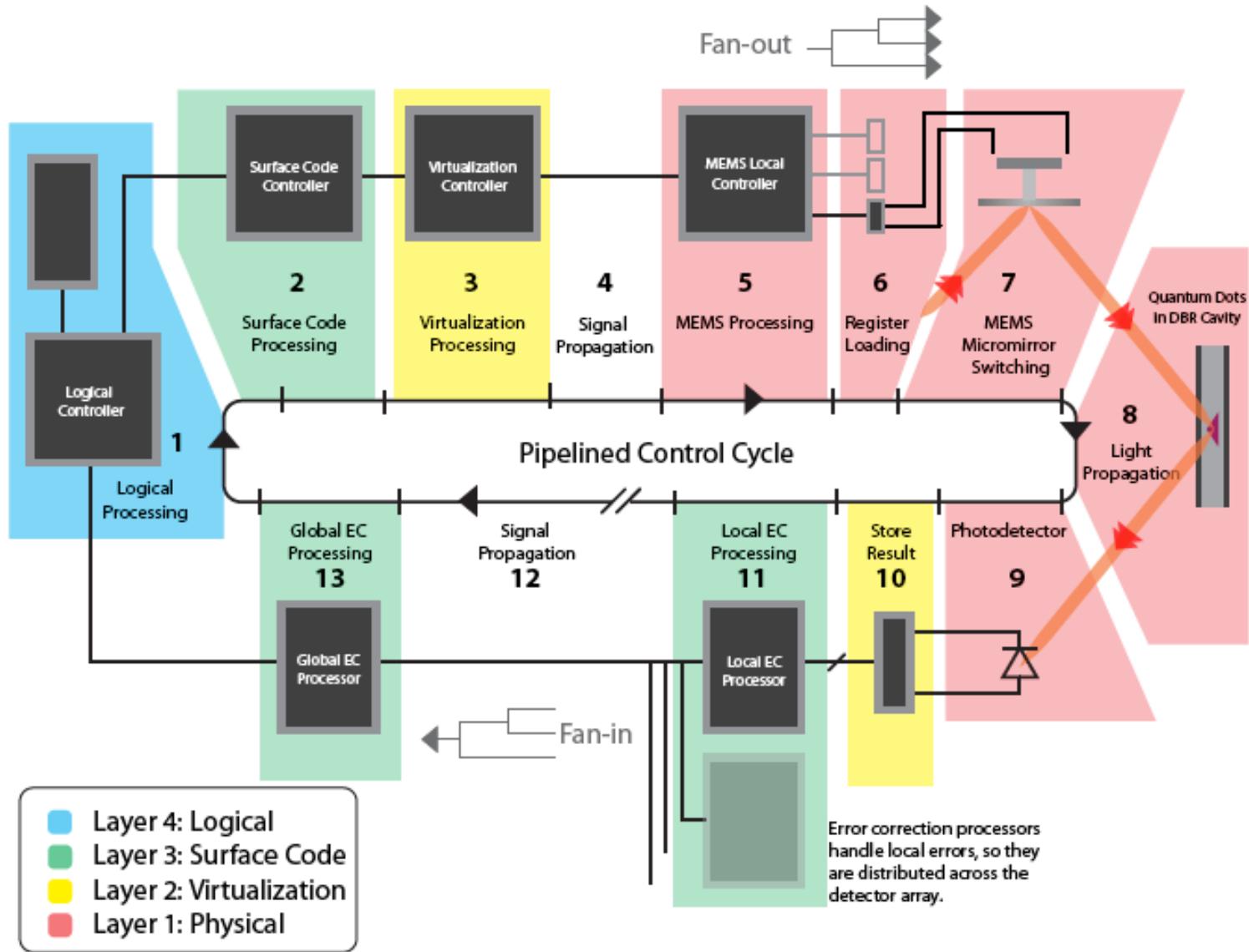
# Layer 4 : Logical

**Mission:** Execute the quantum algorithm on the logical qubits provided by the surface code and output the end result in a classical form

- 2048-bit number factoring – 14 days in contrast to  $\gtrsim 1000$  years in classical computers



# Primary Control Loop of the Surface Code Quantum Computer



# Resource requirement for Shor's factoring machine

— n= 2,048-bit number —

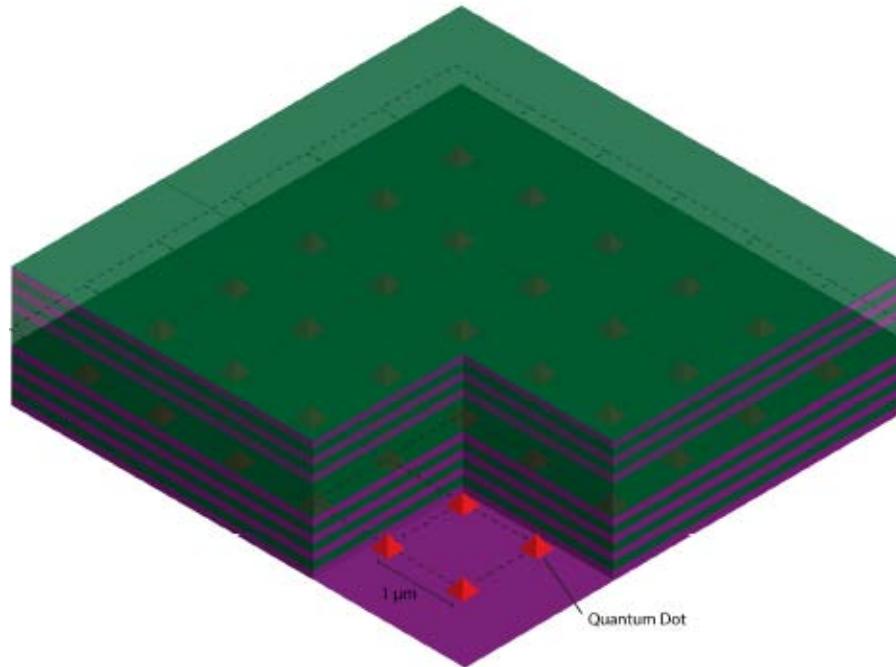
40ps one-bit/1ns two-bit gates, 99.9% fidelity, 3us coherence time

60n~120,000 logical qubits

code distance d=30  $\rightarrow$   $\sim 10^8$  physical qubits

computational time: 100-1000 years by classical methods

$\rightarrow$   $\sim 5$  hours by this quantum computer



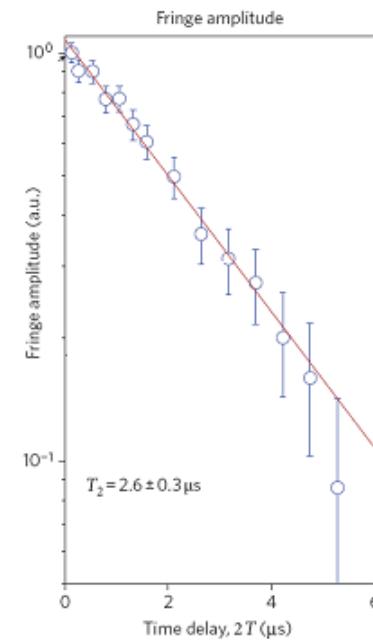
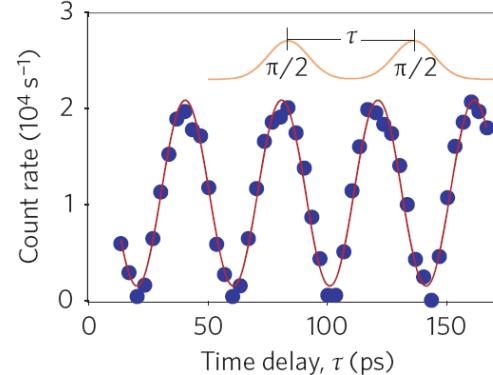
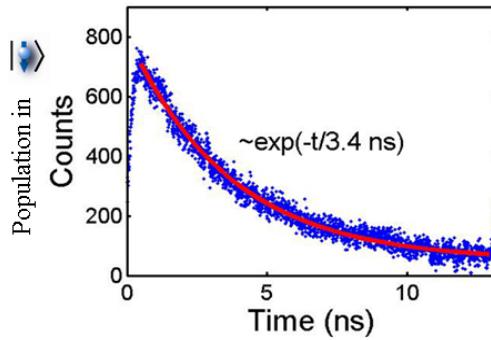
This number of QDs can be implemented in 2D square lattice with  $\sim 1\mu\text{m}$  QD spacing on  $1\text{cm}^2$  chip.

# Summary and Outlook

## Essential elements for semiconductor spin-based quantum information processing

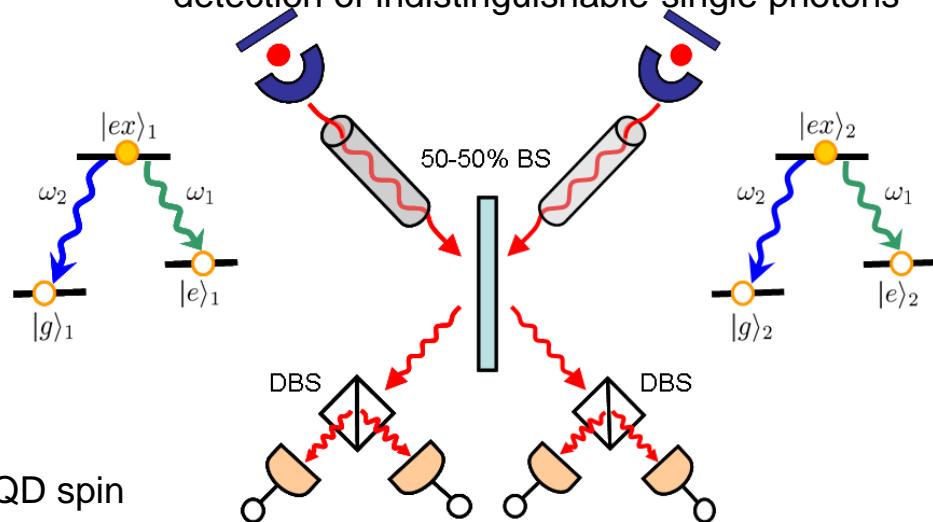
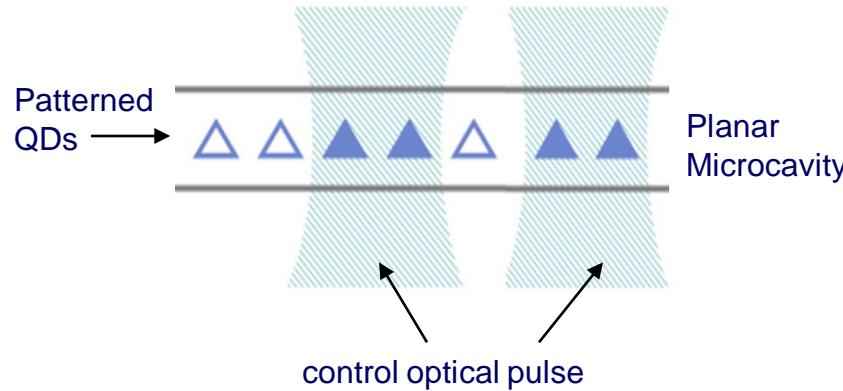


- ✓ Initialization in  $\sim 3\text{nsec}$  with  $F=92\%$
- ✓ Single qubit gate in  $\lesssim 20\text{ psec}$  with  $F=98-99\%$
- ✓ Decoherence time  $T_2 \sim 3\mu\text{sec}$



- Two qubit gate by single optical pulses

- Entanglement distribution by coincidence detection of indistinguishable single photons



- Single shot QND measurement of a single QD spin