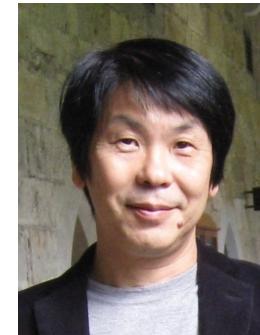




人工知能はいかにして世界から  
知識を獲得し表現・利用しているか

機械学習と知識表現・記号推論の融合による  
**Neuro-Symbolic AI**の実現

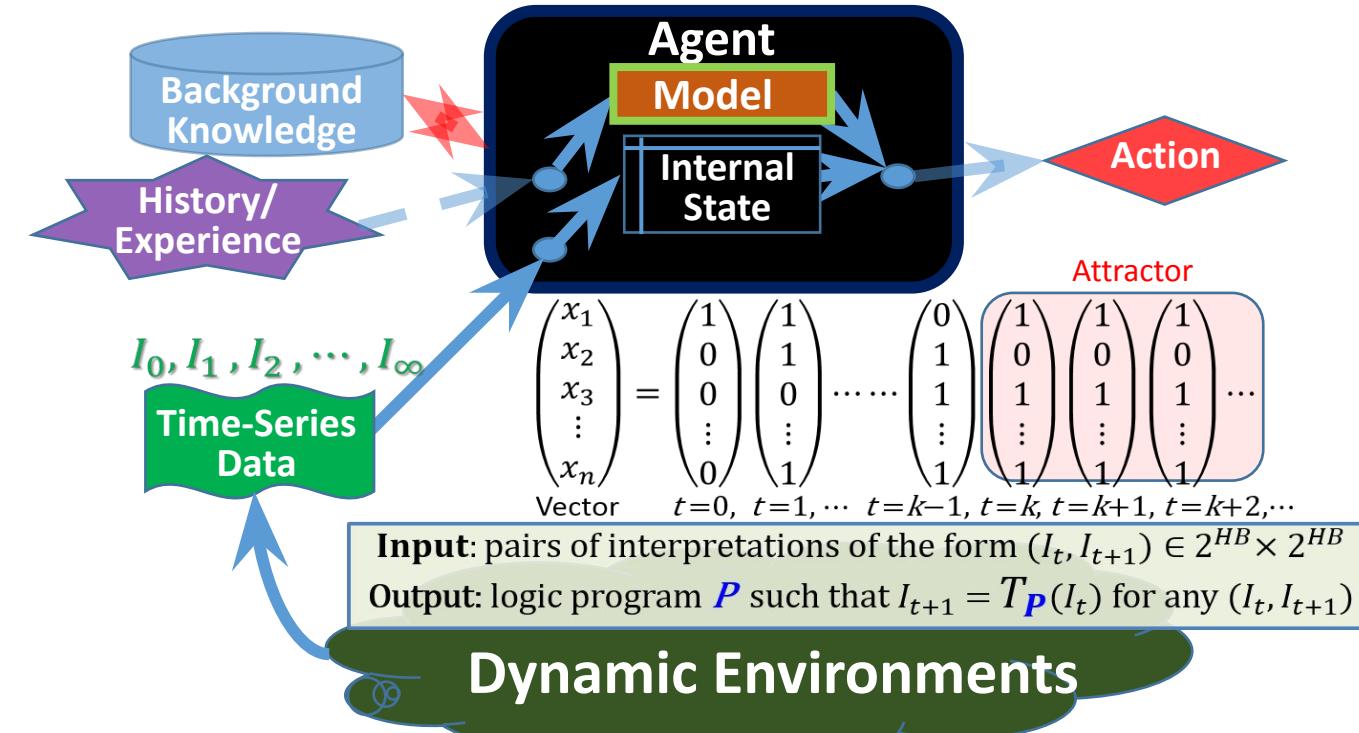


# LFIT: 解釈遷移からの学習

## Learning from Interpretation Transition



Katsumi Inoue  
(Professor)



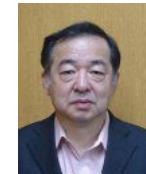
### Applications:

- biology (identification of gene regulatory networks)
- DREAM challenges
- physics (cellular automata)
- robots' actions in uncertain environments
- learning agents' logics
- strategies in games
- etc.

### Extensions:

- delays: Markov( $k$ ) system
- multi-valued variables
- asynchronous update
- nondeterministic / probabilistic transitions
- continuous domains
- neural semantics
- noise tolerance

# Bridging NN learning and logical inference



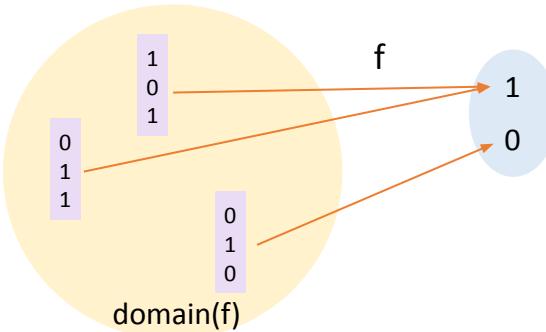
Taisuke Sato  (Professor by Special Appointment)  
[Google Scholar](#) 

$$\mathbf{I}_{in} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 1 & 1 & 0 \end{pmatrix} \begin{matrix} a_1 \\ a_2 \\ a_3 \end{matrix}$$

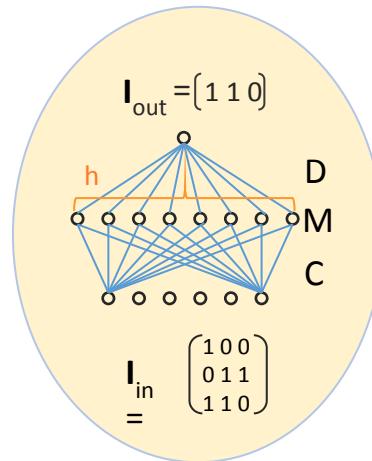
  
 $I_{in}$   
  
 $I_{in}$

$$f(\mathbf{I}_{in}) = \mathbf{I}_{out} = \begin{bmatrix} 1 & 1 & 0 \end{bmatrix}$$

Learning  $\varphi$



feed-forward NN



$\phi(\mathbf{I}_{in}) = \mathbf{I}_{out}$   
 $\varphi = \text{matrix pair } (C, D)$   
 $= \text{DNF learned from } (\mathbf{I}_{in}, \mathbf{I}_{out})$

$$\mathbf{I}_{out} = (D(1 - \min_1(C[\mathbf{1} - \mathbf{I}_{in}; \mathbf{I}_{in}]))) \geq 1$$

Proposition:

$\varphi$  is an **interpolant** between  $\text{dnf}(\mathbf{I}_{in}^P)$  and  $\sim \text{dnf}(\mathbf{I}_{in}^N)$ , i.e.  
 $\vdash \text{dnf}(\mathbf{I}_{in}^P) \rightarrow \varphi, \varphi \rightarrow \sim \text{dnf}(\mathbf{I}_{in}^N)$

$$\text{dnf}(\mathbf{I}_{in}^P) = (a_1 \wedge \sim a_2 \wedge a_3) \vee (\sim a_1 \wedge a_2 \wedge a_3)$$

$$\text{dnf}(\mathbf{I}_{in}^N) = (\sim a_1 \wedge a_2 \wedge \sim a_3)$$

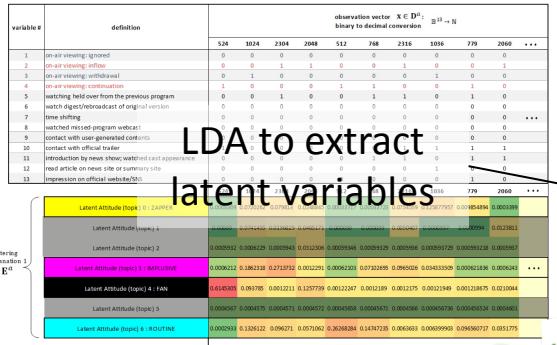


# Explainable Model Fusion for Customer Journey Mapping

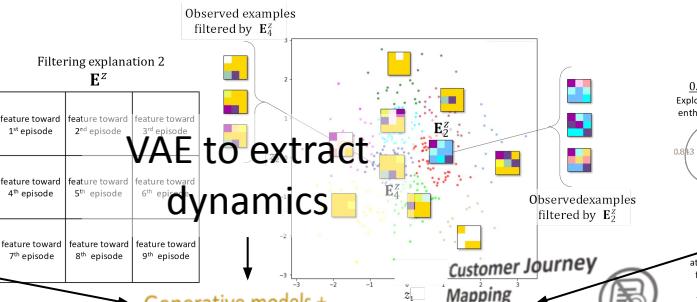


# Kotaro Okazaki

(Doctoral Student)



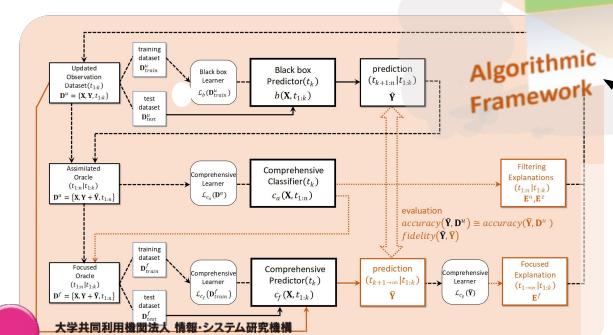
LDA to extract latent variables



# VAE to extract dynamics

# ► Generative models + Inductive Logic Programming

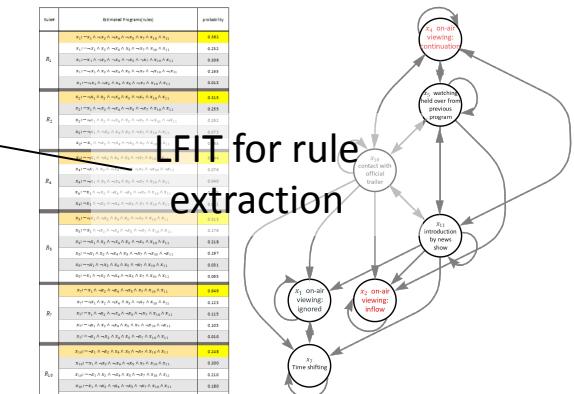
# XAI framework to post-hoc explainability



大学共同利用機関法人 情報・システム研究機構

# 国立情報学研究所

National Institute of Informatics



Ko Okazaki and Katsumi Inoue

"Explainable Model Fusion for Customer Journey Mapping."

Frontiers in Artificial Intelligence: 72.

# Differentiable Logical Inference



Akihiro Takemura  
(Doctoral student)



1. Translate program  $P$  into a Program Matrix

$$D^P$$

$P$      $p :- \text{not } q.$   
            $q :- \text{not } p.$

Program

$$D^P \quad \begin{matrix} p & p & q & \bar{p} & \bar{q} \\ p & (0 & 0 & 0 & 1) \\ q & 0 & 0 & 1 & 0 \end{matrix}$$

Program Matrix

$$x \quad \begin{matrix} p \\ q \end{matrix} \quad \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

Interpretation vector

2. Define Loss function w.r.t. continuous interpretation

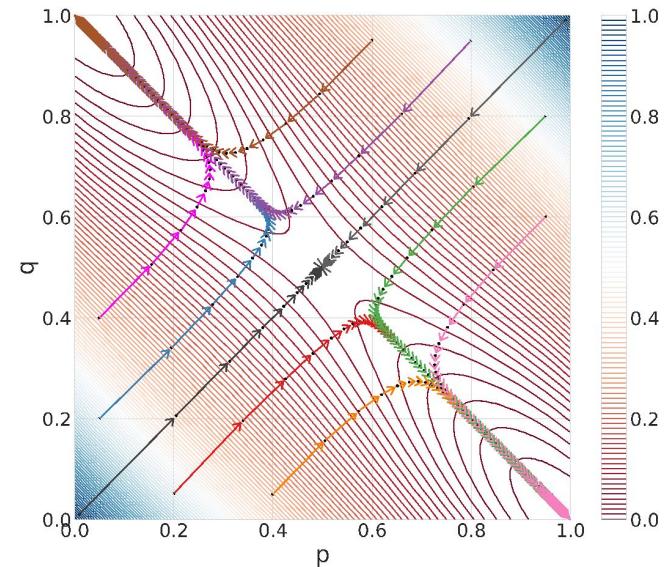
$$L(x)$$

Loss function w.r.t.  $x$

$$\frac{\partial L(x)}{\partial x}$$

Gradient of  $L(x)$  w.r.t.  $x$

3. Minimize the loss with gradient descent



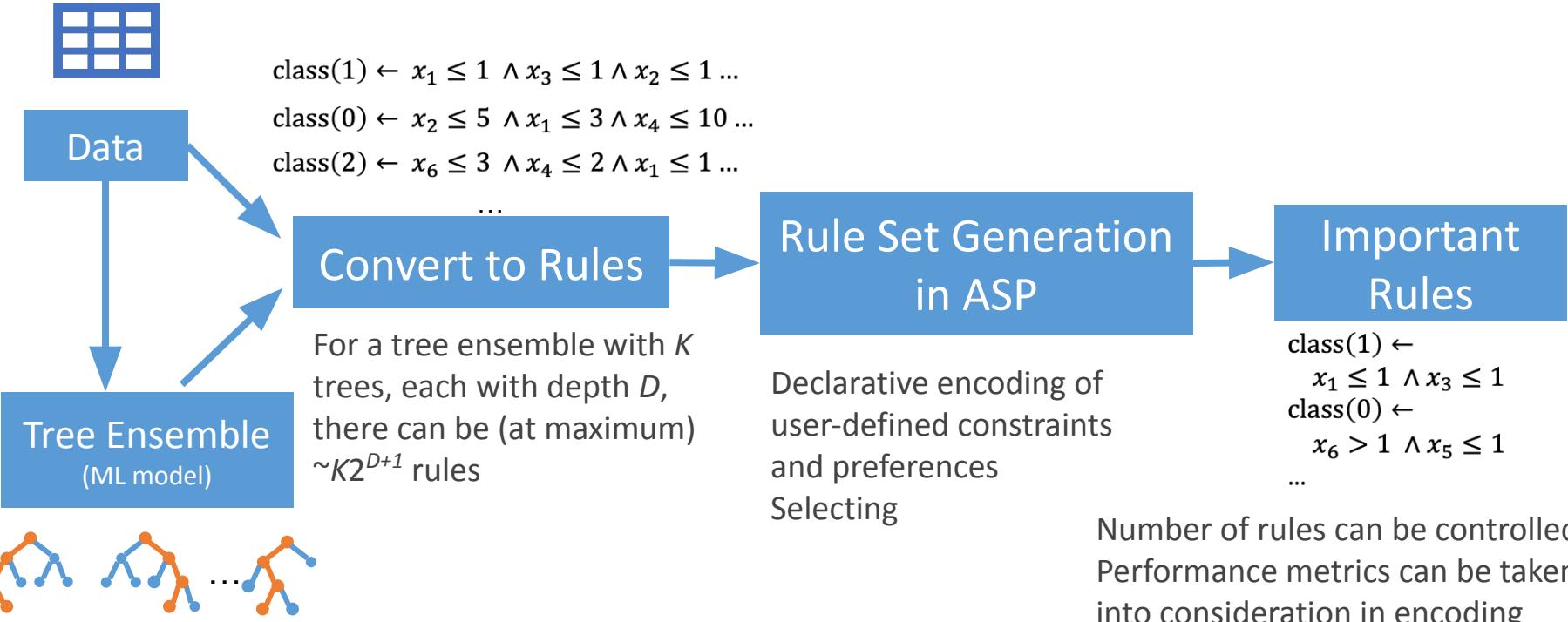
# Explaining Tree Ensemble models with Answer Set Programming



Akihiro Takemura  
(Doctoral student)



Google Scholar

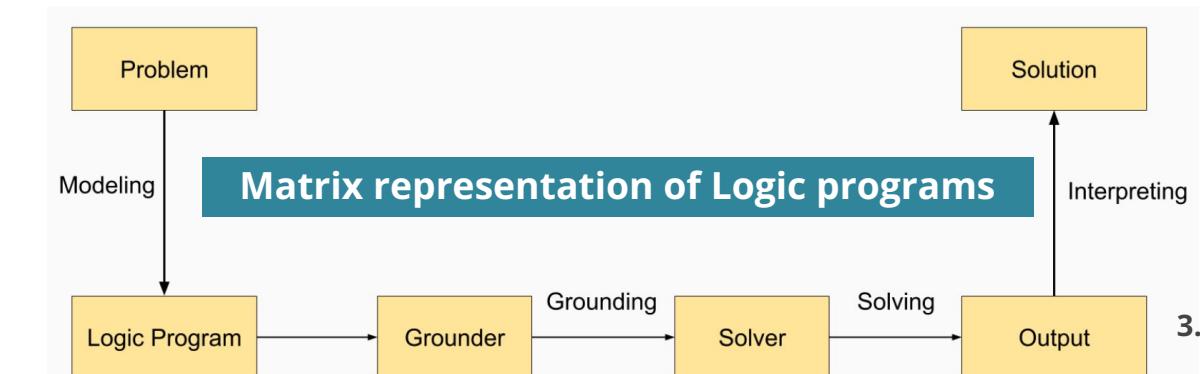


# On Linear Algebraic Computation for Logic Programming - Deduction



Tuan Nguyen Quoc  
(Doctoral student)

 <https://profile.nqtuhan0192.me/>



$$P = \{p \leftarrow q \wedge s, q \leftarrow p \wedge t, s \leftarrow \neg t, t \leftarrow, u \leftarrow v\}$$

$$\begin{array}{c} p & q & s & t & \neg t & u & v \\ \hline p & 0 & 1/2 & 1/2 & 0 & 0 & 0 \\ q & 1/2 & 0 & 0 & 1/2 & 0 & 0 \\ s & 0 & 0 & 0 & 0 & 1 & 0 \\ t & 0 & 0 & 0 & 1 & 0 & 0 \\ \neg t & 0 & 0 & 0 & 0 & 1 & 0 \\ u & 0 & 0 & 0 & 0 & 0 & 1 \\ v & 0 & 0 & 0 & 0 & 0 & 0 \end{array}$$

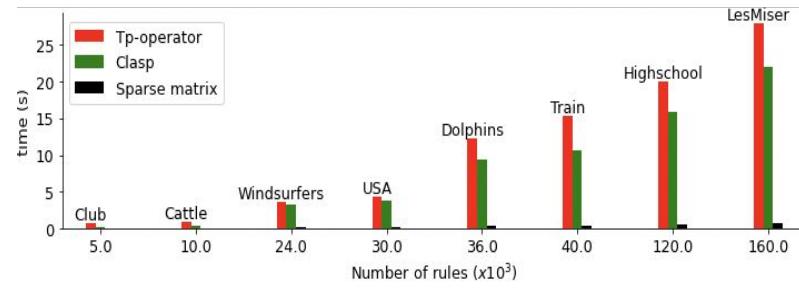
Program matrix

## 2. Perform logic reasoning in vector spaces:

- Deduction  $\frac{P \rightarrow Q}{Q}$
- Abduction  $\frac{Q}{P}$
- Induction  $\frac{P}{Q \rightarrow P}$

## 3. Analyzing the use of matrix in different aspects

- Sparsity
- Differentiability
- Using complex numbers



## 1. Encode logic programs into matrices

- Scalability
- Robustness
- Integrability e.g., ANN

# On Linear Algebraic Computation for Logic Programming - Abduction

## 1. Propositional Horn Clause Abduction

### Problem (PHCAP) with acyclic program

*Example 1:*  $\mathcal{L} = \{p, q, r, s, h_1, h_2, h_3\}$ ,  $\mathbb{H} = \{h_1, h_2, h_3\}$ ,  $\mathbb{O} = \{p\}$ ,

$P = \{p \leftarrow q \wedge r, q \leftarrow h_1 \vee s, r \leftarrow s \vee h_2, s \leftarrow h_3\}$ .

## 2. Matrix representation of Logic programs and its transpose

- flexibility and robustness of numerical computation
- compactness and efficiency of operations
- Integrability e.g., ANN

$$M_P = \begin{pmatrix} p & q & r & s & h_1 & h_2 & h_3 \\ p & 1/2 & 1/2 & & & & \\ q & & & 1 & 1 & & \\ r & & & 1 & & 1 & \\ s & & & & 1 & & \\ h_1 & & & & & 1 & \\ h_2 & & & & & & 1 \\ h_3 & & & & & & & 1 \end{pmatrix}, M_P^T = \begin{pmatrix} p & q & r & s & h_1 & h_2 & h_3 \\ p & 1/2 & & & & & \\ q & & 1/2 & & & & \\ r & & & 1 & 1 & & \\ s & & & & 1 & & \\ h_1 & & & & & 1 & \\ h_2 & & & & & & 1 \\ h_3 & & & & & & & 1 \end{pmatrix}$$

#### Definition

1-step abduction for  $P_{And}$ :

$$M^{(t+1)} = M_P(P_{And})^T \cdot M^{(t)} \quad (1)$$

#### Definition

1-step abduction for  $P_{Or}$ :

$$M^{(t+1)} = \bigcup_{v \in M^{(t)}} \bigcup_{s \in \text{MHS}(\mathbb{S}_{(v, P_{Or})})} \left( (v \setminus \text{head}(P_{Or})) \cup s \right) \quad (2)$$

where:  $\mathbb{S}_{(v, P_{Or})} = \{\text{body}(r_1), \text{body}(r_2), \dots, \text{body}(r_k)\}$  such that  $v \cap \text{head}(P_{Or}) = \{\text{head}(r_1), \text{head}(r_2), \dots, \text{head}(r_k)\}$ .



Tuan Nguyen Quoc  
(Doctoral student)

 dblp  
computer science bibliography  
<https://profile.nqtuhan0192.me/>

$$M^{(0)} = \mathbb{O} = \begin{pmatrix} p & q & r & s & h_1 & h_2 & h_3 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$M^{(1)} = M_P^T \cdot M^{(0)} = \begin{pmatrix} p & q & r & s & h_1 & h_2 & h_3 \\ 0 & 1/2 & 1/2 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\mathbb{S}^{(1)} = \{\{q, r\}\}$$

$$\mathbb{S}_{(M_0^{(1)}, P_{Or})} = \{\{h_1, s\}, \{s, h_2\}\}$$

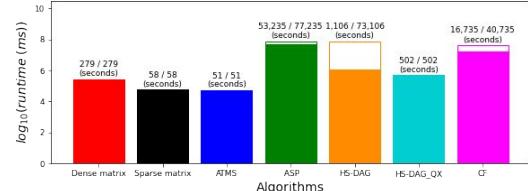
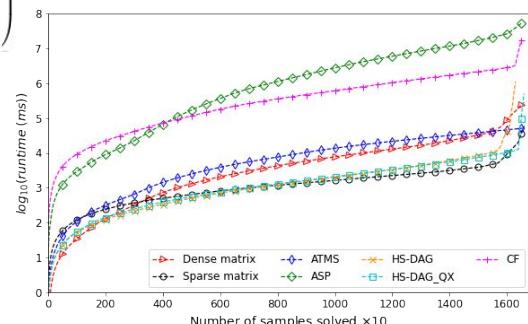
$$\text{MHS}(\mathbb{S}_{(M_0^{(1)}, P_{Or})}) = \{\{s\}, \{h_1, h_2\}\} = M^{(2)}$$

$$M^{(2)} = \begin{pmatrix} p & q & r & s & h_1 & h_2 & h_3 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 \end{pmatrix}$$

$$M^{(3)} = M_P^T \cdot M^{(2)} = \begin{pmatrix} p & q & r & s & h_1 & h_2 & h_3 \\ 0 & 0 & 0 & 0 & 1/2 & 1/2 & 0 \end{pmatrix}$$

$$\mathbb{E} = \{\{h_3\}, \{h_1, h_2\}\}$$

## 4. Experimental results

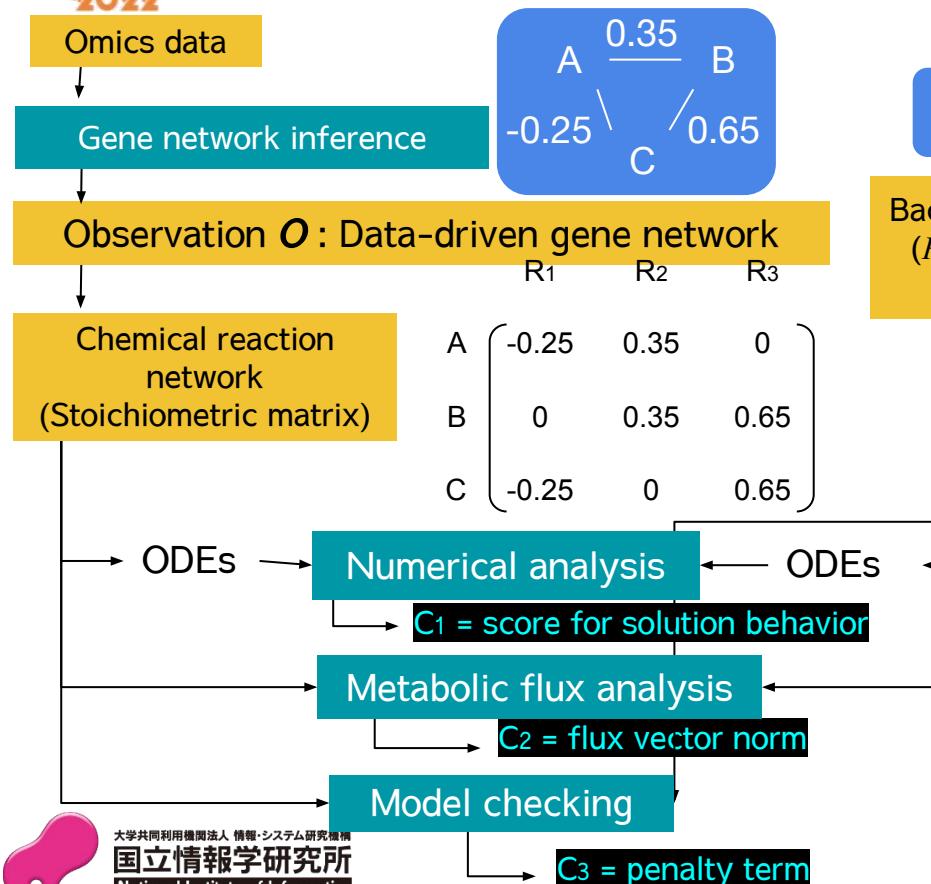




# Learning and Inference of COVID-19 Causal Networks in Continuous Algebraic Space



**ODAKA, Mitsuhiro**   
(5-Year Doctoral Student)  
<https://mitsuhiro-odaka.github.io>



Background knowledge  $\mathcal{B}$  : Knowledge bases  
(*Pathway Commons* V *BioGRID* V *STRING* V  
*KEGG* V *Signor 2.0*)

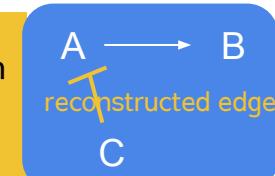
	R <sub>1</sub>	R <sub>2</sub>	R <sub>3</sub>
A	0	-1	0
B	0	1	0
C	0	0	0

Learning edge weights (initial values: 2nd partial corr. coeff.)  
Differentiable cost function =  $C_1 + C_2 + C_3$

$$\begin{array}{ccc}
 A & \left( \begin{array}{ccc} -0.85 & -0.95 & 0 \end{array} \right) & A & \left( \begin{array}{ccc} -1 & -1 & 0 \end{array} \right) \\
 B & \left( \begin{array}{ccc} 0 & 0.75 & 0.05 \end{array} \right) & B & \left( \begin{array}{ccc} 0 & 1 & 0 \end{array} \right) \\
 C & \left( \begin{array}{ccc} -0.95^* & 0 & 0.05 \end{array} \right) & C & \left( \begin{array}{ccc} -1^* & 0 & 0 \end{array} \right)
 \end{array}$$

Thresholding

**Abducibles  $H$ :**  
Chemical reaction network inferred from  
omics data and satisfying qualitative  
property of dynamical behavior of  
models from knowledge bases

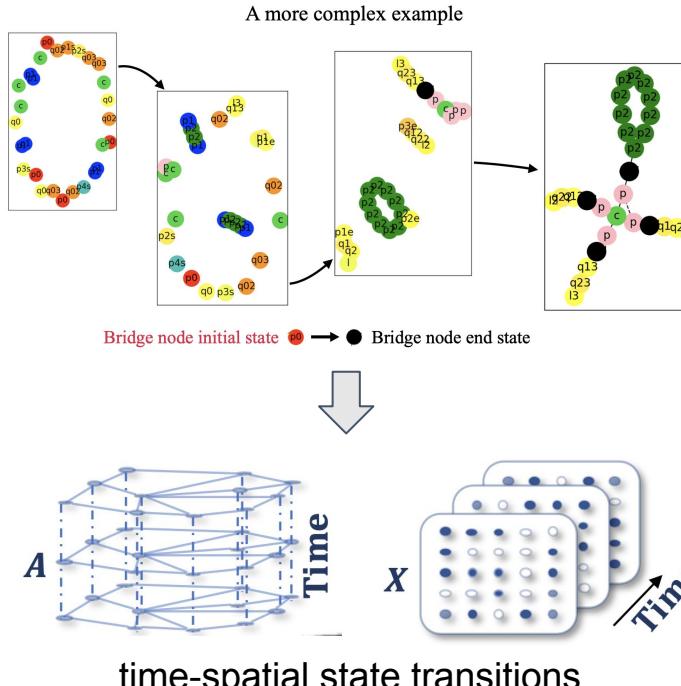


# Network Constructor for rule-learning from transitions

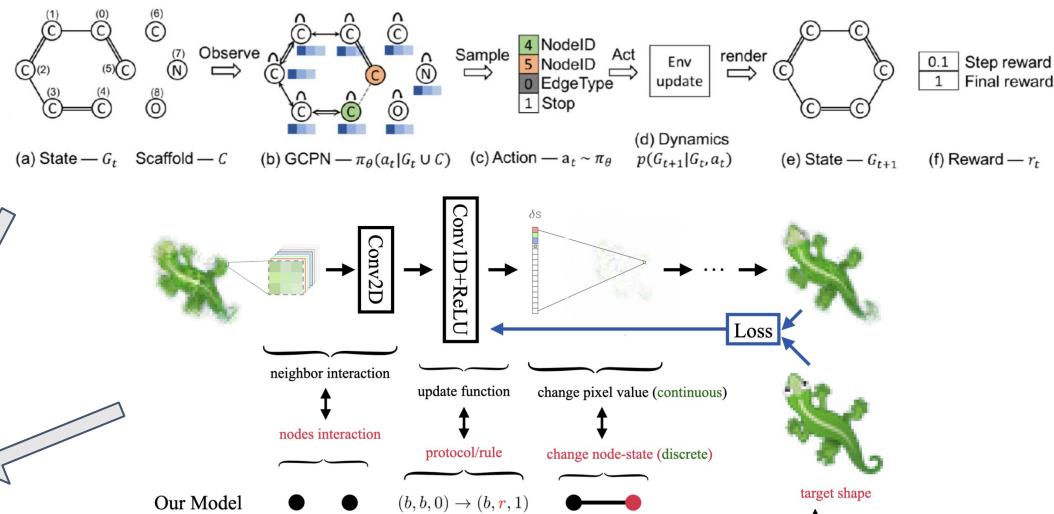


Xu Fanqing  
(3-Year Doctoral Student)

1. Population protocol model\* to create target shape



2. Neuro-graph models creating transitions of target shape



3. Extract constructing rules from transitions  
[protocol-like rules, other logic rules with state information]

$$\delta : Q \times Q \times \{0,1\} \rightarrow Q \times Q \times \{0,1\}$$

→ further interpretation and application

# Neural differentiable SAT solver

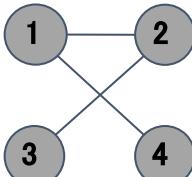


Koji Watanabe  
(5-Year Doctoral Student)



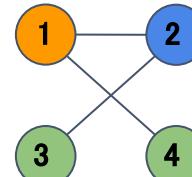
## Problem

1	7	2	4	6		9	3
2	3		7	8	9	5	1
9	4		1	3	7		2
3	6	9	7	2	1	5	
5	7	1		8	2	3	
8	2	4	3	1	9	7	6
1	5	6		3	8	9	
8	3	1	9		4	2	7
7	2	8	3		1	5	



## Solution

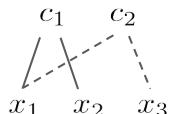
1	5	7	2	4	6	8	9	3
2	3	6	7	8	9	5	4	1
9	4	8	5	1	3	7	6	2
3	6	9	4	7	2	1	5	8
5	7	1	9	6	8	2	3	4
8	2	4	3	5	1	9	7	6
4	1	5	6	2	7	3	8	9
6	8	3	1	9	5	4	2	7
7	9	2	8	3	4	6	1	5



## Representation

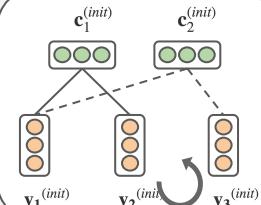
$$S = (x_1 \vee \neg x_2 \vee x_3) \wedge (\neg x_1 \vee x_2 \vee \neg x_3)$$

$$Q = \begin{pmatrix} 1 & 0 & 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 & 0 & 1 \end{pmatrix}$$



## Solving

### DeepLearning

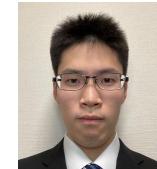


### SAT Solver

Systematic Search  
Stochastic Local Search  
Mathematical Optimization

**Boolean Satisfiability Problem (SAT)** is one of the major problem in logical reasoning and computer science. Existing SAT solvers can solve large-scale problems in a short time, but they require expertise and experience to design algorithms and heuristics suitable for the problem. Therefore, we aim to build a **Neural Differentiable SAT Solver** which can learn how to solve these problems by integrating Deep Learning and differentiable inference/search techniques. SAT solving by deep learning is a topic that is beginning to attract worldwide attention, but there is no established method, making it a promising and challenging research topic.

# Towards Learning Live-cell Dynamics



Ryota Yakushiji  
(Master Student)

